

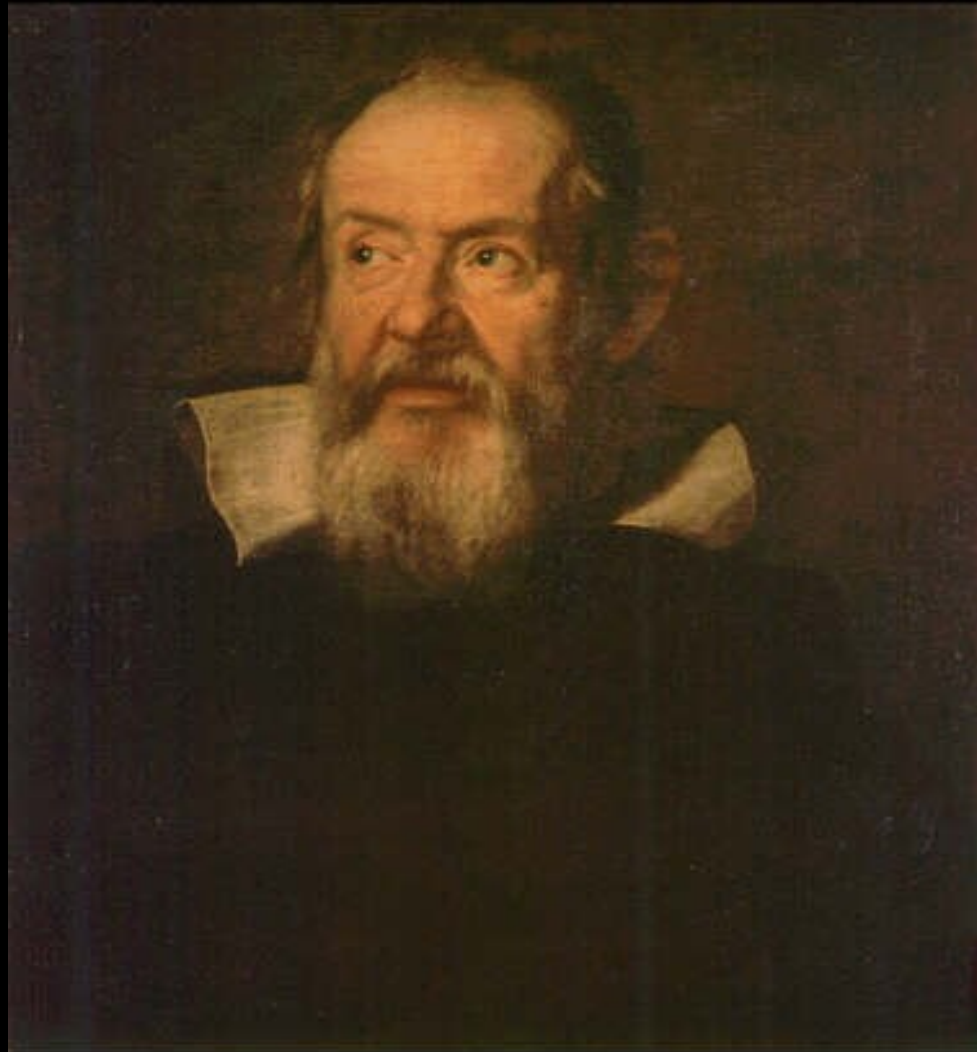
Towards a physics of society

Santo Fortunato

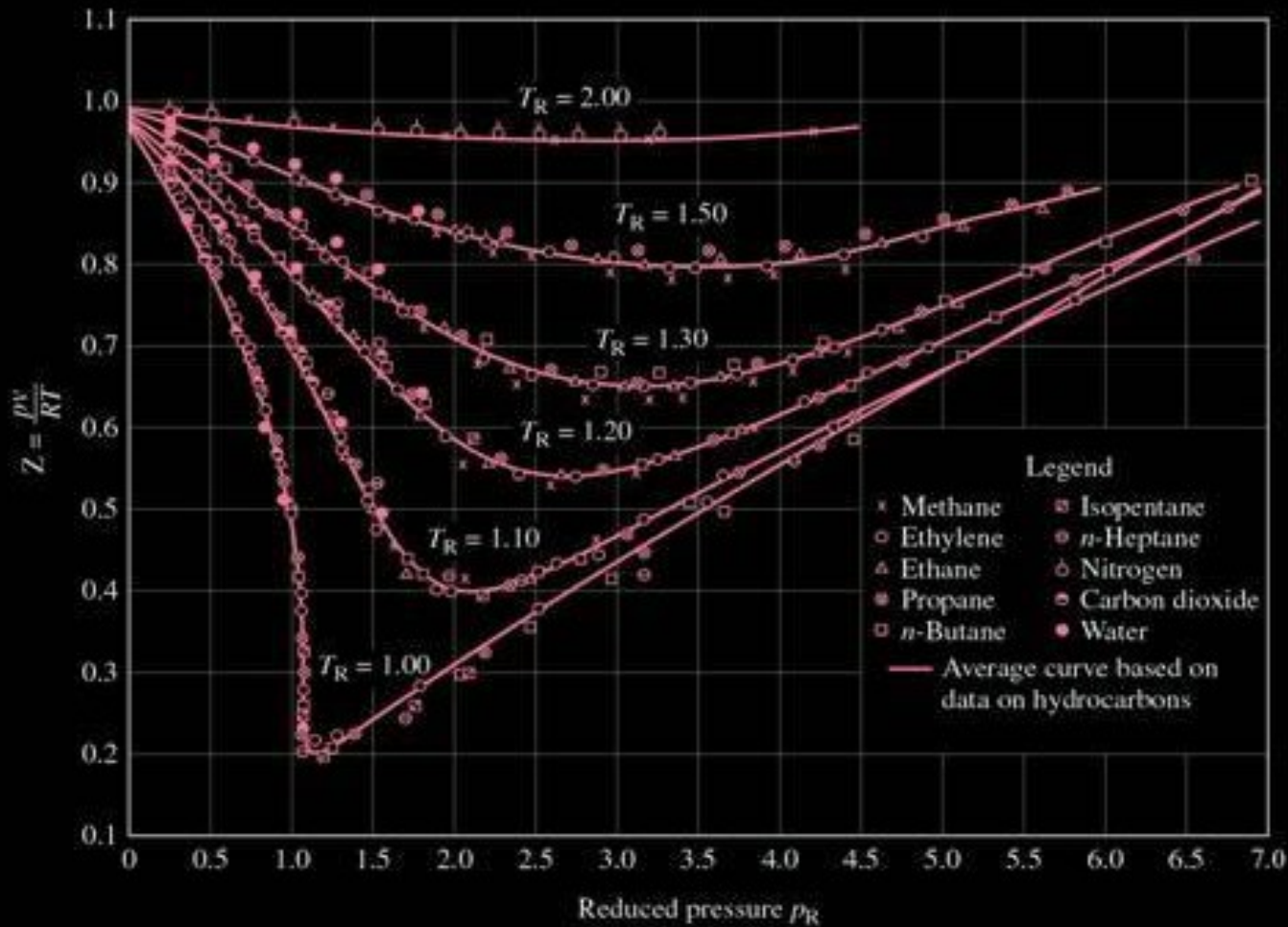


Outline

- **Prologue**
- **Building a phenomenology:**
 - 1) voting behavior**
 - 2) citation behavior**
- **Outlook**



“Measure what is measurable, and make measurable what is not so...”



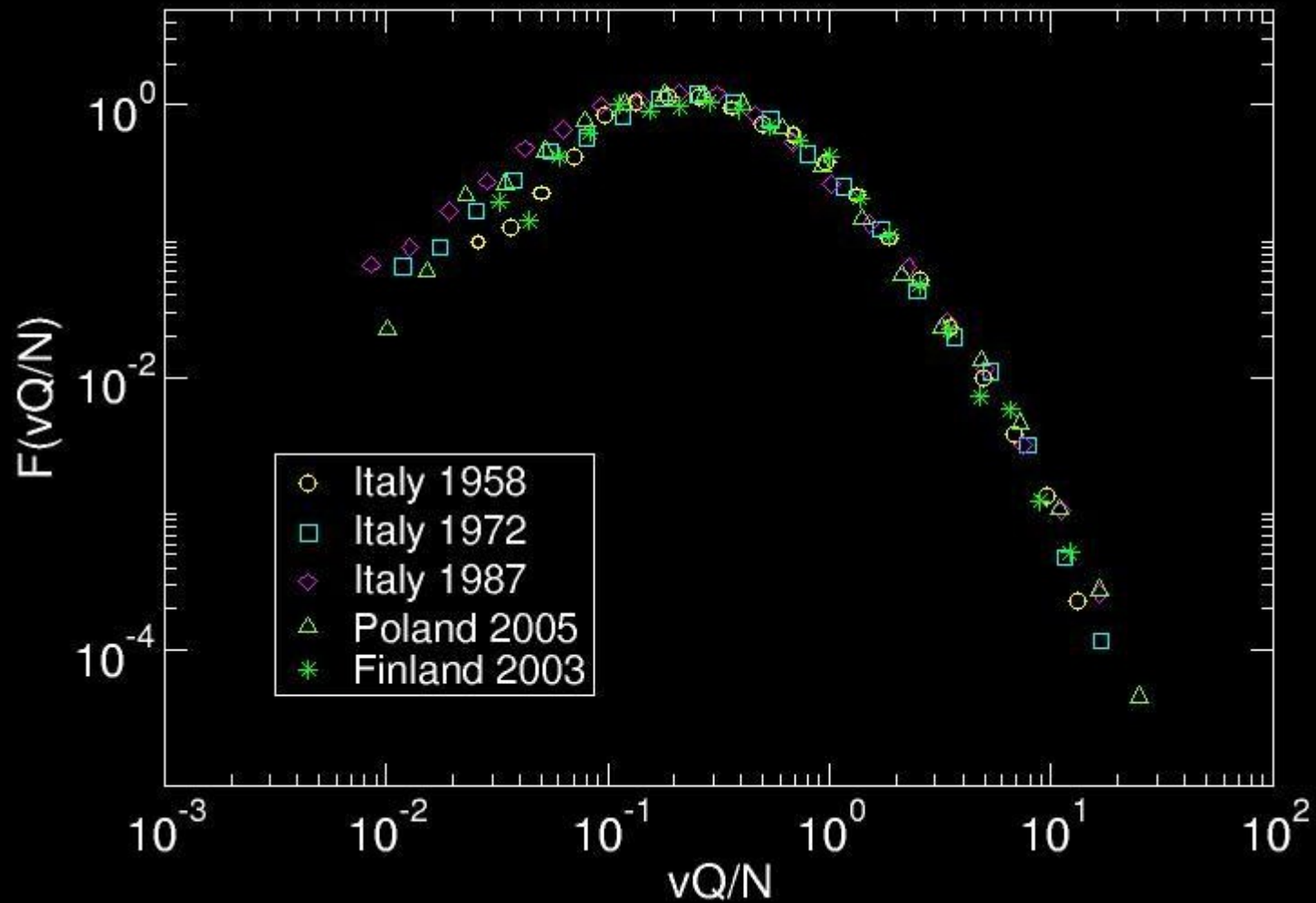
$$T_r = \frac{T}{T_c}$$

$$P_r = \frac{P}{P_c}$$

$$V_r = \frac{V}{V_c}$$

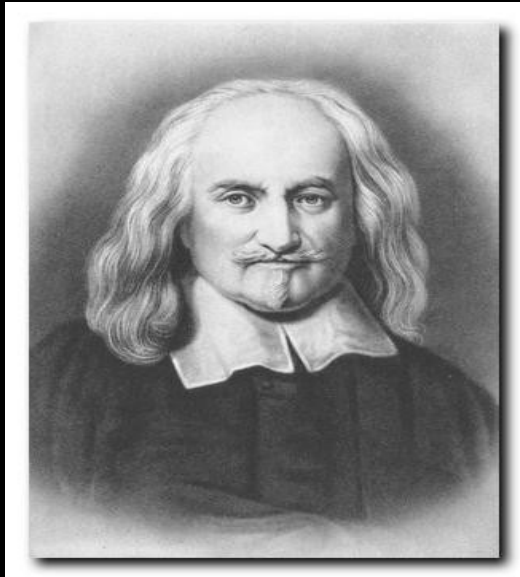
Normalization

Physics

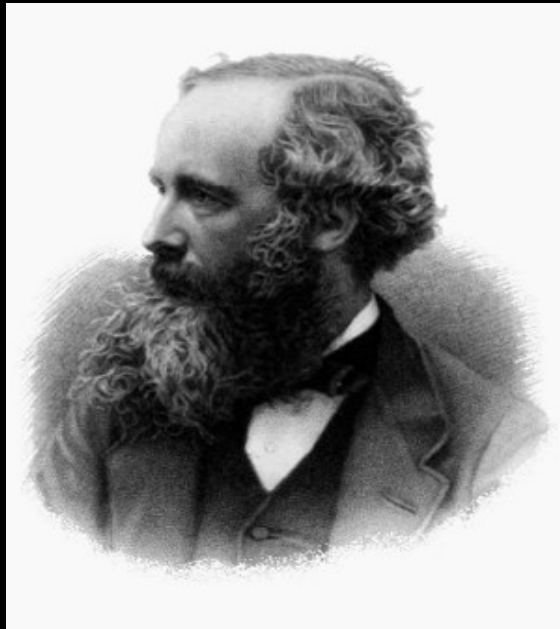


Society!

History



Social statistics: number of births, deaths, crimes, suicides, etc.



From Newtonian mechanics of particles to statistical mechanics to describe gases

Sociophysics



From individuals that interact *locally* to collective behavior and organization.

Risky business!

People are not atoms: their interactions are not reproducible!

Necessary condition: the size of the social groups must be big (large scale behaviour)

In this way, the phenomena won't be much affected by individual features

Interesting aspects for statistical physicists:

- **Large-scale regularities: scaling**
- **Universal features**
- **Microscopic origin of macroscopic behaviour**

Quantitative understanding!

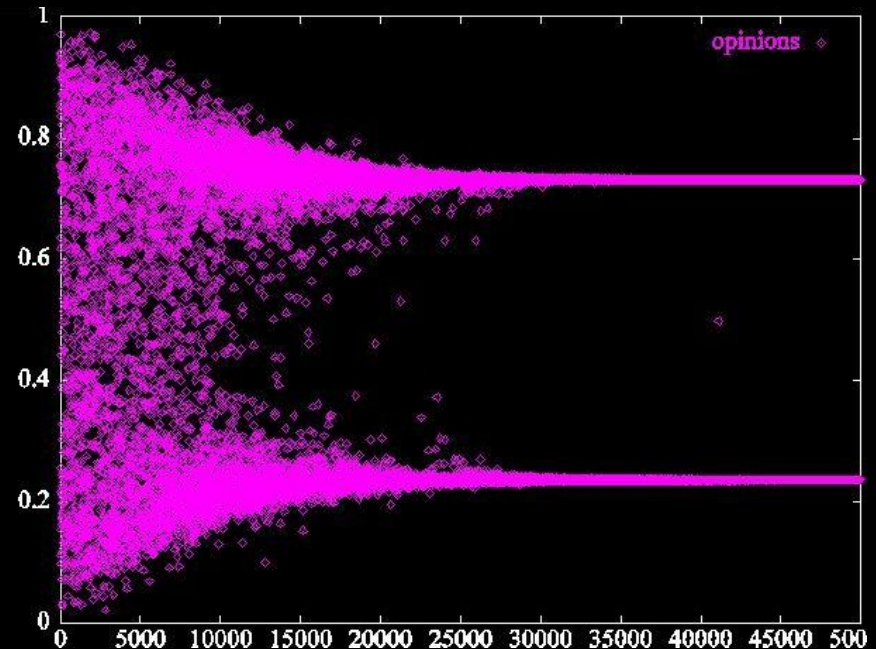
Opinion dynamics

Deffuant et al.(2000)

Opinions are real-valued.

Bounded confidence: opinions need to be close to affect each other

Evolution to one, two or more opinions



Questions

- **Shall we content ourselves with such a qualitative description?**
- **Is it possible to validate this approach?**

Building a phenomenology of social dynamics

**Quantitative characterization of large
scale social phenomena**

- **Voting behavior**
- **Citation behavior**

Elections



- **Large scale social phenomenon**
- **Lots of available data**

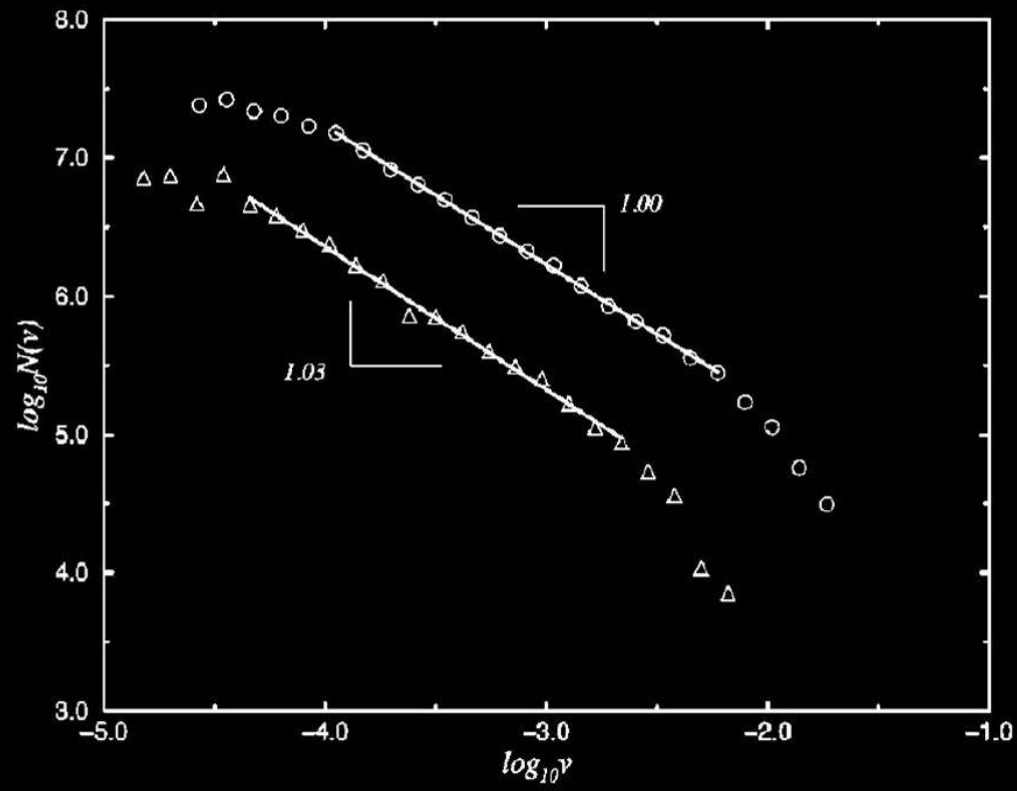
Elections

State elections in Brazil 1998 (Costa Filho et al., PRE, 1999)

**v = # votes received
by a candidate**

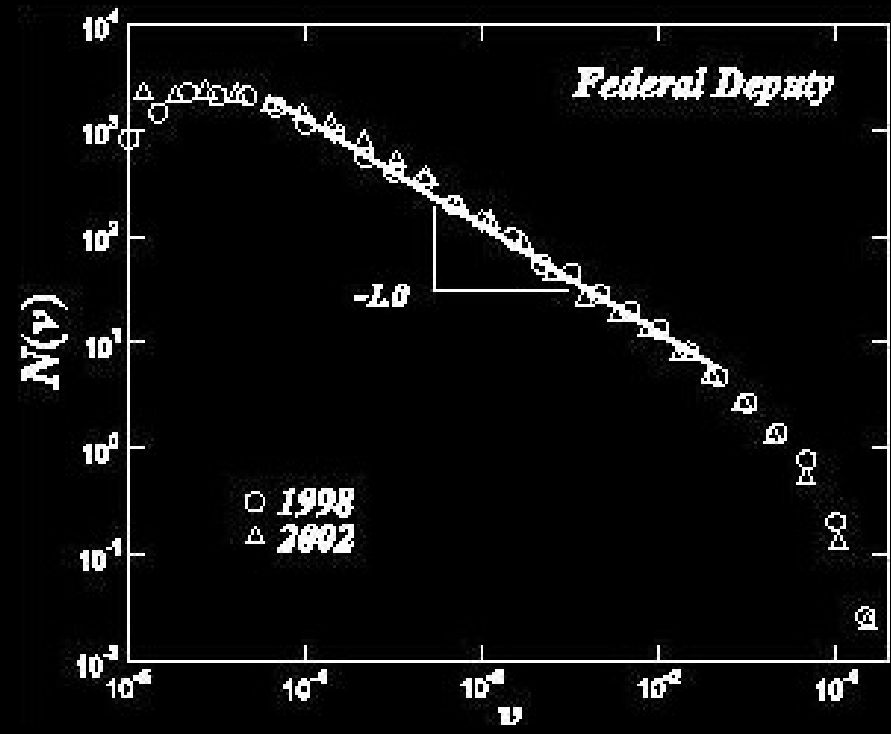
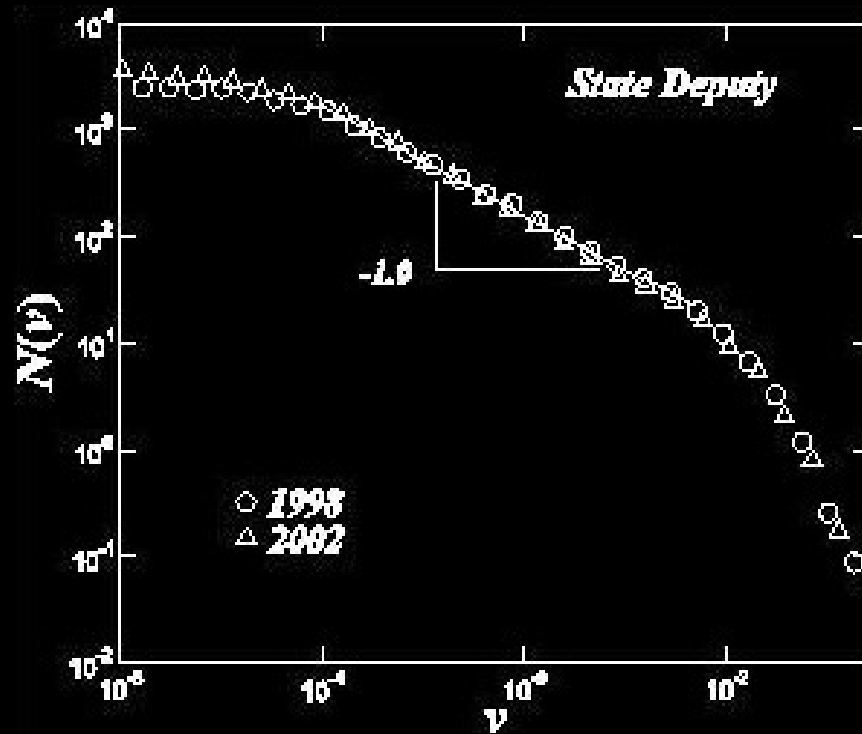
**Focus: distribution of
 v across all
candidates**

$1/v$ behavior



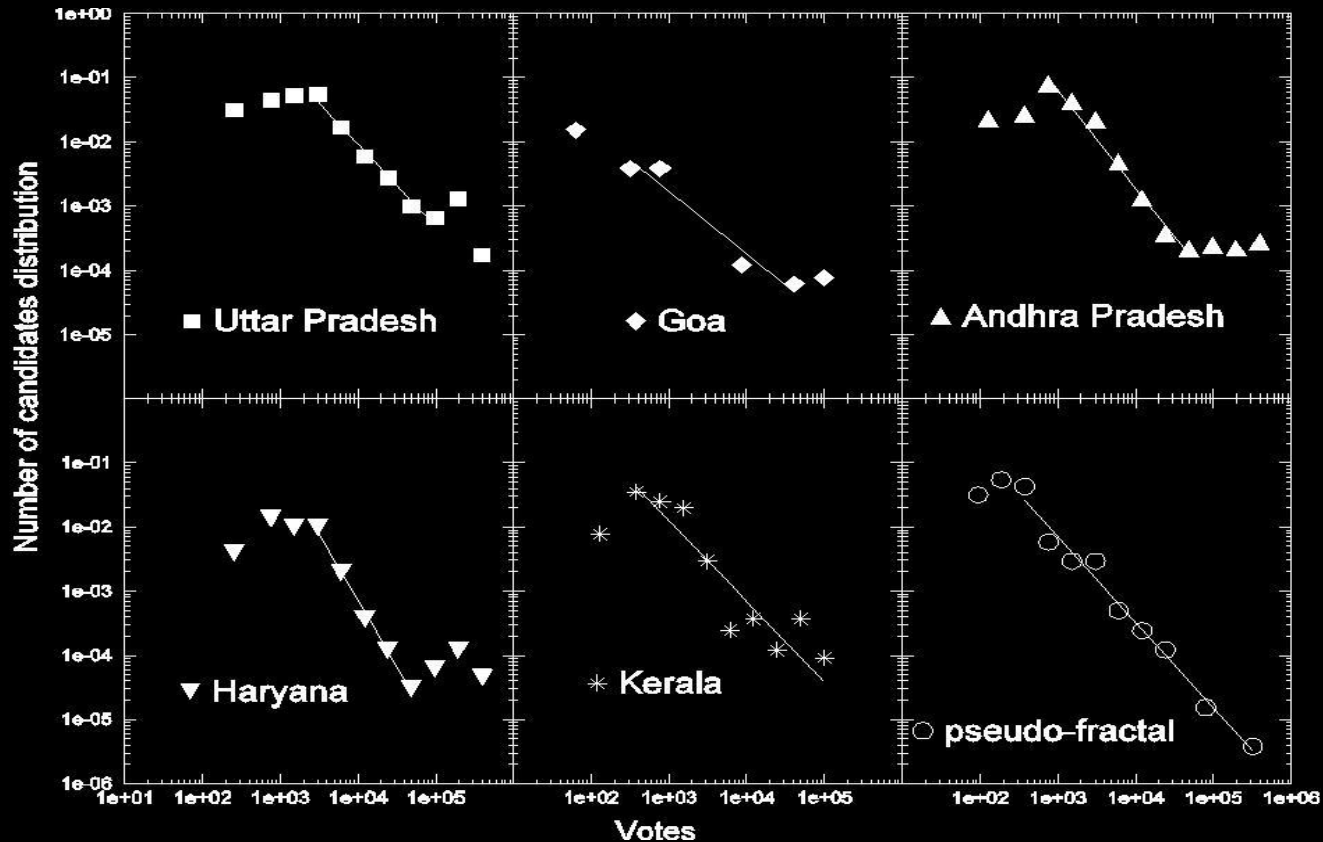
Elections in Brazil 2002

(Costa Filho et al., Physica A 2003)

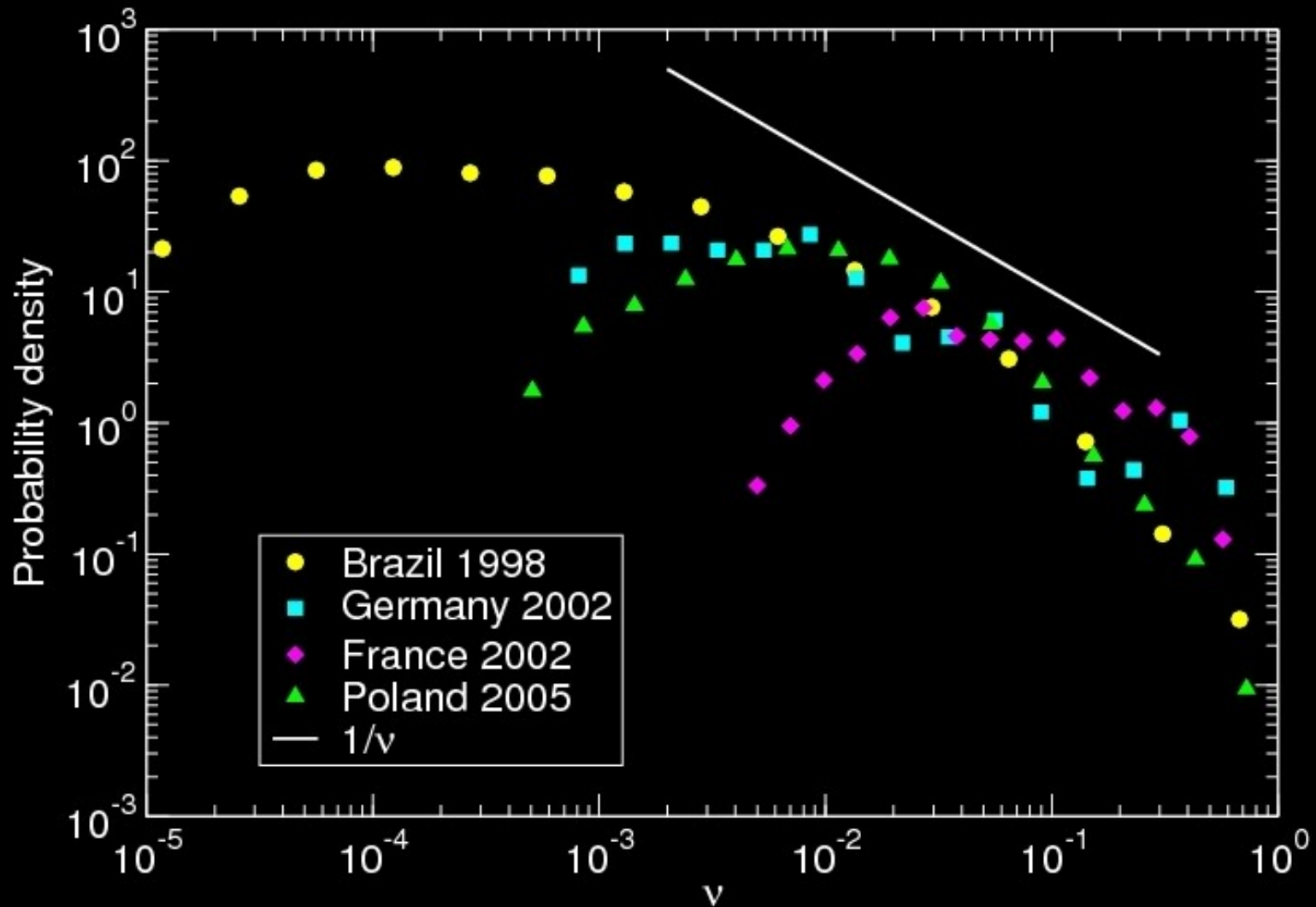


1/v decay reproducible over the years

Indian elections (González et al. IJMPC, 2004)



- **$1/v$ decay occurs in different countries**
- **Is it universal?**



The $1/\nu$ behaviour is not universal!

Problem: is it correct to put together candidates of different parties?

Support for different parties wildly fluctuates, in an unpredictable way !

If we model the competition of candidates of the same party, the party does not play any role!

Candidates are chosen based on some form of contact between them and the voters: model!

A new analysis (S.F. & C. Castellano, Phys. Rev. Lett. 99, 138701, 2007)

Proportional elections with open lists

Examples:

Italy (1946-1992), Poland, Finland

**Distribution of votes for candidates
within a party**

$P(v, Q, N)$

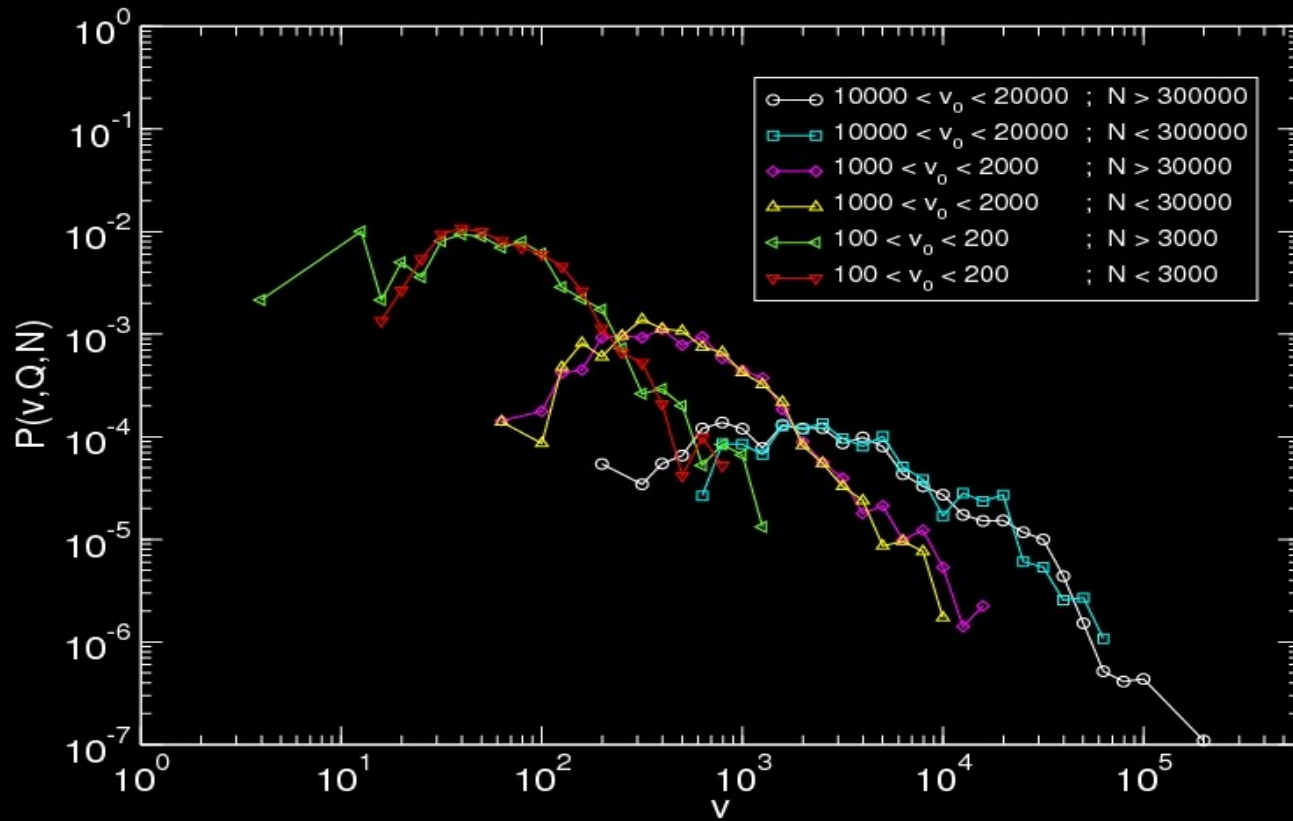
N = total votes for party

**Q = number of party
candidates**

Scaling I

Only two independent variables!

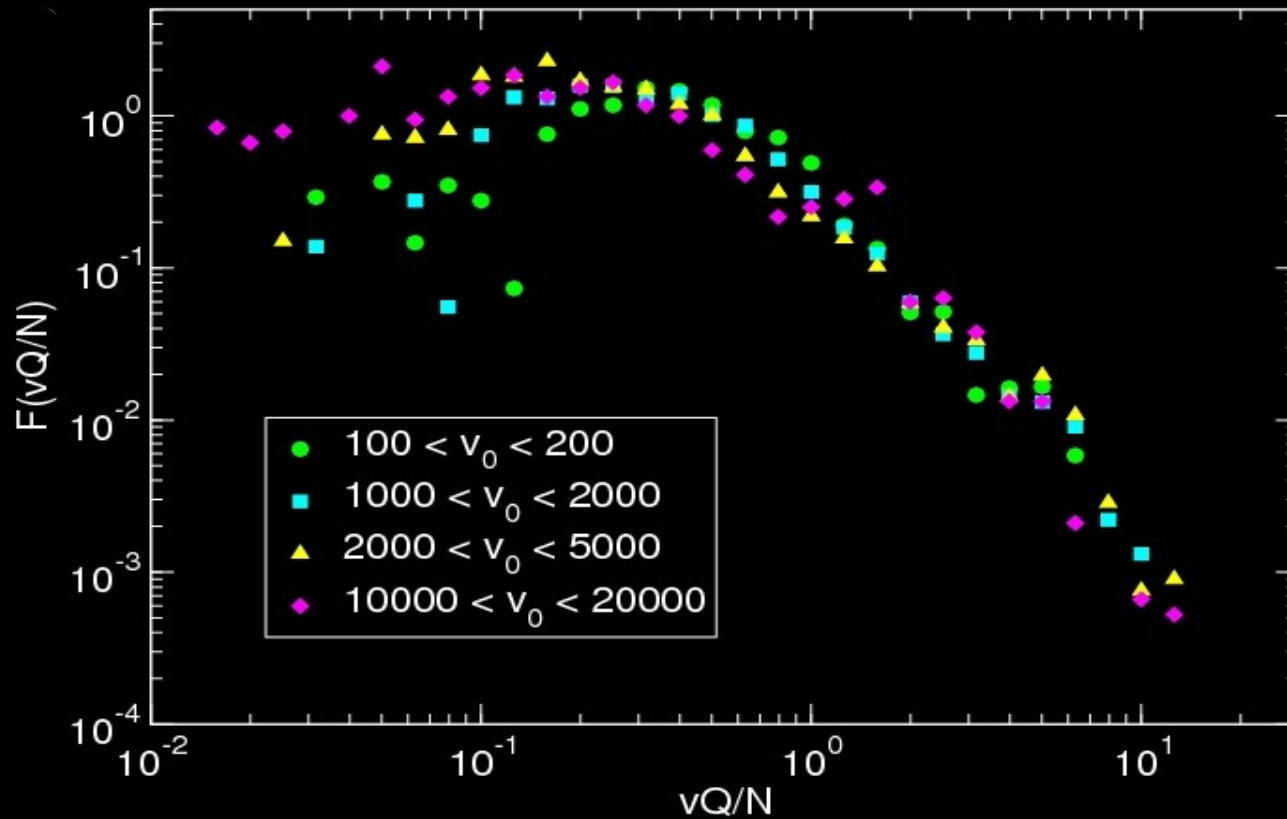
$$P(v, Q, N) = P^*(v, N/Q) = P^*(v, v_0)$$



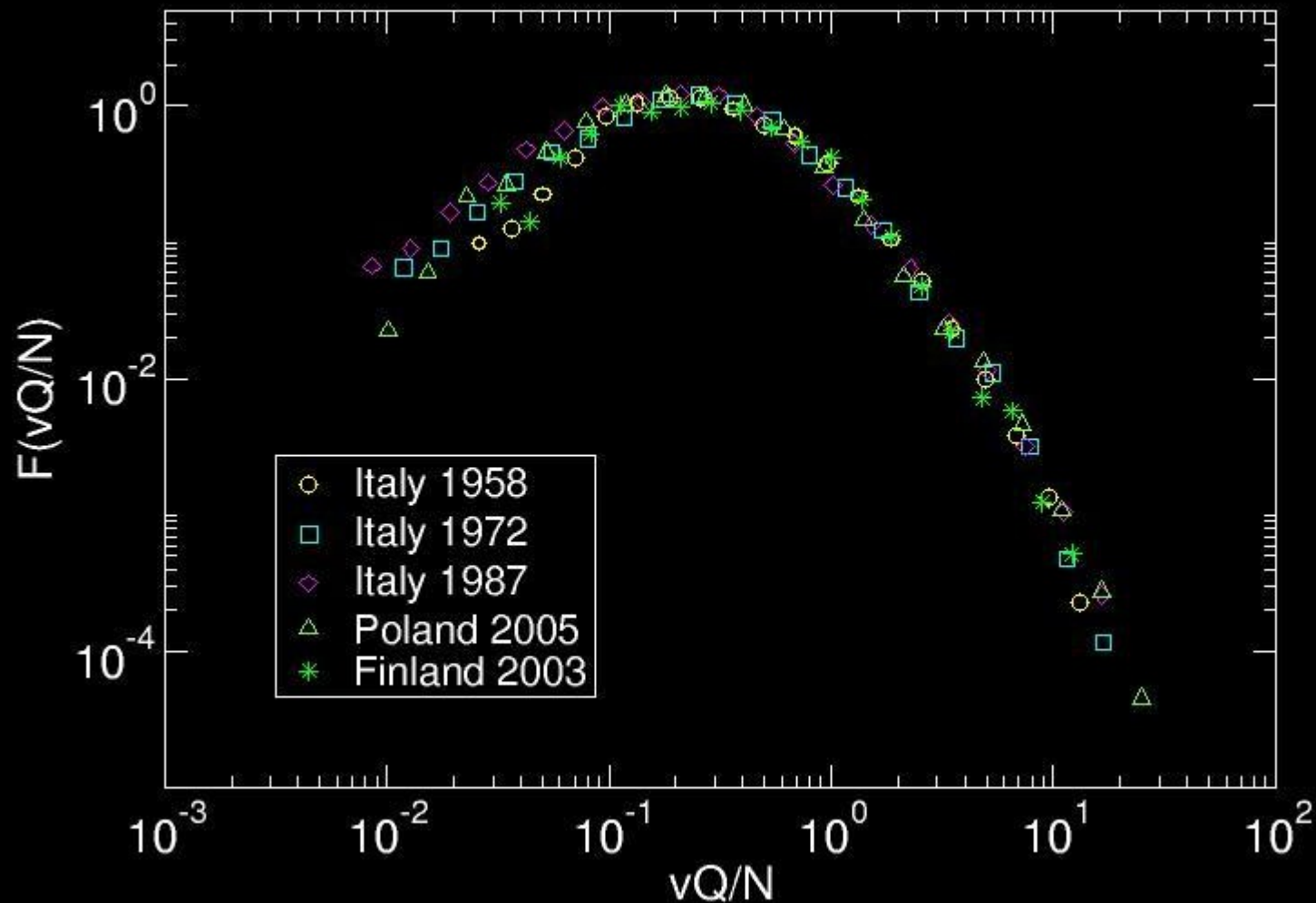
Scaling II

Only one independent variable!

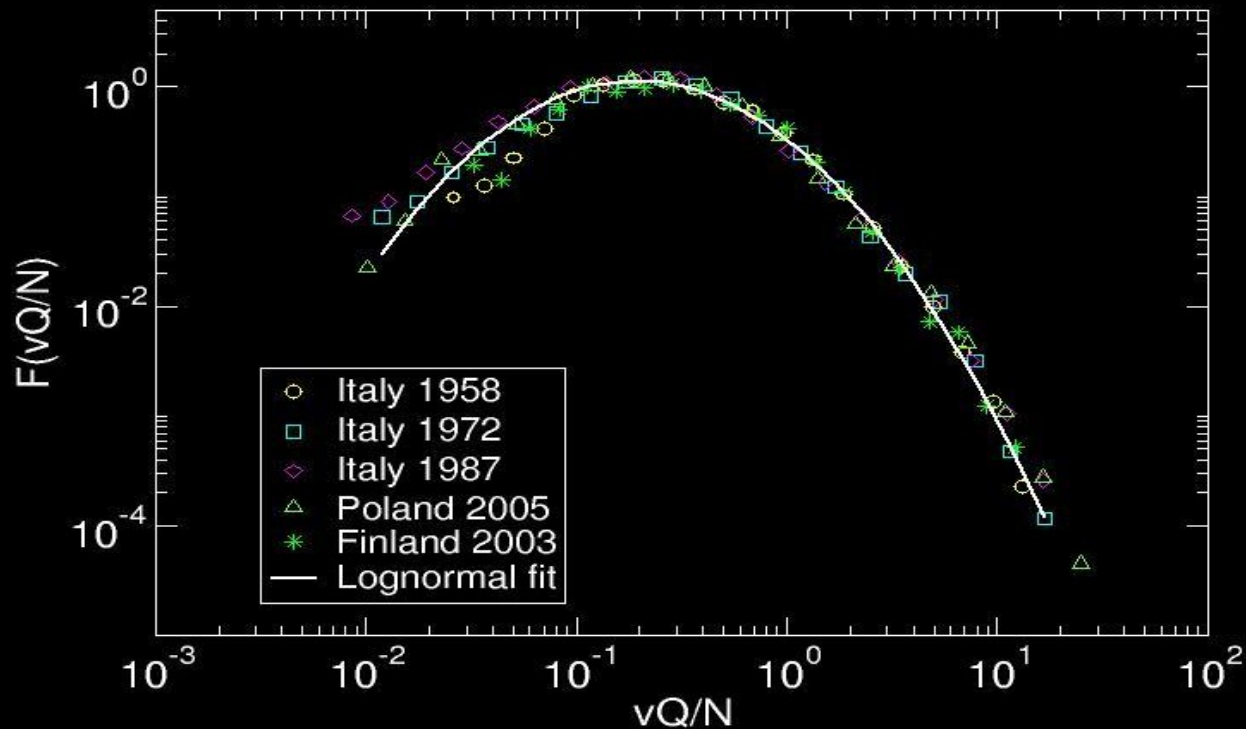
$$\mathbf{P(v,Q,N)=P^*(v,N/Q)= F(vQ/N)!}$$



The scaling function is universal!



The universal curve has a lognormal shape!

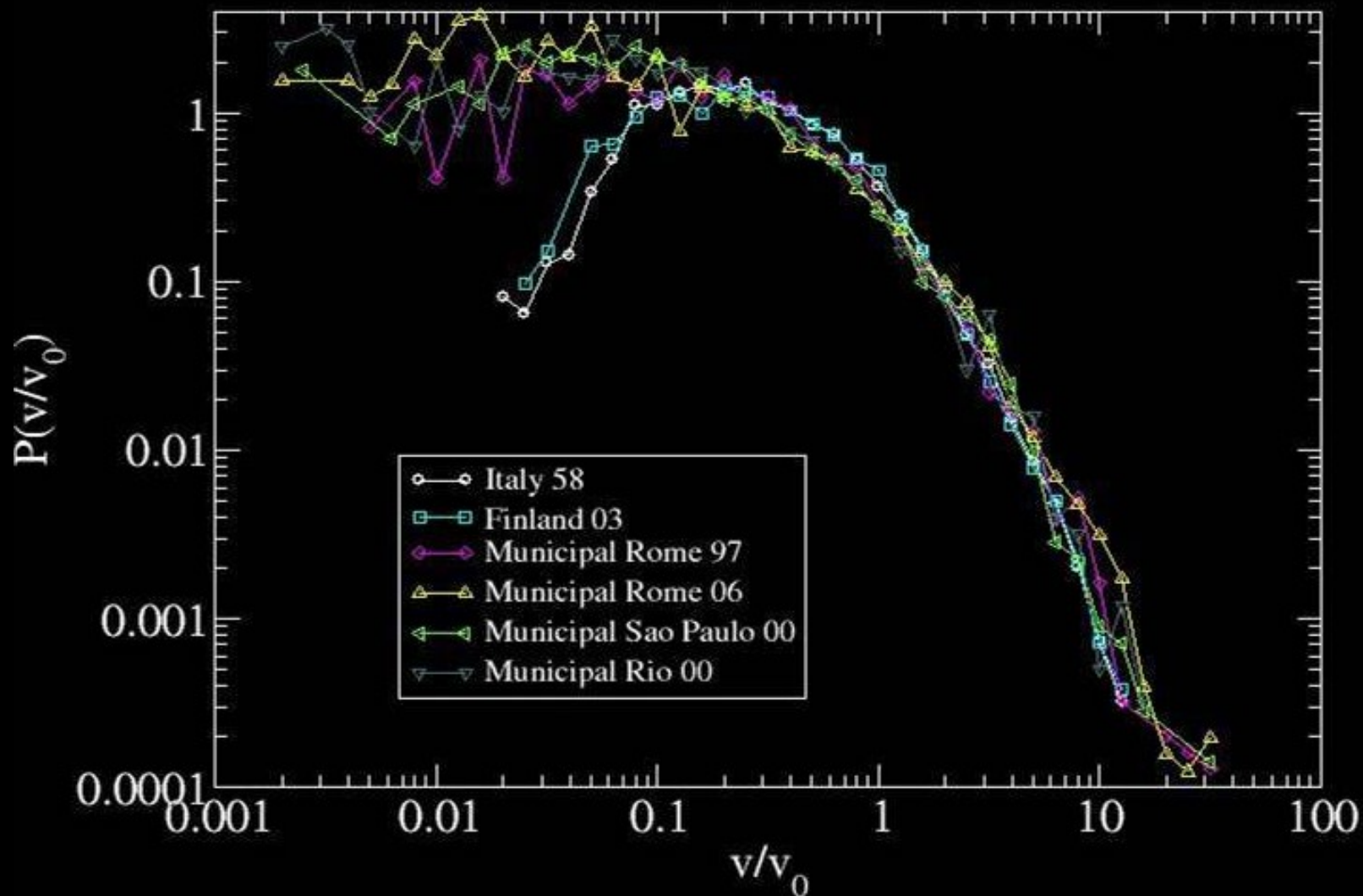


$$F(x) = \frac{1}{\sqrt{2\pi\sigma x}} e^{-(\ln(x)-\mu)^2 / 2\sigma^2}$$

$$\mu = -0.45$$

$$\sigma^2 = 0.91$$

Municipal elections display identical decay



This week

The natural pattern behind our votes

Voting follows the same pattern regardless of country or economics, and it could all be based on networking

MARK BUCHANAN

ARE you swayed by TV and internet voting campaigns? Political parties all over the world certainly think you are, and spend millions on advertising their candidates. Now an analysis of election results over 30 years in different countries shows that, for each political party, voting follows the same pattern, regardless of nationality, culture, history or economics.

The most important factor determining a candidate's success compared with rivals in the same party turns out to be his or her personal ability to connect with the public. In other words, the key factor could be how many friends you've got on Facebook.

"When it comes to voting," says Santo Fortunato of the Institute for Scientific Interchange in Turin, Italy, "people act in the same way regardless of national identity and the economic or political context. Even modern campaign tools like television and the internet have no great effect."

The influence of the candidate's political party and the prevailing

economic conditions usually confound attempts to uncover a voting pattern. Fortunato's approach has revealed that there is indeed a pattern, and that social networking can explain it.

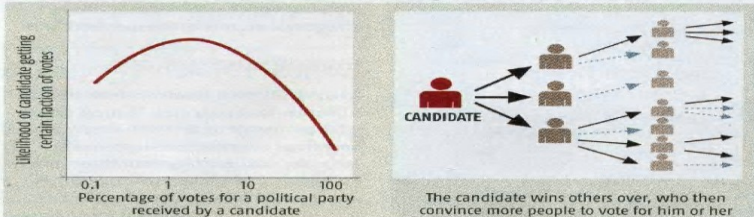
Over the past decade, several independent teams of researchers studying the mathematics of voting behaviour noted an intriguing pattern in election results in countries where elections had many candidates. They found that most candidates received a small number of votes while a few did much better, winning a large fraction of votes.

Looking in detail at elections in Brazil and India, the actual numbers seemed to vary in a regular way: twice as many candidates received 20 per cent as did 40 per cent, twice as many again received 10 per cent as did 20 per cent, and so on. Mathematically, in other words, the number of candidates receiving x per cent of the votes seemed to be simply inversely proportional to x .

However, this didn't seem to be the case in other countries with

A UNIVERSAL PATTERN OF VOTING

When the influence of political parties is removed, a candidate's personal ability to connect with the public is the most important factor influencing the number of votes received



The candidate wins others over, who then convince more people to vote for him or her



MARKUS SPANTEL/ISTOCK

different election systems, says Fortunato. Working with physicist Claudio Castellano of the University of Rome, Fortunato looked at data from elections in Germany, France, Italy and Poland, and found that there appeared to be no pattern across nations or political systems to the numbers of votes received by each candidate, as one might well expect. On closer examination, though, they found that the differences between nations do not seem to be down to political or cultural differences, but instead reflect the differing influence of political parties within each nation. Controlling for this, they have discovered that how votes get divided between candidates really does follow a universal pattern that seems to be

unaffected by political systems, culture or economic conditions.

Voters, they say, can be drawn to vote for a candidate for two main reasons. First, there's the intrinsic appeal of a candidate, based on their personality and character, their articulated positions and ability to connect with the voters. Then there's the influence of political parties, which attract voters to a broad philosophy or set of policies. The distribution of votes between candidates depends on both factors, and so doesn't reflect a candidate's personal attraction alone.

Fortunato and Castellano suspected that there might be a voting pattern hidden by this mingling of influences that held across nations. To test the idea they looked for data from

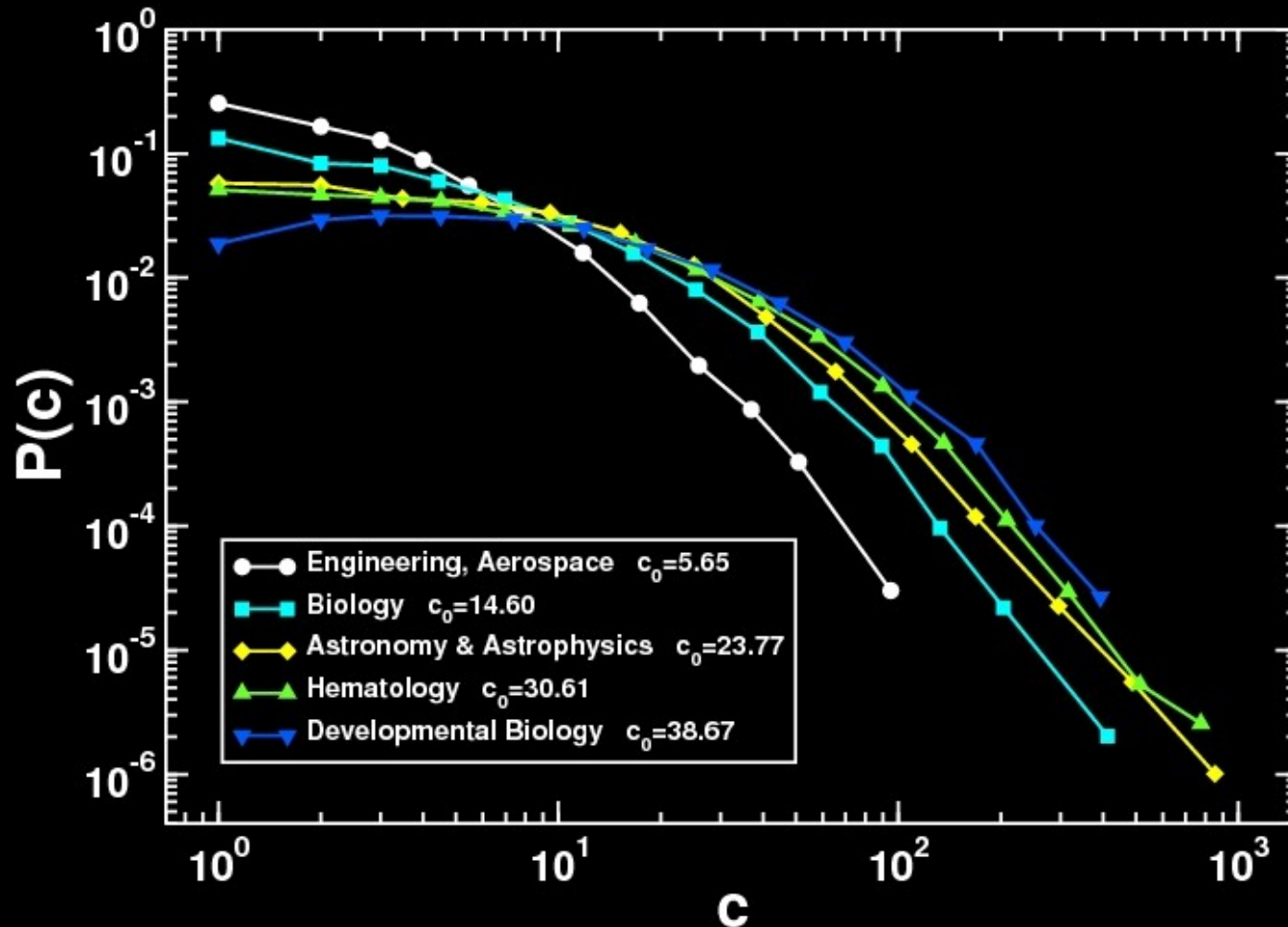
Citations

References

1. Zárský V, Cvrčková F: **Small GTPases in the morphogenesis of yeast and plant cells.** In *Molecular Mechanisms of Signalling and Membrane Transport*. Edited by Wirtz KW. Berlin: Springer, 1997, 75-88.
2. Sanderfoot AA, Raikhel N: **The specificity of vesicle trafficking: coat proteins and SNAREs.** *Plant Cell*, 1999, **11**:629-642.
3. Li H, Wu G, Ware D, Davis KR, Yang Z: **Arabidopsis Rho-related GTPases: differential gene expression in pollen and polar localization in fission yeast.** *Plant Physiol*, 1998, **118**:407-417.
4. Field C, Oegema K: **Cytokinesis in eukaryotes: a mechanistic comparison.** *Curr Opin Cell Biol*, 1999, **11**:68-90.
5. Evangelista M, Blundell K, Longtine MS, Chow CJ, Adames N, Pringle R, Peter M, Boone C: **Bni1p, a yeast formin linking Cdc42p and the actin cytoskeleton during polarized morphogenesis.** *Science*, 1997, **276**:118-122.
6. Zeller R, Haramis AG, Zuniga A, McGuigan C, Dono R, Davidson G, Chabaris S, Gibson T: **Formin defines a large family of morphoregulatory genes and functions in establishment of the polarizing region.** *Cell Tissue Res*, 1999, **296**:85-93.
7. Heil-Chapelaine R, Adames N, Cooper JA: **Formin' the connection between microtubules and the cell cortex.** *J Cell Biol*, 1999, **144**:809-811.
8. Frazier J, Field C: **Actin cytoskeleton: are FH proteins local organizers?** *Curr Biol*, 1997, **7**:R414-R417.

Lots of data from various sources

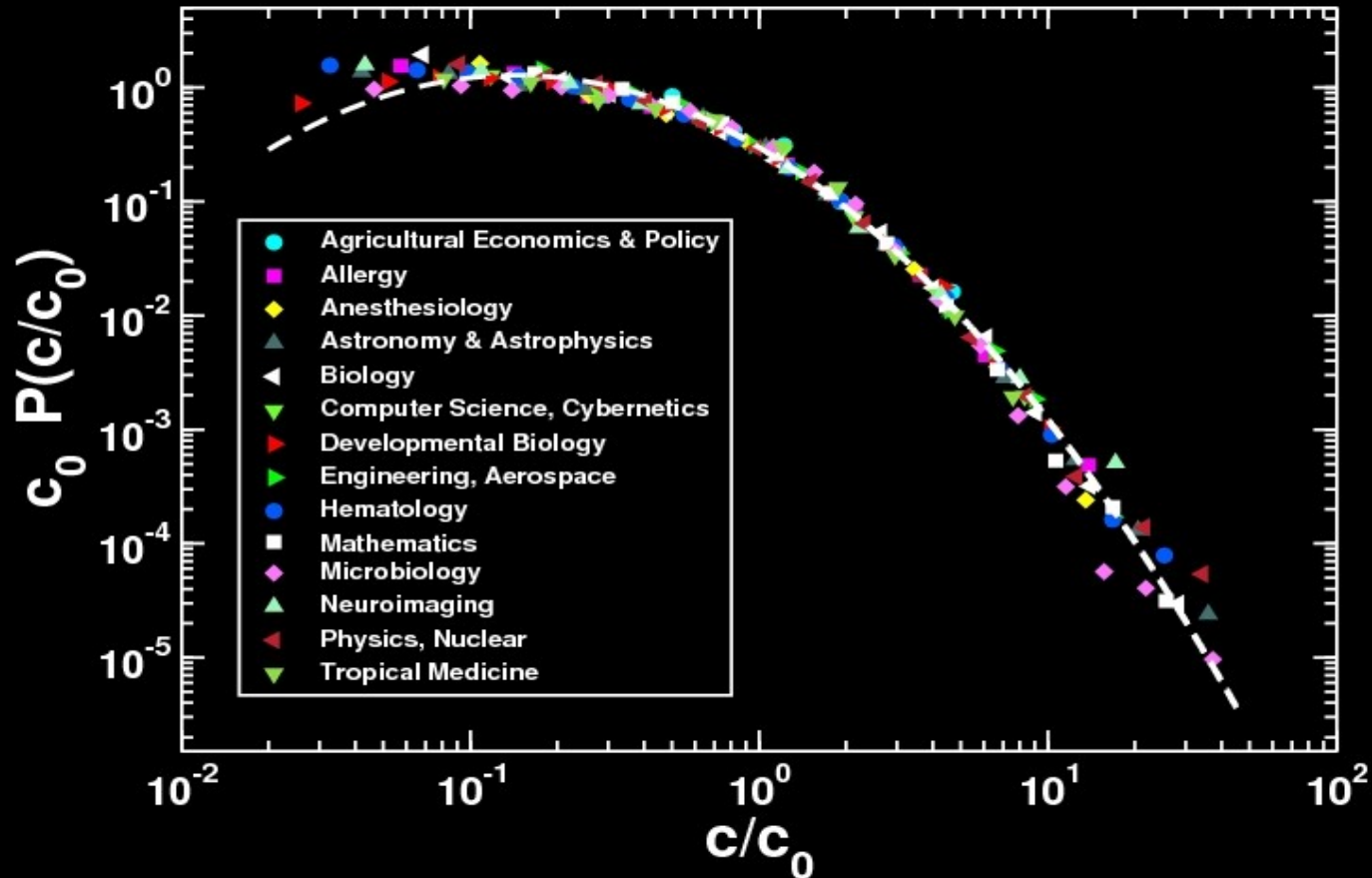
Distribution of cites?



Dependence on field (ISI category)!

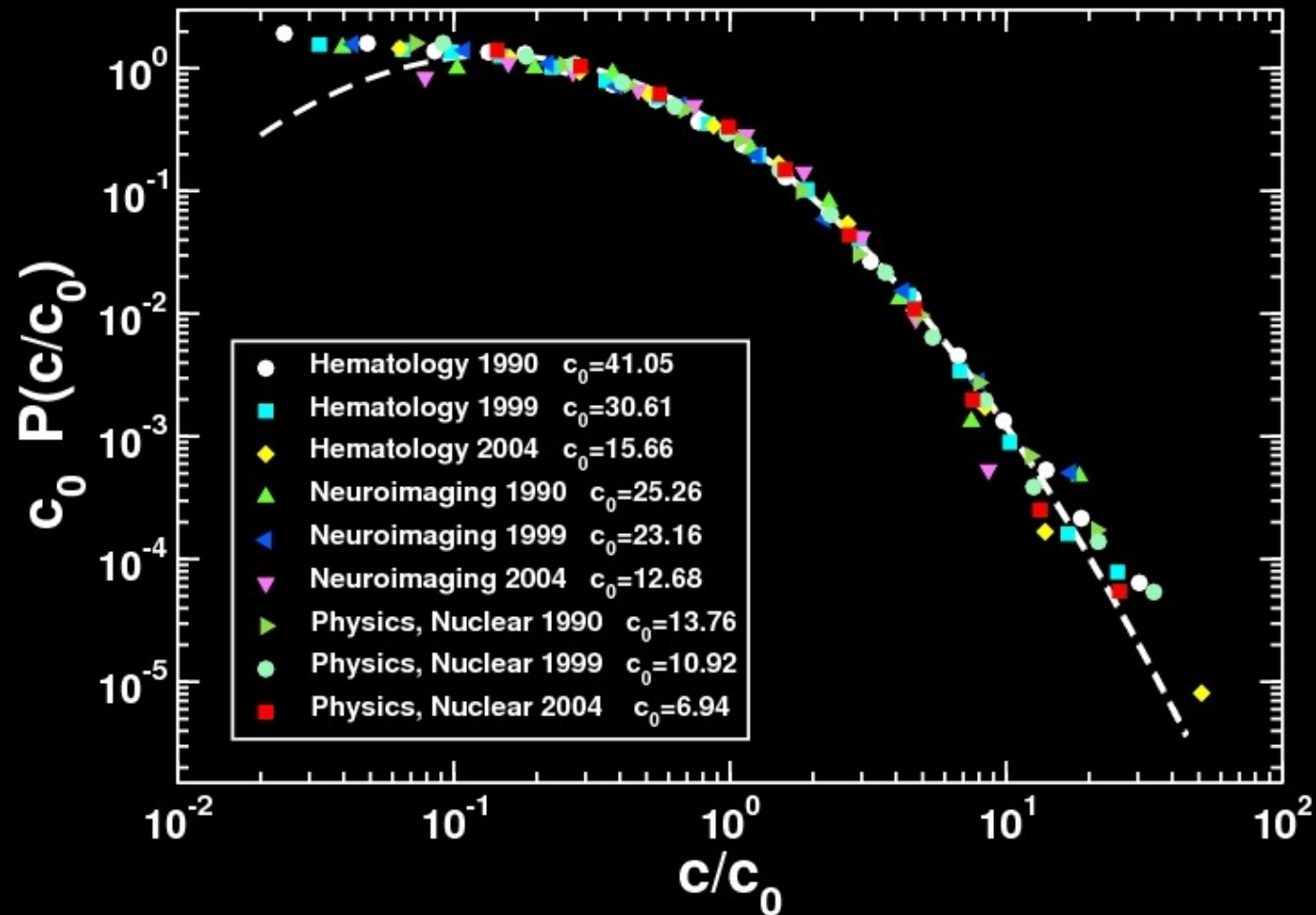
The average number of citations per paper c_0 varies a lot with the field

Could c_0 be the reason of the discrepancy?

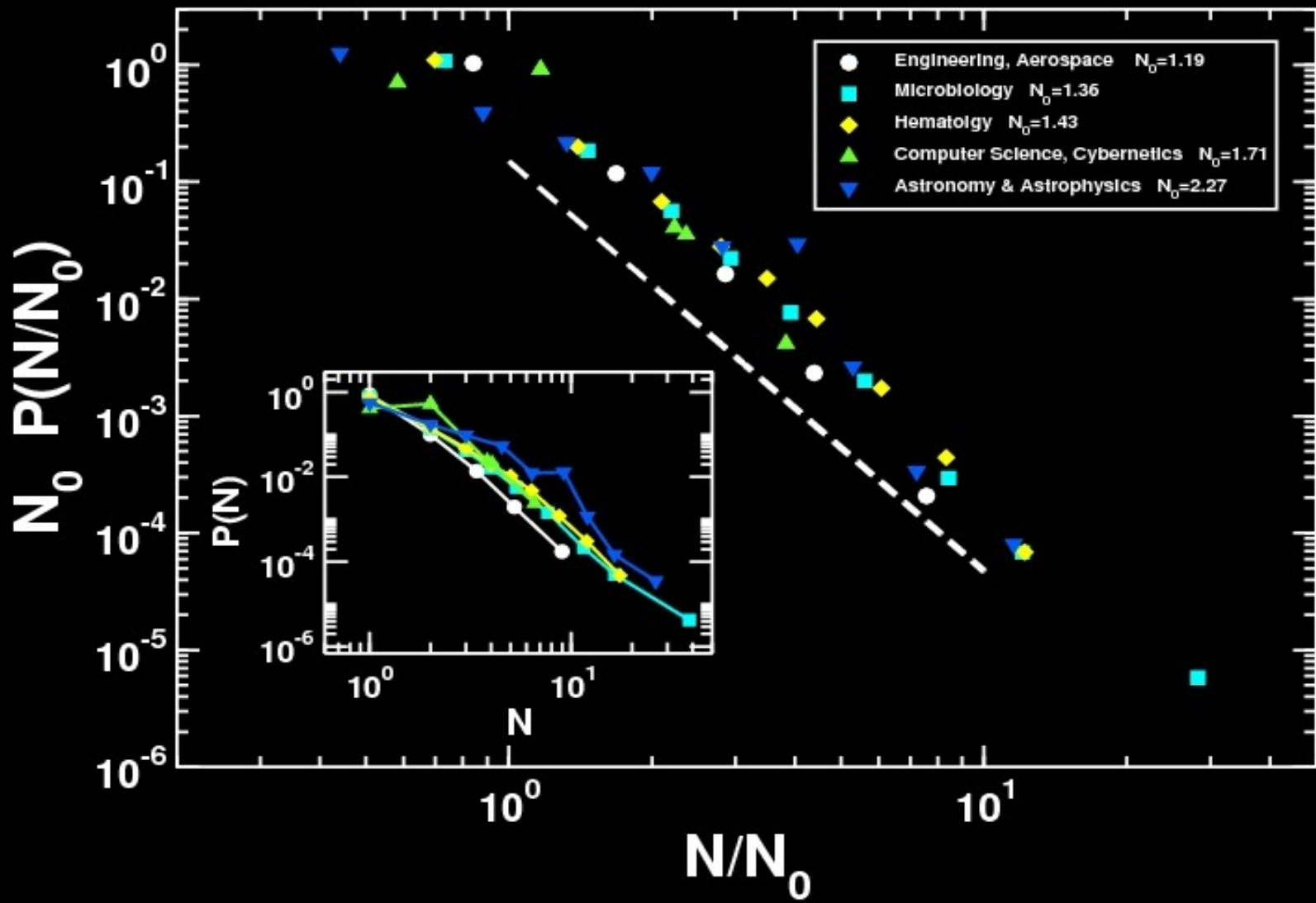


F. Radicchi, S.F. and C. Castellano, arXiv:0806.0974

The universal distribution is stable in time!



Another regularity: scientific productivity!



Other evidence?

- **Elections**
- **Consumer behavior**
- **Financial behavior**
- **Web user behavior**
- **Web-based experiments**

Information not only from stationary states, but also from dynamics

**Ex. “Collective opinion shifts”,
Michard & Bouchaud, EPJB (2005)**

Outlook

- **The distribution of the number of votes received by candidates of the same party in proportional elections is universal!**
- **The distribution of the number of citations of papers in the same discipline, normalized by the average citation score, is universal!**
- **Search for other regularities in data is necessary to create a quantitative phenomenology in social dynamics**

arXiv:0710.3256v1 [physics.soc-ph] 17 Oct 2007

Statistical physics of social dynamics

Claudio Castellano¹

SMC, INFN-CNR and Dipartimento di Fisica, "Sapienza" Università di Roma, Piazzale A. Moro 2, 00185 Roma I-ITALY

Santo Fortunato²

Complex Networks Lagrange Laboratory, ISI Foundation, Viale S. Severo 65, 10133, Torino, I-ITALY

Vittorio Loreto³

Dipartimento di Fisica, "Sapienza" Università di Roma and SMC, INFN-CNR, Piazzale A. Moro 2, 00185 Roma I-ITALY and Complex Networks Lagrange Laboratory, ISI Foundation, Viale S. Severo 65, 10133, Torino, I-ITALY

Statistical physics has proven to be a very fruitful framework to describe phenomena outside the realm of traditional physics. The last years have witnessed the attempt by physicists to study collective phenomena emerging from the interactions of individuals as elementary units in social structures. Here we review the state of the art by focusing on three major research lines *i.e.*, opinion, cultural and language dynamics. In addition we discuss other social phenomena, such as crowd behavior, hierarchy formation, human dynamics, social spreading. We highlight the connections between these problems and other, more traditional, topics of statistical physics. We also emphasize the comparison of model results with empirical data from social systems.

Contents

| | |
|---|----------|
| I. INTRODUCTION | 1 |
| II. GENERAL FRAMEWORK: CONCEPTS AND TOOLS | 2 |
| A. Order and disorder: the Ising paradigm | 2 |
| B. Role of topology | 2 |
| C. Dynamical systems approach | 2 |
| D. Agent-based modeling | 2 |
| III. OPINION DYNAMICS | 3 |
| A. Introduction | 3 |
| B. Voter model | 3 |
| 1. Regular lattices | 3 |
| 2. Modifications and applications | 3 |
| 3. The voter model on networks | 3 |
| C. Majority rule model | 3 |
| D. Social impact theory | 3 |
| E. Senajd model | 3 |
| F. Bounded confidence models | 3 |
| 1. Continuous opinions | 3 |
| 2. Defiant model | 3 |
| 3. Hegselmann-Krause model | 3 |
| G. Other models | 3 |
| H. Empirical data | 3 |
| IV. CULTURAL DYNAMICS | 3 |
| A. Axelrod model | 3 |
| B. Variants of Axelrod model | 3 |
| C. Other multidimensional models | 3 |
| V. LANGUAGE DYNAMICS | 3 |
| A. Evolutionary approaches | 3 |
| 1. Evolutionary language game | 3 |
| 2. Quasispecies-like approach | 3 |
| B. Semiotic Dynamics approach | 3 |
| 1. The Naming Game | 3 |
| 2. Symmetry breaking: a controlled case | 3 |
| 3. The role of the interaction topology | 3 |
| 4. Beyond consensus | 3 |
| C. Comparison between evolutionary and self-organized approaches to language dynamics | 3 |
| D. Language competition | 3 |
| 1. Macroscopic models | 3 |
| 2. Microscopic models | 3 |
| VI. OTHER ISSUES | 3 |
| A. Crowd behavior | 3 |
| B. Formation of hierarchies | 3 |
| C. Human dynamics | 3 |
| D. Social spreading phenomena | 3 |
| E. Coevolution of states and topology | 3 |
| VII. OUTLOOK | 3 |
| 1. Information dynamics and the Social Web | 3 |
| 2. Language and communication systems | 3 |
| 3. Evolution of social networks | 3 |
| Acknowledgments | 3 |
| References | 3 |
| I. INTRODUCTION | |

¹Electronic address: claudio.castellano@roma1.infn.it
²Electronic address: fortunato@isi.it
³Electronic address: vittorio.loreto@roma1.infn.it

The concept that many laws of nature are of statistical origin is so firmly grounded in virtually all fields of modern physics, that statistical physics has acquired the status of a discipline on its own. Given its success and its very general conceptual framework, in recent years there has been a trend toward applications of statistical physics to interdisciplinary fields as diverse as biology, medicine, information technology, computer science, etc.. In this context, physicists have shown a rapidly growing interest for a statistical physical modeling of fields patently very far from their "traditional"

<http://www.arxiv.org/pdf/0710.3256>
to appear in **Reviews of Modern Physics**