## Folding funnels in energy landscapes

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- native (target) structure very different from unfolded chain
- huge configuration space, rugged energy landscape: many local minima.
- how does the molecule "find" the global target state?





from National Partnership for Advanced Computational Infrastructure website

## Dynamics on a discrete landscape

We define an energy landscape over a state space X by an energy function E and a move set M

$$E: X \to \mathbb{R}, M: X \to \mathcal{P}(X - \{x\})$$

Transition probabilities (Metropolis dynamics)

$$p(y|x) = \frac{1}{|M(y)|} \min\{1, \exp(-\beta(E_y - E_x))\} \quad \text{for } y \in M(x)$$
  
and

$$p(x|x) = 1 - \sum_{y \in M(x)} p(y|x)$$

Expected times  $\tau_x$  it takes to go from a state x to a target state fulfill

$$\tau_x = \sum_{y \in M(x) \cup \{x\}} p(y|x)\tau_y + 1 .$$

with  $\tau_0 = 0$  (target state).

## Time to target in one dimension



6

- The system leaves the basin of a local minimum via the lowest saddle with the highest probability (neglecting entropy effects).
- Rough deterministic approximation of the dynamics: Jump to the minimum reachable over the lowest saddle. Iterate this.
- Folding funnel: Set of all starting states (structures) from which the sequence of steps over the lowest saddles eventually leads to the ground state.

## Geometric definition of a funnel

Define the funnel recursively as the following set F of states:

- 1. (1) The ground state is contained in F.
- 2. (2) The local minimum x belongs to funnel F if a minimum saddle connects it directly to local minimum in the funnel F.
- 3. (3) A state z belongs to the funnel if it is connected by a gradient descent path to a local minimum in F.



Random instance of the number partitioning problem of size 8.



xbix sequence: CUGCGGCUUUGGCUCUAGCC



- Rigorous and simple definition of *funnel* in arbitrary energy landscape.
- Energy landscapes of well-folding RNA sequences have large ground state funnels.
- Next step: examine funnels of protein folding landscapes

Work supported in part by the EMBIO project in FP-6.