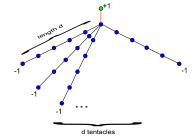
## Online Prediction on Large Diameter Graphs

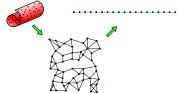
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- Learn labelling of a graph online
- Mistake bounds:
  M ≤ f(complexity(u), geometry(G))
- Limitation of Laplacian methods
- e.g. Min norm interpolation:



• Mistake bound =  $\Theta(\sqrt{|V|})$ 

 Spine: approximate structure-preserving embedding of any graph into a path



- 1-NN  $\equiv$  Halving Algorithm on S
- $M = \mathcal{O}\left(\phi_{\mathcal{G}}(\mathbf{u})\log\left(\frac{|V|}{\phi_{\mathcal{G}}(\mathbf{u})}\right)\right)$
- Cumulative time to predict m labels  $\mathcal{O}(m \log m + |E|)$
- Second solution:
  - Exploits cluster structure
  - Exploits connectivity
    - Logarithmic guarantee

