

# Learn to Weight Term in Information Retrieval Using Category Information

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# Outline

- 1 Overview of Term Weighting Methods in Information Retrieval
  - Term Weighting based on TF.IDF
  - Term Weighting based on Language Models
  - Problems with Existing Term Weighting Methods
- 2 Learn Term Weights Using Category Information
  - A Framework for Learning Term Weights Using Category Information
  - A Regression Approach
  - A Probabilistic Approach
- 3 Experiment
  - Experimental Design
  - Baseline Approaches
  - Experimental Results
- 4 Summary

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# Term Weighting Methods based on TF.IDF

- Most popular methods in information retrieval.
- Consist of three factors
  - Term frequency (TF):  $f(w, \mathbf{d})$ 
    - How frequent does the term  $w$  appear in document  $\mathbf{d}$
  - Inverse document frequency (IDF):
    - How rare is term  $w$  in a collection  $\mathcal{C}$

$$idf(w) = \log \left( \frac{N + 0.5}{N(w)} \right)$$

$N$  : the total number of documents in collection  $\mathcal{C}$

$N(w)$  : the number of documents in  $\mathcal{C}$  having word  $w$

- Document normalization factor, e.g.  $\|\mathbf{d}\|_2$ 
  - Reduce the bias of long documents

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## Okapi: An Example of TF.IDF Term Weighting

Similarity between query  $\mathbf{q}$  and document  $\mathbf{d}$  is:

$$sim(\mathbf{d}, \mathbf{q}) = \sum_{w \in \mathbf{q}} \frac{k f(w, \mathbf{q}) f(w, \mathbf{d})}{f(w, \mathbf{d}) + k(1 - b + b \frac{|\mathbf{d}|}{\bar{\mathbf{d}}})} \log \left( \frac{N + 0.5}{N(w)} \right)$$

where

$f(w, \mathbf{q})$  : term frequency of  $w$  in query  $\mathbf{q}$

$f(w, \mathbf{d})$  : term frequency of  $w$  in  $\mathbf{d}$

$\bar{\mathbf{d}}$  : is the average document length of collection  $\mathcal{C}$ .

$k, b$  : weight parameters determined empirically

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# Term Weighting Methods based on Language Models

- Assume each document  $\mathbf{d}$  is generated by a statistical model  $\theta_d$
- Estimate  $\theta_d$  by maximizing likelihood  $p(\mathbf{d}|\theta_d)$
- Usually a smoothing technique, such as Jelinek Mercer smoothing and Dirichlet smoothing, is used to deal with the sparse data problem

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# An Example of Language models for Information Retrieval

- The unigram language model  $p(w|\mathbf{d})$  based on Jelinek Mercer smoothing:

$$\begin{aligned} p(w|\mathbf{d}) &= (1 - \alpha)p(w|\mathcal{C}) + \alpha \frac{f(w, \mathbf{d})}{|\mathbf{d}|} \\ &= p(w|\mathcal{C}) \left( 1 - \alpha + \alpha \frac{f(w, \mathbf{d})}{|\mathbf{d}|p(w|\mathcal{C})} \right) \end{aligned}$$

where  $\alpha$  is a smoothing parameter.

- The similarity of query  $\mathbf{q}$  to document  $\mathbf{d}$  is estimated as

$$\text{sim}(\mathbf{q}, \mathbf{d}) \propto p(\mathbf{q}|\mathbf{d}) \propto \prod_{w \in \mathbf{q}} [p(w|\mathbf{d})]^{f(w, \mathbf{q})}$$



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# Problems with Existing Term Weighting Methods

The essential difficulty with determining term weights is the lack of supervision.

- **Problems with TF.IDF methods**

Either IDF or TF is sufficient to determine if a word is informative.

- IDF factor  $\rightarrow$  rare words are informative words
- But, typos are usually rare and uninformative.

- **Problems with language modeling approaches**

They are generative models  $\rightarrow$

Insufficient to distinguish informative words from uninformative ones

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- Given: each document is assigned to a set of categories
- Goal: learn term weights from the assigned categories of documents
- Main idea:
  - Each document is represented by both a bag of words and a set of categories
  - Compute document similarity based on word  $s_w(\mathbf{d}_i, \mathbf{d}_j)$
  - Compute document similarity based on category  $s_c(\mathbf{d}_i, \mathbf{d}_j)$
  - Find term weights  $\rightarrow s_w(\mathbf{d}_i, \mathbf{d}_j) \approx s_c(\mathbf{d}_i, \mathbf{d}_j)$



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# A Framework for Learning Term Weights Using Category Information

- For each document  $\mathbf{d}_i$ , we have

$$\text{Word based Rep. } \mathbf{w}_i = (w_{i,1}, w_{i,2}, \dots, w_{i,n})^T$$

$$\text{Category based Rep. } \mathbf{c}_i = (c_{i,1}, c_{i,2}, \dots, c_{i,n})^T$$

- Word based document similarity

$$s_w(\mathbf{d}_i, \mathbf{d}_j; \mu) = \sum_{k=1}^m \mu_k w_{i,k} w_{j,k}$$

- Category based document similarity

$$s_c(\mathbf{d}_i, \mathbf{d}_j; \eta) = \sum_{k=1}^m \eta_k c_{i,k} c_{j,k}$$

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# A Framework for Learning Term Weights Using Category Information (Cont'd)

- Find weights  $\eta$  and  $\mu$  s.t.  $s_w(\mathbf{d}_i, \mathbf{d}_j; \mu) \approx s_c(\mathbf{d}_i, \mathbf{d}_j; \eta)$  for any two documents  $\mathbf{d}_i$  and  $\mathbf{d}_j$

$$(\eta^*, \mu^*) = \arg \min_{\eta, \mu} \sum_{i \neq j} l(s_c(\mathbf{d}_i, \mathbf{d}_j; \eta), s_w(\mathbf{d}_i, \mathbf{d}_j; \mu))$$

where  $l(x, y)$  is a loss function measures the difference between  $x$  and  $y$ .

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# A Regression Approach Toward Learning Term Weights

- Define loss function  $l(s_c, s_w) = \|s_c - s_w\|^2$
- Objective function  $\mathcal{F}_{reg}$

$$\mathcal{F}_{reg} = (\eta^T, \mu^T) \begin{pmatrix} Q_c & -P^T \\ -P & Q_w \end{pmatrix} \begin{pmatrix} \eta \\ \mu \end{pmatrix}$$

where

$$[Q_w]_{i,j} = (\mathbf{u}_i^T \mathbf{u}_j)^2, [Q_c]_{i,j} = (\mathbf{v}_i^T \mathbf{v}_j)^2, [P]_{i,j} = (\mathbf{u}_i^T \mathbf{v}_j)^2$$

$\mathbf{u}_i$  : frequency vector for the  $i$ -th term

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# The Regression Approach: Constraints

- Trivial solution  $\eta = \mu = 0 \rightarrow \mathcal{F}_{reg} = 0$
- L2 Constraint:

$$\|\eta\|_2^2 + \|\mu\|_2^2 \geq 1$$

- Problem: negative term weight  $\mu_i < 0$   
 $\rightarrow$  When two documents share word  $w_i$ , they are less likely to be similar
- L1 Constraint:

$$\eta_i \geq 0; \quad \mu_j \geq 0$$

$$\sum_{i=1}^m \eta_i + \sum_{i=1}^n \mu_i \geq 1$$

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# The Regression Approach: Final Form

- Final form for the regression approach

$$\begin{aligned} \min_{\eta, \mu} \quad & (\eta^T, \mu^T) \begin{pmatrix} Q_c & -P^T \\ -P & Q_w \end{pmatrix} \begin{pmatrix} \eta \\ \mu \end{pmatrix} \\ \text{s. t} \quad & \eta \succeq \mathbf{0}, \mu \succeq \mathbf{0} \\ & \|\eta\|_1 + \|\mu\|_1 \geq 1 \end{aligned}$$

- Solve by quadratic programming techniques

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# A Probabilistic Approach Toward Learning Term Weights

- Probability for documents to be similar based on words

$$p_{i,j}^w = \frac{1}{1 + \exp(-s_w(\mathbf{d}_i, \mathbf{d}_j; \mu) + \mu_0)}$$

- Probability for documents to be similar based on categories

$$p_{i,j}^c = \frac{1}{1 + \exp(-s_c(\mathbf{d}_i, \mathbf{d}_j; \eta) + \eta_0)}$$

- Loss function: cross entropy function

$$l(s_c(\mathbf{d}_i, \mathbf{d}_j; \eta), s_w(\mathbf{d}_i, \mathbf{d}_j; \mu)) = -p_{i,j}^c \log p_{i,j}^w - (1 - p_{i,j}^c) \log(1 - p_{i,j}^w)$$



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# The Probabilistic Approach: Final Form

- Objective function  $\mathcal{F}_{prob}$

$$\mathcal{F}_{prob} = \sum_{i \neq j}^N p_{i,j}^c \log p_{i,j}^w + (1 - p_{i,j}^c) \log(1 - p_{i,j}^w)$$

- The final form for the probabilistic approach:

$$\begin{aligned} \arg \max_{\eta, \mu, \eta_0, \mu_0} \quad & \mathcal{F}_{prob} - \alpha_w \sum_{i=1}^n \mu_i - \alpha_c \sum_{i=1}^m \eta_i \\ \text{s. t.} \quad & \eta \succeq 0, \mu \succeq 0 \end{aligned}$$

where  $\alpha_w > 0$  and  $\alpha_c > 0$  are regularization parameters.

# The Probabilistic Approach: Optimization Strategy

## Alternating Optimization

- Learn term weights  $\mu$  with fixed category weights  $\eta$ 
  - Decouple the correlation among  $\mu$

$$\mathcal{F}_{prob}(\mu', \eta) - \mathcal{F}_{prob}(\mu, \eta) \geq \sum_{i=1}^n g_i(\mu'_i - \mu_i)$$

$\mu'$  and  $\mu$  are term weights of two consecutive iterations.

- Solve

$$g'_i(\delta_i) = 0 \rightarrow \mu' = \mu + \delta$$

- Learn category weights  $\eta$  with fixed term weights  $\mu$ 
  - A similar procedure for optimizing  $\eta$  with fixed  $\mu$

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# Experimental Design

- Document collection
  - A document collection from the ad hoc retrieval task of ImageCLEF
  - Totally 28,133 documents, 933 categories
  - Average document length  $\sim 50$
  - Average number of categories for a document  $\sim 5$
- Evaluation Queries
  - 5 queries from ImageCLEF 2003 for training  $\alpha_w$  and  $\alpha_c$
  - 25 queries from ImageCLEF 2004 for testing
- Evaluation metrics
  - Average precision for top retrieved documents
  - Average precision across 11 recall points
  - Precision recall curve



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  - 25 queries from ImageCLEF 2004 for testing
- Evaluation metrics
  - Average precision for top retrieved documents
  - Average precision across 11 recall points
  - Precision recall curve

# Experimental Design

- Document collection
  - A document collection from the ad hoc retrieval task of ImageCLEF
  - Totally 28,133 documents, 933 categories
  - Average document length  $\sim 50$
  - Average number of categories for a document  $\sim 5$
- Evaluation Queries
  - 5 queries from ImageCLEF 2003 for training  $\alpha_w$  and  $\alpha_c$
  - 25 queries from ImageCLEF 2004 for testing
- Evaluation metrics
  - Average precision for top retrieved documents
  - Average precision across 11 recall points
  - Precision recall curve

# Outline

- 1 Overview of Term Weighting Methods in Information Retrieval
  - Term Weighting based on TF.IDF
  - Term Weighting based on Language Models
  - Problems with Existing Term Weighting Methods
- 2 Learn Term Weights Using Category Information
  - A Framework for Learning Term Weights Using Category Information
  - A Regression Approach
  - A Probabilistic Approach
- 3 **Experiment**
  - Experimental Design
  - **Baseline Approaches**
  - Experimental Results
- 4 Summary

# Baseline Approaches

- State-of-art information retrieval methods
  - The Okapi method (**Okapi**)
  - The language model with JM smoothing (**LM**)
- Inverse category frequency (**ICF**)

$$icf(w) = \log \left( \frac{m}{m(w)} \right)$$

$m(w)$  : number of categories having word  $w$

- Replace  $idf(w)$  with  $icf(w)$  in the Okapi method

## Baseline Approaches (Cont'd)

- Category-based query expansion (**CQE**)

- 1 Retrieve top  $k = 100$  documents for query  $\mathbf{q}$  using Okapi
- 2 Expand query  $\mathbf{q}$  to include category information

$$\mathbf{q}' = \{f(w_1, \mathbf{q}), \dots, f(w_n, \mathbf{q}); f(c_1, \mathbf{q}), \dots, f(c_m, \mathbf{q})\}$$

$f(c_i, \mathbf{q})$  : the number of top  $k$  documents in category  $c_i$

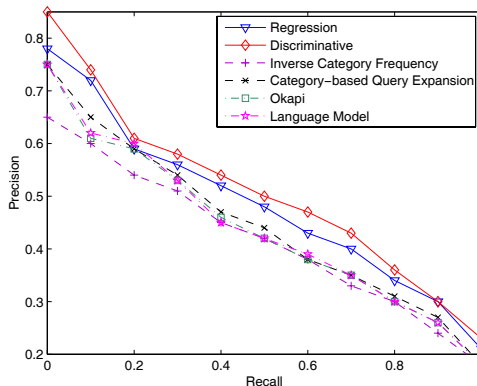
- 3 Retrieve documents using the expanded query  $\mathbf{q}'$

$$\log p(\mathbf{q}'|\mathbf{d}) = \frac{\beta \sum_{i=1}^n f(w_i, \mathbf{q}) \log p(w_i|\mathbf{d})}{\sum_{i=1}^n f(w_i, \mathbf{q})} + \frac{(1 - \beta) \sum_{i=1}^m f(c_i, \mathbf{q}) \log p(c_i|\mathbf{d})}{\sum_{i=1}^m f(c_i, \mathbf{q})}$$

# Outline

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# Precision Recall Curves



- Probabilistic approach > Language Model & Okapi

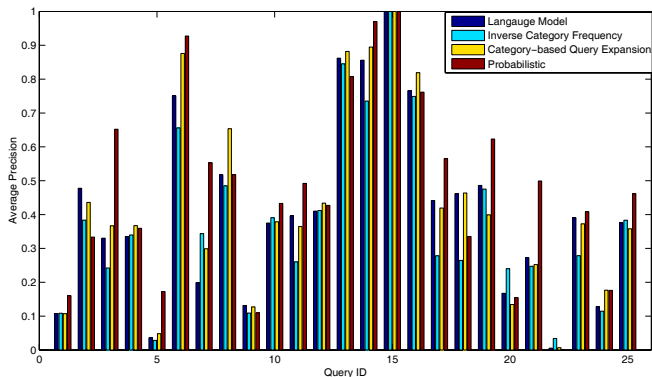
# Average Precision

	Using Category				No Category	
	Reg.	Prob.	ICF	CQE	Okapi	LM
Avg. Prec.	0.45	<b>0.48</b>	0.38	0.42	0.41	0.41
Prec @ 5 doc	0.55	<b>0.56</b>	0.40	0.50	0.47	0.50
Prec @ 10 doc	0.48	<b>0.52</b>	0.40	0.48	0.45	0.48
Prec @ 20 doc	<b>0.46</b>	<b>0.46</b>	0.39	0.42	0.39	0.38
Prec @ 100 doc	<b>0.21</b>	<b>0.21</b>	0.19	0.19	0.20	0.20

- Reg. and Prob. > Okapi and LM
  - Category information is useful
- ICF and CQE < Okapi and LM
  - Need to exploit category information wisely



# Retrieval Precision for Individual Queries



- Over 16 queries, probabilistic approach > language model
- Over 5 queries, probabilistic approach < language model

# Summary

- Proposed two algorithms for learning term weights using category information
  - A regression approach
  - A probabilistic approach
- Empirical studies with the ImageCLEF dataset verify the effectiveness of the proposed algorithms
- Future work
  - Improve learning efficiency for large numbers of documents and large-sized vocabularies
  - Extend to image retrieval for annotated images