# What/when causal expectation modeling in monophonic pitched melodies and percussive audio 

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## Outline

- Goals
- Background
- System Design
- Evaluation
- Future Work
- Conclusions


## Goals

- Build a system for producing musical expectations based on the observation of musical audio
- The system has to be unsupervised and causal to respect cognitive constraints
- this enables to study the effect of exposure

A use case for musical sequence learning models

- what/when expectation task
- As a first step, we focus on constant tempo musical patterns
- Drum loops
- Monophonic Pitched Melodies


## Background

- Prediction-driven listening [Ellis, Abdallah]
- Symbolic pitch sequences learning systems
- [Todd, Mozer, Tillmann, Eck \& Schmidhuber, Pearce \& Wiggins]
- Bayesian score following and accompaniment of audio signals
- [Raphael, Cemgil, Orio]
- Unsupervised learning and concatenative synthesis
- [Schwarz, Jehan]
- Improvisation systems
- [Pachet, Assayag, Dubnov, Cont]


## System Design

## Audio to Symbolic



## Symbolic to Audio

## Feature Extraction Module

Extracts on-the-fly the following features:

- Beats [Davis et al. 2005]
- Onsets (High frequency content based)
- meter description is not explicitly modeled
- Timbre Descriptors
- rough spectral shape (ZCR, SC)
- MFCC
- pitch (YIN-FFT, [Brossier 2004])
- Timbre descriptors can be computed on the onset frame (fast), or averaged over the IOI region


## Feature Extraction Module: output



## Onsets

## Beats

## Dimensionality Reduction Module

- On-line unsupervised clustering to create symbols for both temporal and timbre features
- Prior to this, we perform a bootstrap step
- Accumulates timbre features and beat-relative IOI
- We normalize the timbre
- GMM+EM grid, choose best number of components


## Bootstrap GMM+EM grid

- Create GMM grid
- each row is an independent run
- for each row, each column is associated with a GMM with number of components $=1,2, \ldots, K_{\max }$
- Fit each GMM using EM
- Simple regularization procedure to avoid excessively low variances.
- For each model, compute information criterion
- BIC, AIC, AICc
- Get median of best $K$ over each row


## GMM Grid: Example (drums)

Timbre


IOI


## Running state: Online K-Means

- For each incoming point
- Cluster assignment

$$
C(x)=\operatorname{argmin}_{1<j<K}\left\|x-\mu_{j}\right\|^{2}
$$

- Cluster mean update

$$
\Delta \mu_{j}=\eta\left(x-\mu_{j}\right)
$$

- $\eta$ is the learning rate


## Dimensionality Reduction Module: Output (drums)



Timbre Symbols


Clustered Inter-onset intervals (quarter duration)


Unclustered Inter-onset intervals (quarter duration
Time Symbols

## Dimensionality Reduction Module: Output (sung melody)



Timbre Symbols


Clustered Inter-onset intervals (quarter duration)


Unclustered Inter-onset intervals (quarter duration

Time Symbols

## Dimensionality Reduction Module: Output (sung melody)



Timbre Symbols

$$
\eta=0.9
$$

Clustered Inter-onset intervals (quarter duration)


Unclustered Inter-onset intervals (quarter duration

Time Symbols

## Dimensionality Reduction Module: Output (sung melody)



Timbre Symbols
Time Symbols

## Prediction By Partial Match [Cleary\&Witten, Pearce\&Wiggins]

- probability of next symbol given context sequence

$$
p\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right)= \begin{cases}\alpha\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right) & \text { if } c\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right)>0 \\ \gamma\left(e_{(i-n)+1}^{i-1}\right) p\left(e_{i} \mid e_{(i-n)+2}^{i-1}\right) & \text { if } c\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right)=0\end{cases}
$$

- $\alpha$ is computed based on the counts of a given symbol after the observed context
- $\gamma$ controls the recursive backoff
- enables to integrate predictions based on lower order contexts when needed
- if symbol never seen before in any context: uniform distribution


## Next Event Prediction Module: output



## Evaluation

- Listening to looped patterns
- We compute a weighted F-Measure to compare transcription and expectation
- weights needed because unused clusters can appear

$$
W F M=\sum_{i=1}^{K_{t}} w_{i} F_{i}
$$

- The systems performs twice better than using random predictors


## Evaluation: Drums and Sung Melody

- Drums: WFM histogram



- Drums: Depending of descriptor set

| ZCR, SC | MFCC |
| :--- | :--- |
| $0.60(3.22,2.33)$ | $0.69(1.50,2.42)$ |

- Sung Melodies

| Excerpt | Folk.1 | Folk.2 | Folk.3 |
| :--- | :---: | :---: | :---: |
| Exp.2 | $0.08(7,4)$ | $0.32(5,3)$ | $0.24(5,3)$ |
| Exp.4 | $0.22(6,4)$ | $0.34(6,3)$ | $0.25(5,5)$ |
| Exp.8 | $0.64(7,5)$ | $0.53(7,3)$ | $0.37(5,2)$ |

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## Expectation Entropy

- PPM gives posterior distribution over possible next symbol
- We compute expectation entropy

$$
H(p)=-\sum_{K} p\left(e_{i}\right) \log _{2} p\left(e_{i}\right)
$$



## Expectation Entropy




Music

## Concatenative Synthesis

- [Schwarz, Jehan]
- For each predicted timbre symbol, concatenate in output stream a prototypical audio slice of this symbol having the predicted IOI length
- Examples
- Drums
- Melody


## Discussion

- Bootstrapping is cheating
- Cheat more: define a timbre and timing distance based on a whole collection
- Bootstrap step run in parallel instead of once [Marxer]
- allows to track variations in the attended signal
- clusters can appear and disappear
- A less discrete system
- from hard to soft cluster assignment [McKay]
- work with transient regions instead of crisp onsets


## Summary

- An on-line and unsupervised system for computing expectation in audio signals
- Can be applied to different kinds of monophonic musical signals
- But the sequential prediction system is purely symbolic and markov-chain based
- Expectation entropy may be used to mark temporal cues in the attended signal


## Thanks

Technology

## PPM

$$
\begin{gathered}
\gamma\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right)=\frac{t\left(e_{(i-n)+1}^{i-1}\right)}{\sum_{K} c\left(e_{(i-n)+1}^{i-1}\right)+t\left(e_{(i-n)+1}^{i-1}\right)} \\
\alpha\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right)=\frac{c\left(e_{i} \mid e_{(i-n)+1}^{i-1}\right)}{\sum_{K} c\left(e \mid e_{(i-n)+1}^{i-1}\right)+t\left(e_{(i-n)+1}^{i-1}\right)}
\end{gathered}
$$

