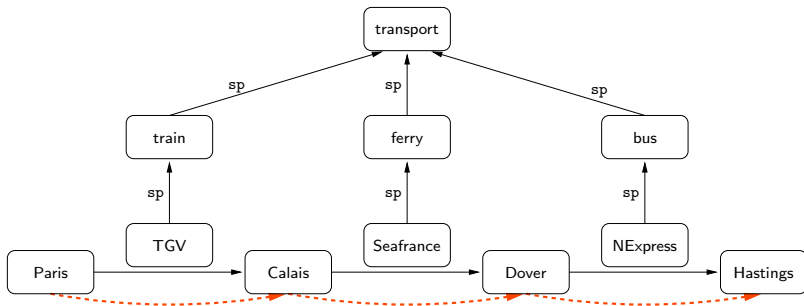
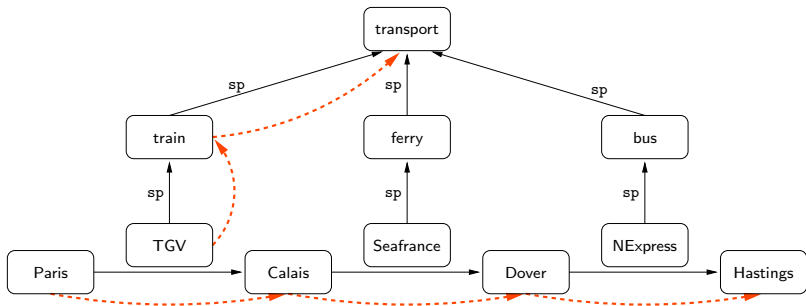


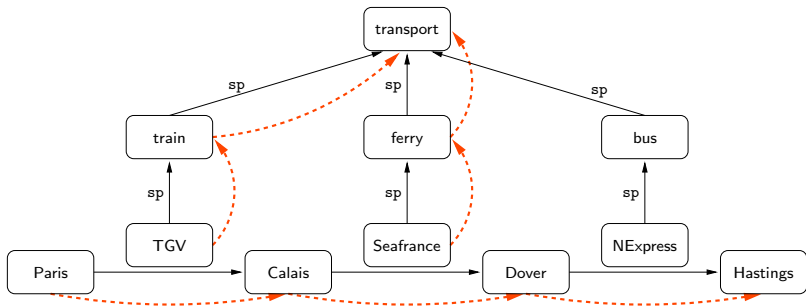
Are Paris and Hastings connected
by a sequence of transportation services?



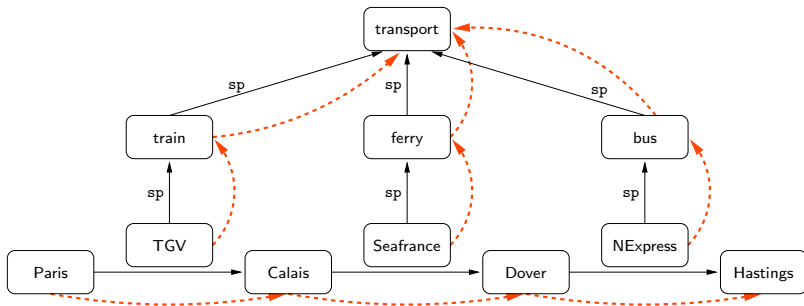
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nSPARQL: A Navigational Language for RDF

Jorge Pérez Marcelo Arenas Claudio Gutierrez

Departamento de Ciencia de la Computación
Pontificia Universidad Católica de Chile
Universidad de Chile

Khipu group
<http://www.khipu.cl>

Our contributions

- ▶ define a navigational language for RDF
- ▶ show that it can be efficiently evaluated

Our contributions

- ▶ define a navigational language for RDF
- ▶ show that it can be efficiently evaluated

We incorporate these features in SPARQL

- ▶ show that the language can express interesting RDFS queries
- ▶ study the expressive power of this language

Outline

Nested regular expressions

- Syntax and semantics

- Complexity

nSPARQL

- Syntax and semantics

- nSPARQL and RDFS evaluation

- Expressiveness

Concluding remarks

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Nested regular expressions

Syntax and semantics

Complexity

nSPARQL

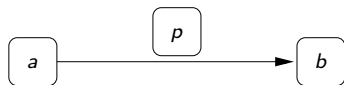
Syntax and semantics

nSPARQL and RDFS evaluation

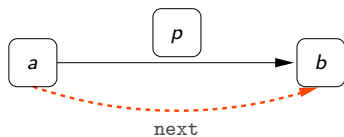
Expressiveness

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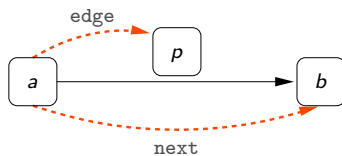
Navigational axes for RDF triple (a, p, b)



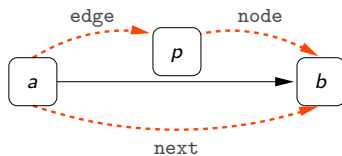
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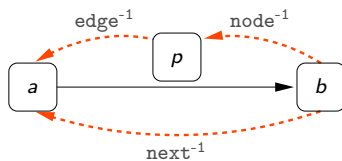
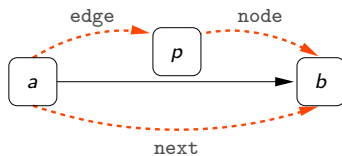
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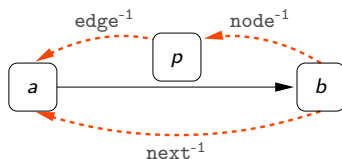
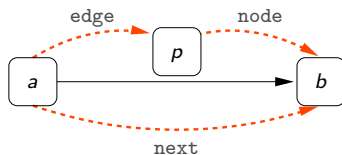
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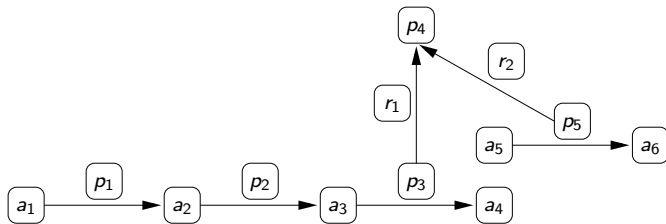


Navigational axes for RDF triple (a, p, b)

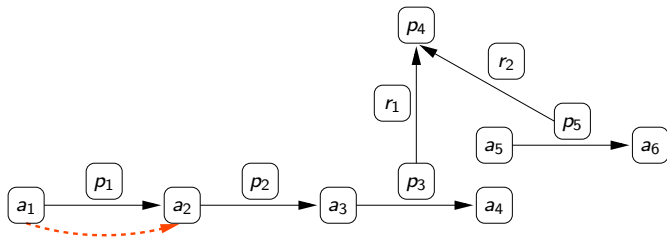


plus self axis

A sequence of axes defines a path in an RDF graph.

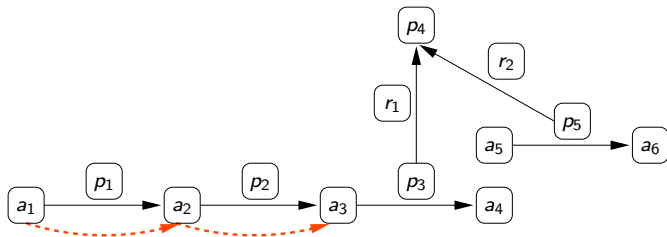


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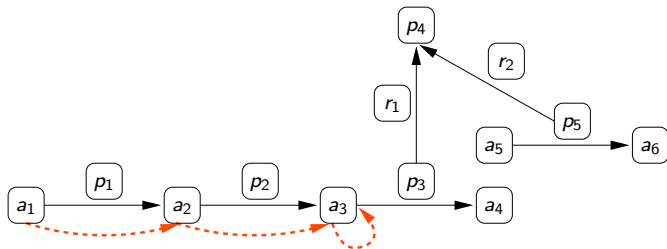
next

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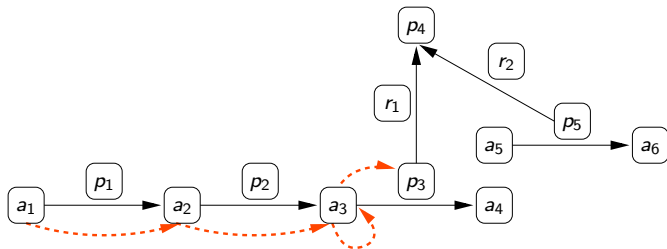
next/next

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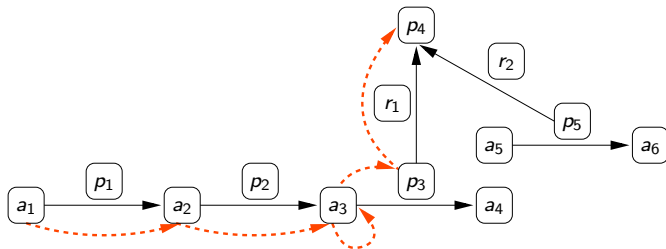
`next/next/self`

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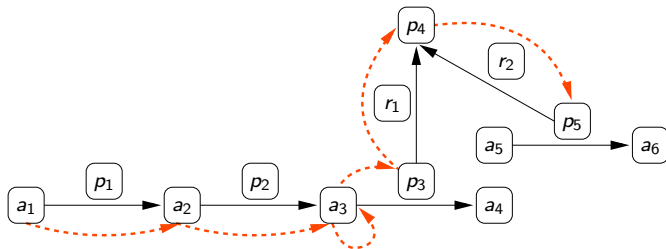
`next/next/self/edge`

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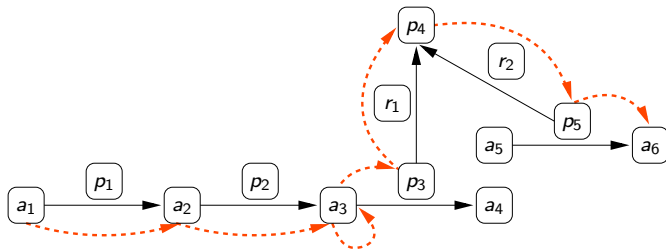
next/next/self/edge/next

A sequence of axes defines a path in an RDF graph.



`next/next/self/edge/next/next-1`

A sequence of axes defines a path in an RDF graph.



`next/next/self/edge/next/next-1/node`

Syntax of nested regular expressions over RDF

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$exp :=$

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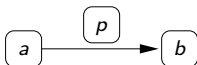
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- ▶ $[\text{exp}]$ is a *nesting* expression

Semantics of nested regular expressions over RDF

The *evaluation* of an expression exp is a set of pairs (a, b) of nodes such that b is reachable from a by following exp .

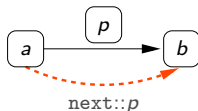
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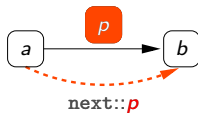
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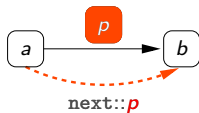
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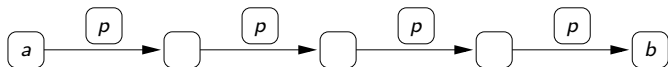
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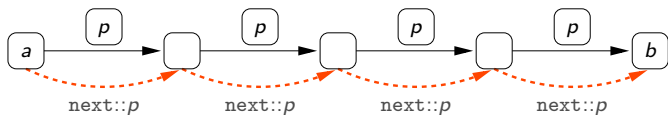
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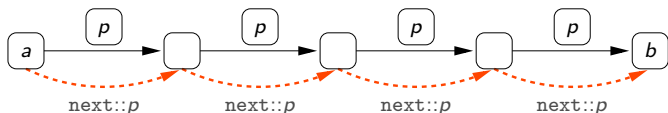
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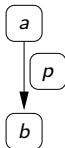
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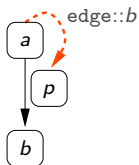
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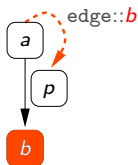
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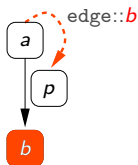
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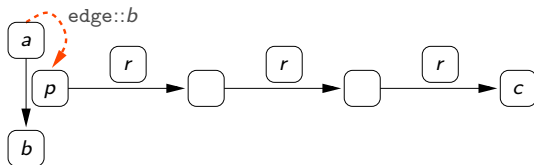
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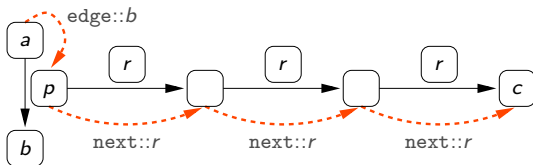
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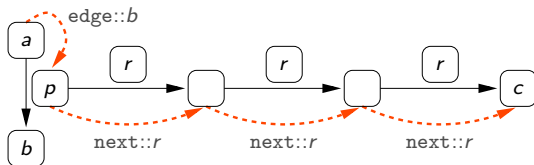
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Semantics of nested regular expressions over RDF

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(a, p) is in the evaluation of $edge::b$

(a, c) is in the evaluation of $edge::b/(next::r)^*$

Semantics of nested regular expressions over RDF graphs

Definition

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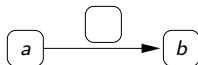
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$$(exp^+ \equiv exp/exp^*)$$

Nesting allows for existential checking.

Intuition:

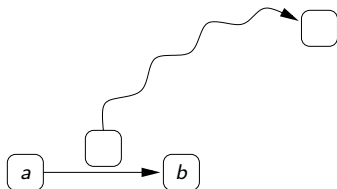
`next::[exp]` navigates from node *a* to node *b* if they are connected with an edge that satisfies a path condition given by *exp*.



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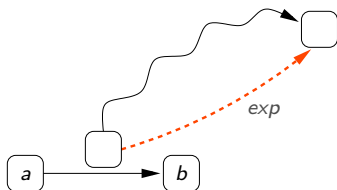
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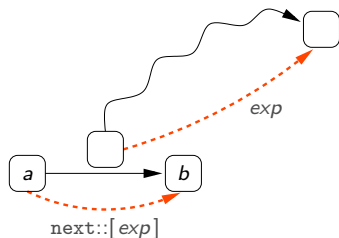
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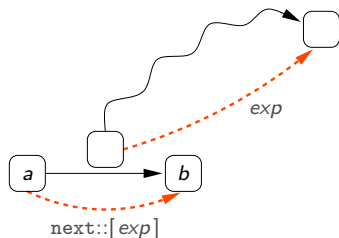
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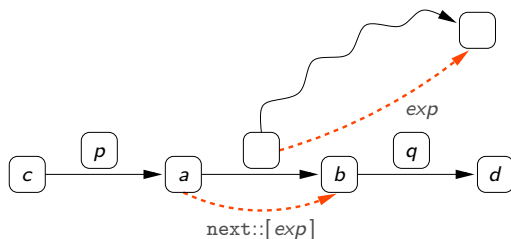


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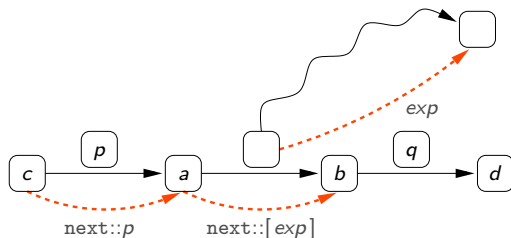


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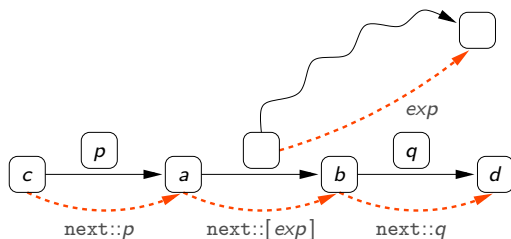


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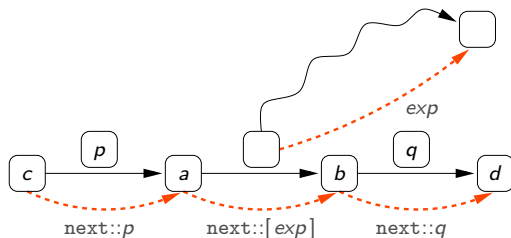


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Semantics of nested regular expressions over RDF

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We consider the associated decision problem:

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- ▶ RDF graph G
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Given a nested regular expression exp and an RDF graph G , testing whether a pair (a, b) is in $\llbracket exp \rrbracket_G$ can be done in time

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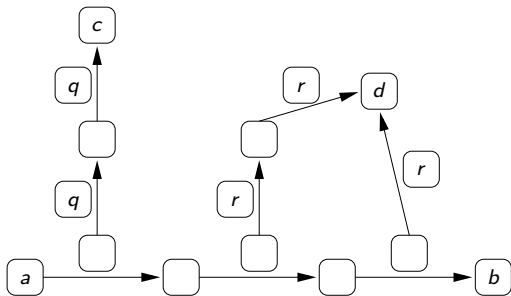
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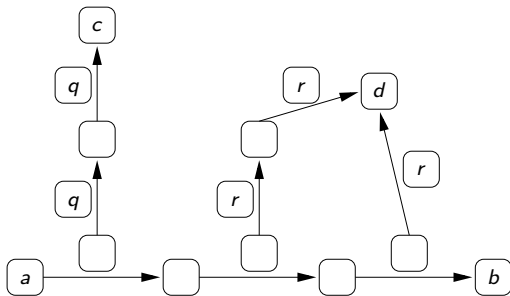
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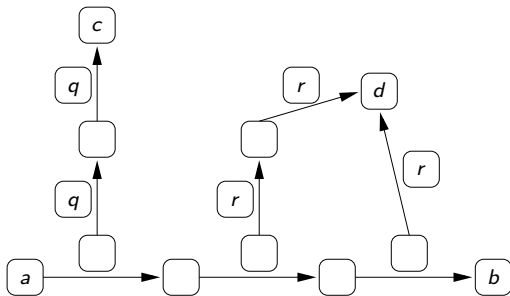
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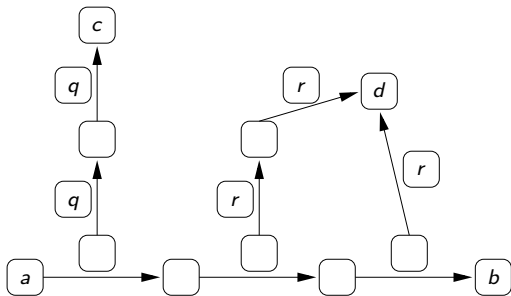


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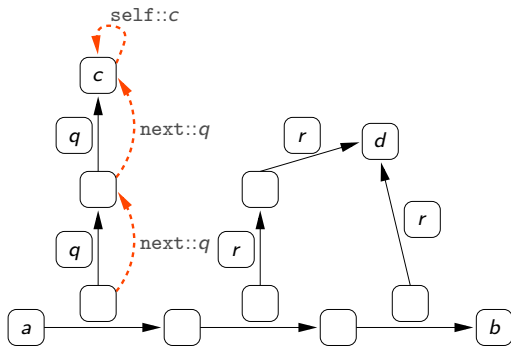


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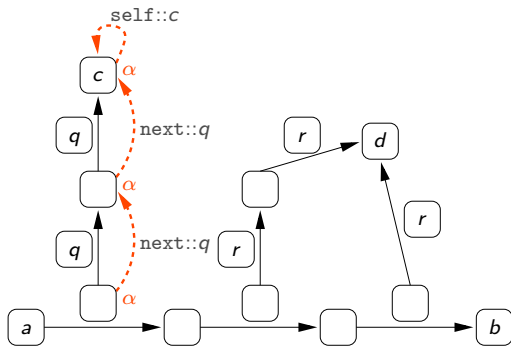


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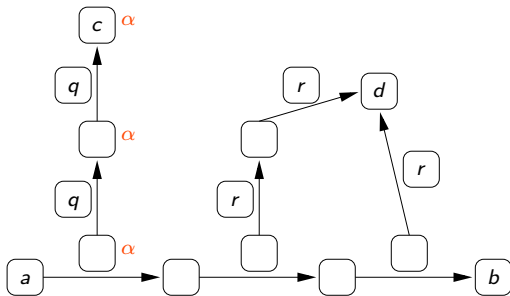


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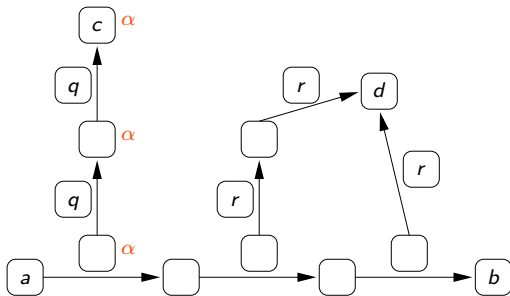


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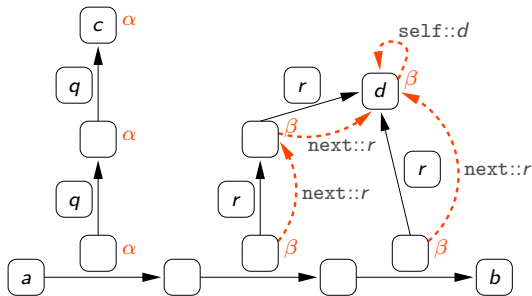


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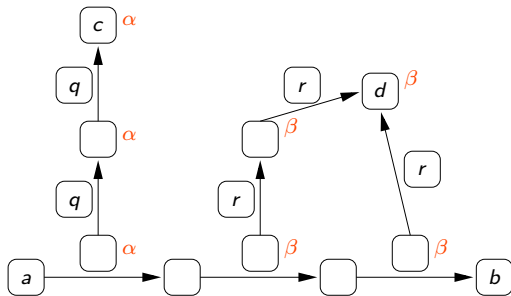


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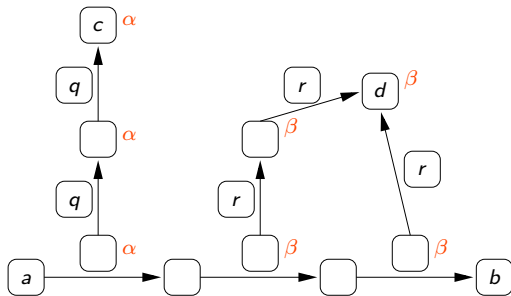


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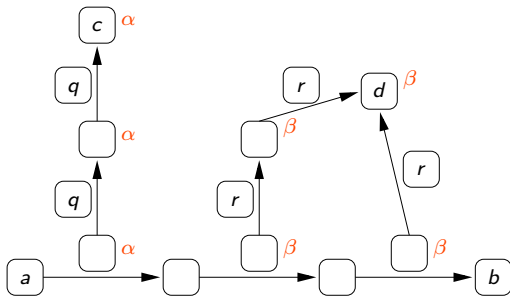


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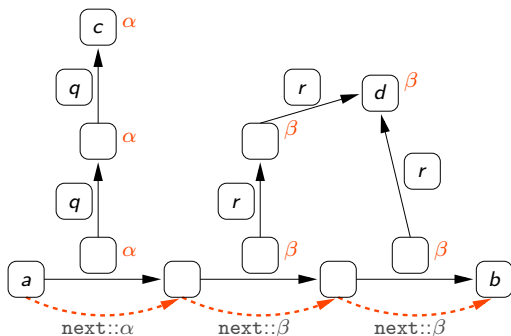
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SPARQL

We use the SPARQL formalization proposed in **[PAG06]**

`?X :name "john"`

$(?X, \text{name}, \text{john})$

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$(P_1 \text{ AND } P_2)$

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algebraic syntax

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Example

$((?X, \text{name}, \text{john}) \text{ AND } (?X, \text{email}, ?E))$

nSPARQL: navigational SPARQL

Nested-regular-expression triple (nre-triple)

$(?X, exp, ?Y)$

- ▶ *exp* is a nested regular expression
- ▶ *?X*, *?Y* are variables (could also be URIs).

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Given an RDF graph G

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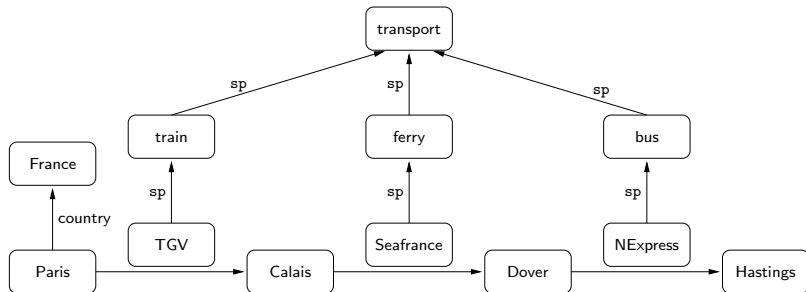
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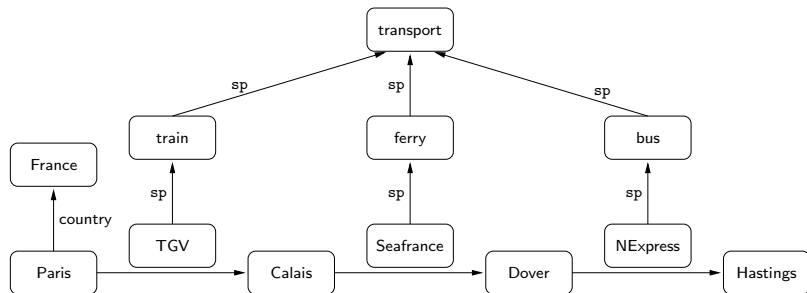
Nested regular expressions do not add extra complexity.

- ▶ An nSPARQL fragment inherits the complexity of the corresponding SPARQL fragment.

nSPARQL examples

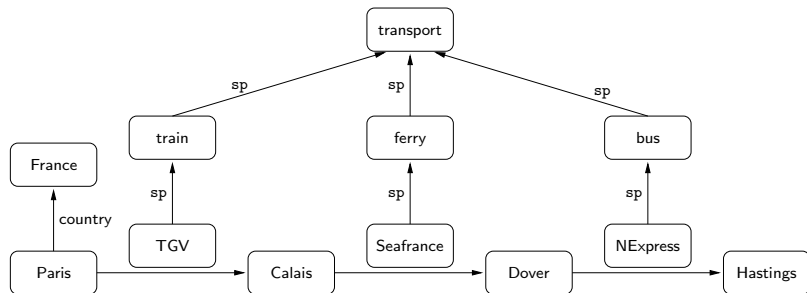


nSPARQL examples



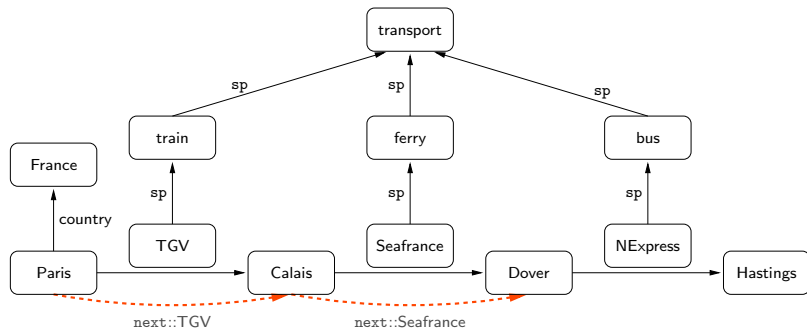
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nSPARQL examples



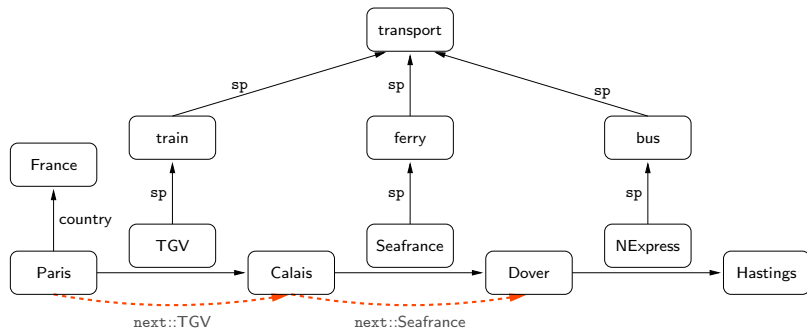
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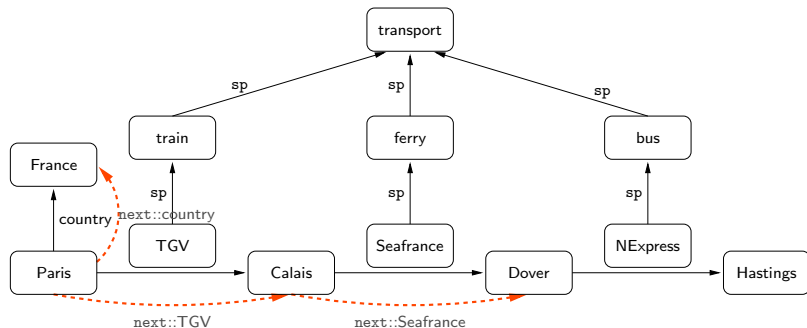
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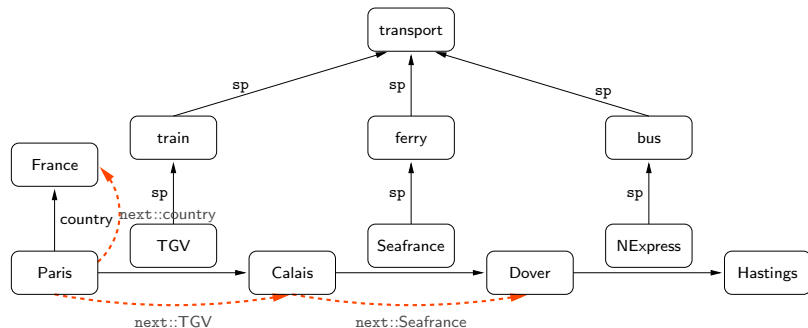
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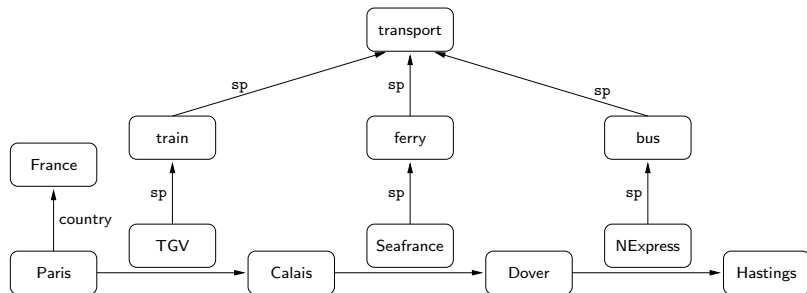
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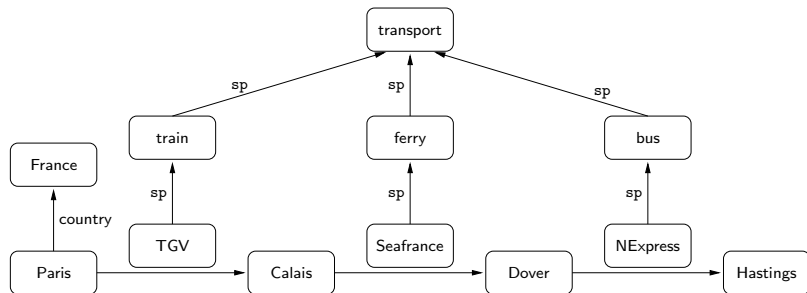
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 $\{?X \rightarrow \text{Paris}, ?Y \rightarrow \text{France}\}$

nSPARQL examples



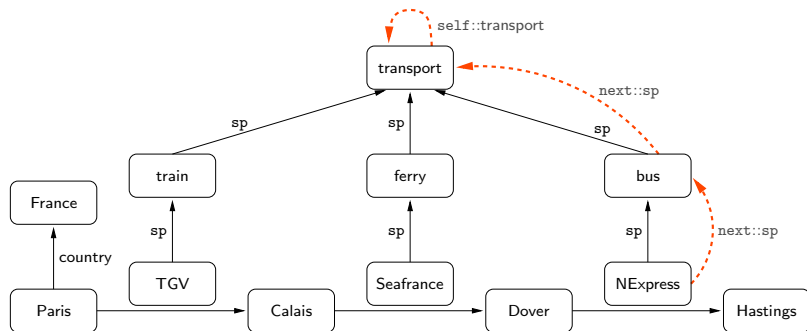
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nSPARQL examples



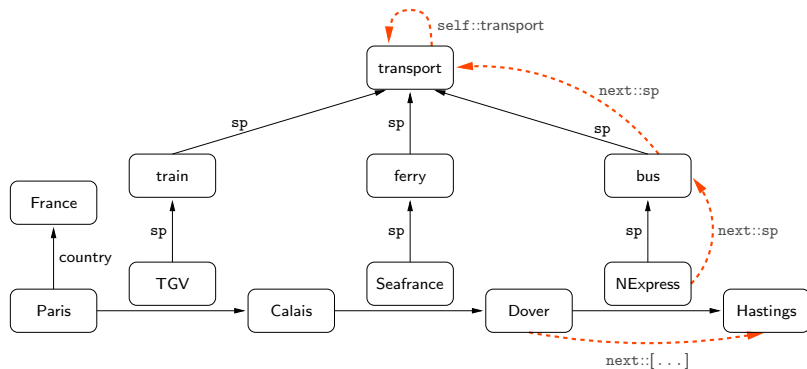
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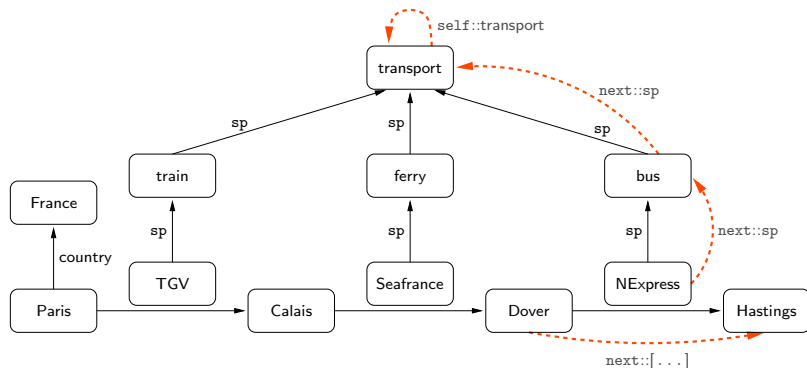
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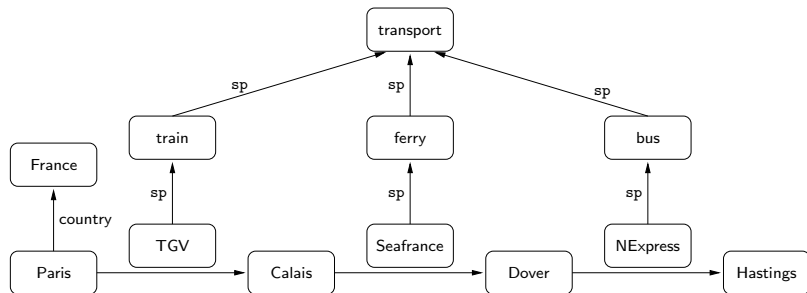
nSPARQL examples



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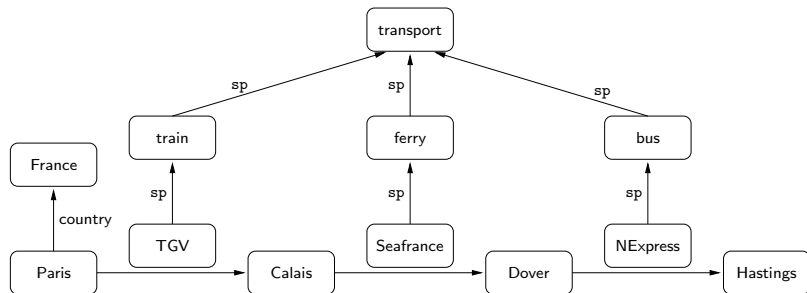
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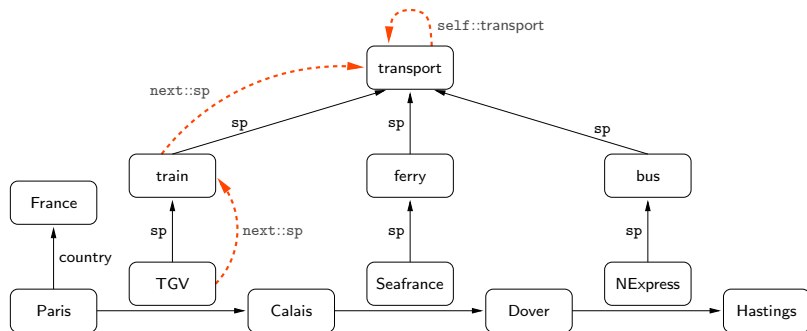
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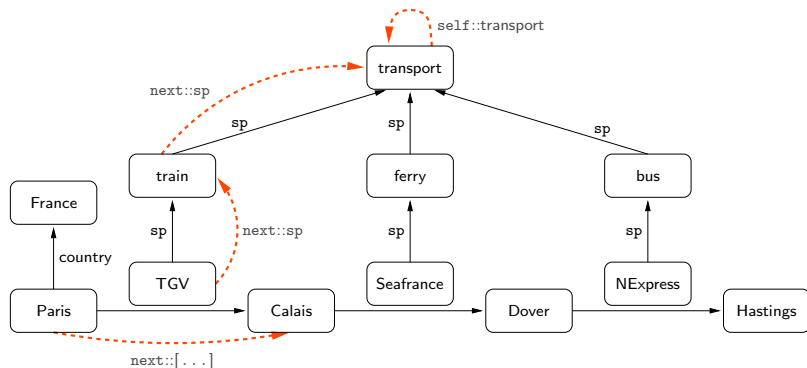
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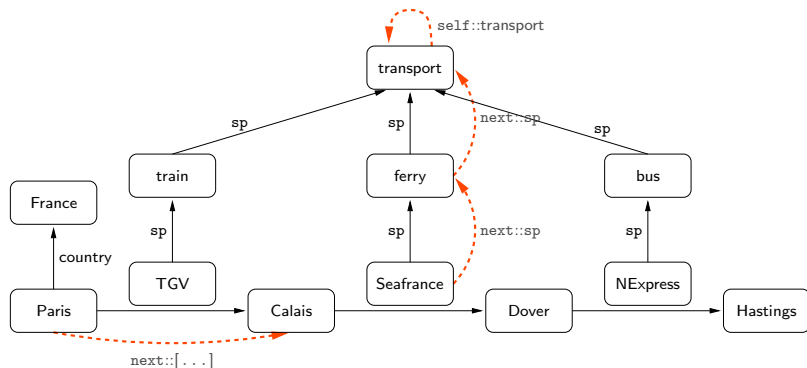
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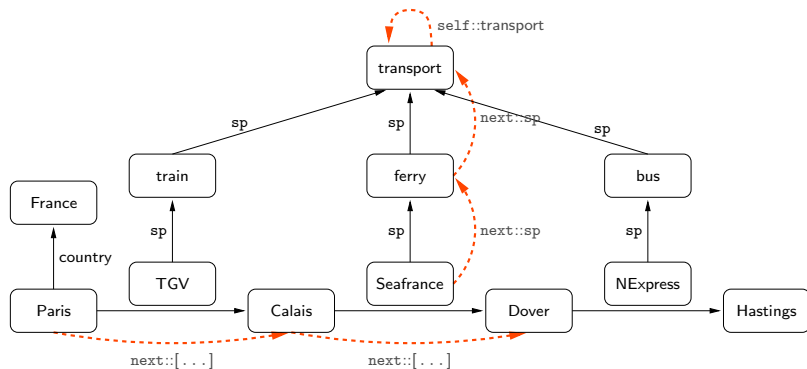
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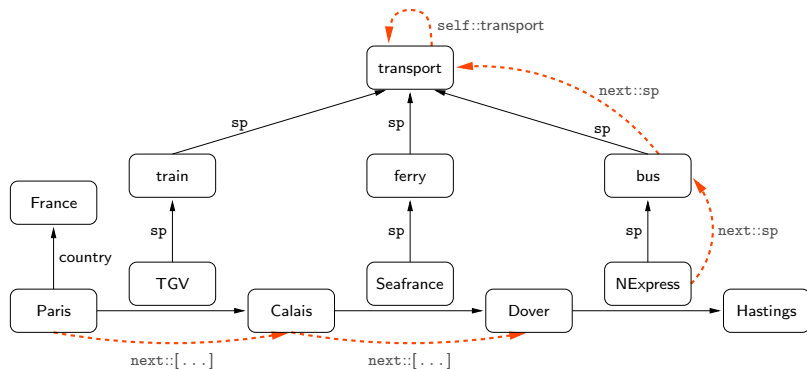
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nSPARQL examples



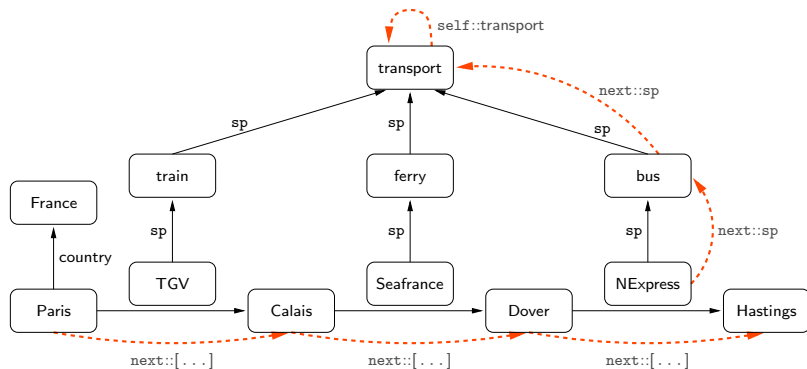
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nSPARQL examples



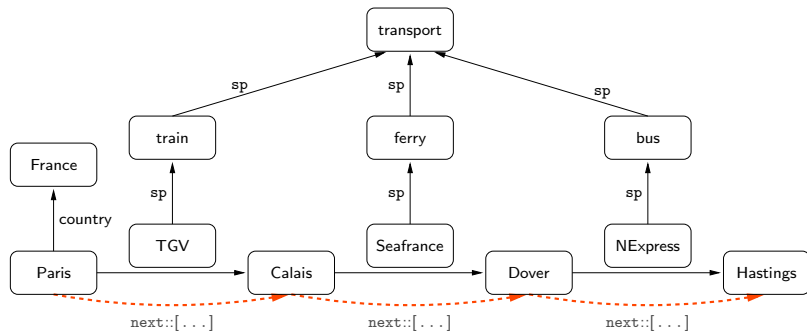
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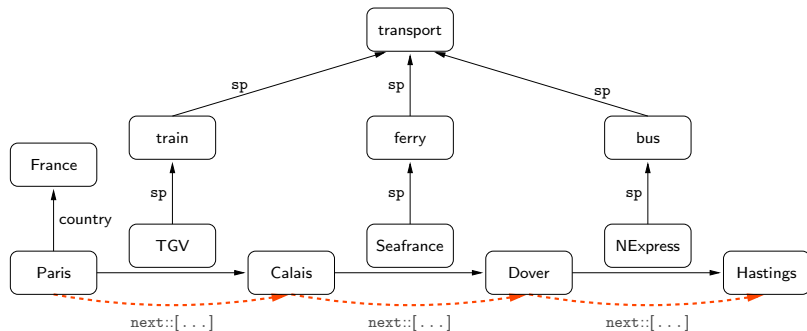
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nSPARQL examples



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nSPARQL examples



$(?X, (\text{next}::[(\text{next}::\text{sp})^*/\text{self}::\text{transport}]]^+, \text{Hastings})$

$\{?X \rightarrow \text{Paris}\}$

$\{?X \rightarrow \text{Calais}\}$

$\{?X \rightarrow \text{Dover}\}$

Outline

Nested regular expressions

Syntax and semantics

Complexity

nSPARQL

Syntax and semantics

nSPARQL and RDFS evaluation

Expressiveness

Concluding remarks

RDFS evaluation via the closure

Consider the sub-vocabulary of RDFS $\{\text{sp}, \text{sc}, \text{dom}, \text{range}, \text{type}\}$ and its semantics via deductive rules.

Closure of G: obtained by applying rules to exhaustion.

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Closure of G : obtained by applying rules to exhaustion.

Definition

Given a SPARQL pattern P , its *RDFS evaluation* over a graph G is the usual evaluation of P over the *closure* of G .

nSPARQL is enough for RDFS evaluation of standard SPARQL queries.

Theorem

Given a SPARQL triple $t = (?X, a, ?Y)$, there exists an nSPARQL triple $r = (?X, \text{trans}(a), ?Y)$ such that

the RDFS evaluation of t can be obtained by directly evaluating r over the input graph.

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Proof idea

- ▶ $\text{trans}(\text{sc}) = (\text{next}::\text{sc})^+$
- ▶ ...
- ▶ $\text{trans}(a) = \text{next}::[(\text{next}::\text{sp})^*/\text{self}::a]$ ($a \notin \{\text{sp}, \text{sc}, \dots\}$)

$\text{trans}(\text{type})$ uses next , edge , node^{-1} .

nSPARQL is enough for RDFS evaluation of standard SPARQL queries.

Theorem

Given a SPARQL pattern P , we can translate it into an nSPARQL pattern Q such that

the RDFS evaluation of P can be obtained by directly evaluating Q over the input graph.

Just rewrite every triple of P .

nSPARQL without nesting is not enough.

Let rSPARQL the fragment of nSPARQL obtained by forbidding nesting in expressions (usual regular expressions over the axes).

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Proposition

The RDFS evaluation of SPARQL triple pattern $(?X, a, ?Y)$ cannot be obtained with any rSPARQL pattern.

Nested regular expressions and
SPARQL operators are complementary.

- ▶ nSPARQL add expressive power to SPARQL

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Do SPARQL operators add expressive power to nSPARQL expressions?

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Do SPARQL operators add expressive power to nSPARQL expressions?

Theorem

There is an nSPARQL pattern that is not equivalent to any nSPARQL pattern that does not use OPT.

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nested regular expressions:

- ▶ natural navigation through an RDF graph
- ▶ low complexity of evaluation

nSPARQL:

- ▶ combines the power of SPARQL operators and nre
- ▶ RDFS evaluation by traversing the input graph
- ▶ allow expressing natural queries

nSPARQL: A Navigational Language for RDF

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