

Machine Learning, Market Design, and Advertising

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December 13, 2008

Paid Search

The screenshot shows a web browser window with the address bar containing the URL `http://www.google.com/search?client=safari&rls=en-us&q=harry+potter&ie=UTF-8&...` and the search term "harry potter". The page displays search results for "harry potter" with approximately 94,200,000 results. The organic results include a theater listing for "Harry Potter and the Order of the Phoenix" and news articles. The sponsored links section features advertisements for "The Tales of Beedle the Bard" from Books-247.com, a personality test from DaVinciMethod.com, and "Harry Potter & the Deathly Hallows" from Amazon.com.

harry potter - Google Search

http://www.google.com/search?client=safari&rls=en-us&q=harry+potter&ie=UTF-8&... harry potter

Web Images Maps News Shopping Gmail more Sign in

Google harry potter Search Advanced Search Preferences

Web News Images Blogs Video Books Results 1 - 10 of about 94,200,000 for **harry potter**. (0.05 s)

Harry Potter and the Order of the Phoenix showtimes for IL 60614 - [Change location](#)
2hr 18min - Rated PG-13 - Action/Adventure/Drama/Scifi/Fantasy
 AMC Loews Streets of Woodfield 20 - 601 N. Martingale Road, Schaumburg, IL, USA - [Map](#)
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[More theaters »](#)

News results for harry potter

Harry Potter exhibit coming to Museum of Science and Industry - 14 hours ago
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Harry Potter: The Tales of Beedle the Bard becomes fastest-selling ... - [Telegraph.co.uk](#) - [95 related articles »](#)

Sponsored Links

The Tales of Beedle the Bard
J.K. Rowling Top Seller Books 2009
The Tales of Beedle the Bard
[Books-247.com/Harry+Potter](#)

Is Harry Potter Like You?
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Harry Potter
Harry Potter & the Deathly Hallows
FREE Super Saver Shipping!
[www.Amazon.com](#)

Harry potter
Fantastic prices on **harry potter**
Deal with Canadians and save
[www.ebay.ca](#)

GSP

Definition: *Generalized Second Price* (GSP) auction

- advertisers bid for keywords in advance.
- on query,
 - find all bids that *match* query.
 - rank by bid.
 - if ad clicked, charge next highest bid.

(can also scale bids by “quality” or click-through rate)

Overview

Part I: Beyond GSP.

- Advertising market overview.
- Short-comings of GSP.
- Proposal: add pre-sale market.
- Many connections to ML.

Part II: Machine learning and market design.

Part I: Beyond GSP.

Online/Search Advertising Markets

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- *search engine*
- *users*
- *advertisers*

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(short-term profit maximization is probably short-sighted)

Properties of GSP

Recall Definition: Generalized Second Price (GSP) auction

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Properties:

- *low-level bidding language*: bids for keywords.
- *decentralized*: advertisers are optimizers
- *local*: advertisers adapt bids to market conditions.
- *diffuse info*: advertisers know demand, engine knows supply.
- *online greedy*: allocation ignores future supply and past allocation

GSP non-optimality

Evidence of GSP Non-optimality:

- *search engine marketers* are necessary (i.e., significant bid cost).
- pervasive use of *broadmatch*.
- Many advertisers do not actively change bids.
- Budgets often *binding* (advertisers could bid less and get more).

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Note: better to have expressive bids and low bid-maintenance cost.

Example: "Harry Potter"

The screenshot shows a Google search for "harry potter" in a Safari browser window. The search results are displayed in a grid format. On the left, there are search filters for "Web", "Images", "Maps", "News", "Shopping", and "Gmail". The main search bar contains "harry potter" and a "Search" button. Below the search bar, there are links for "Advanced Search" and "Preferences". The search results are categorized into "Web", "News", "Images", "Blogs", "Video", and "Books". The top result is "Harry Potter and the Order of the Phoenix showtimes for IL 60614 - Change location", which includes a movie icon, the title, showtimes (1:35 and 7:05pm), and the location (601 N. Martingale Road, Schaumburg, IL, USA). Below this, there are "News results for harry potter" with a small photo of a man and several news headlines, including "Harry Potter exhibit coming to Museum of Science and Industry" and "'Harry Potter' Star Emma Watson 'Intrigued' For 'Deathly Hallows ...'". On the right side, there are "Sponsored Links" for "The Tales of Beedle the Bard" from Books-247.com, "Is Harry Potter Like You?" from DaVinciMethod.com, "Harry Potter" from Amazon.com, and "Harry potter" from ebay.ca.

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Web Images Maps News Shopping Gmail more Sign in

Google deathly hallows Search Advanced Search Preferences

Web Video News Blogs Shopping Results 1 - 10 of about 3,110,000 for **deathly hallows**. (0.23 sec)

Harry Potter and the Deathly Hallows - Wikipedia, the free ...
Harry Potter and the **Deathly Hallows** is the seventh and final of the Harry Potter novels written by British author J. K. Rowling. The book was released on ...
en.wikipedia.org/wiki/Harry_Potter_and_the_Deathly_Hallows - 158k - [Cached](#) - [Similar pages](#)

Magical objects in Harry Potter - Wikipedia, the free encyclopedia
30 Jul 2007 ... The coins are also used in Harry Potter and the **Deathly Hallows** to The **Deathly Hallows** are three magical objects that appear in Harry ...
en.wikipedia.org/wiki/Magical_objects_in_Harry_Potter - 172k - [Cached](#) - [Similar pages](#)

Harry Potter and the Deathly Hallows: Part I (2010)
Directed by David Yates. With Daniel Radcliffe, Emma Watson, Helena Bonham Carter. Visit IMDb for Photos, Showtimes, Cast, Crew, Reviews, Plot Summary, ...
www.imdb.com/title/tt0926084/ - 43k - [Cached](#) - [Similar pages](#)

Video results for deathly hallows

Sponsored Links

Harry Potter 7 Special
Only \$9.99 while supply lasts
Harry Potter's Final Book, Save \$25
www.booksonboard.com

Deathly Hallows at Amazon
Millions of books, new and used
Qualified orders over \$39 ship free
Amazon.ca/books

Broadmatch Discussion

Discussion:

- Compare Amazon's value-per-click:
Probably "Harry Potter" < "Deathly Hallows"
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Suggestion:

- Use "conversion tracking" to learn *conversion rates*.
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- Use auction where advertisers bid *true value-per-click*.
(incompatible with GSP)

Challenges and Tasks

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What would be a better mechanism?

Beyond GSP

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Related Examples:

- *timber*: 20% spot auction, 80% pre-sale (prices from spot)
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How should we design the advertising pre-sale market?

Part II: Machine learning and market design.

Setting

Setting:

- can estimate supply.
- can estimate preferences.
(if advertisers provide automated reports)
- can cluster tail.

Market Design Goal:

- incentivize advertisers to provide automated reports.
- optimize objective.

Pricing-based mechanisms

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Claim: many justifications for pricing-based approach.

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Natural Objective: for class of offers \mathcal{G} , find offer that maximizes objective payoff. (e.g., social welfare, profit, etc.)

Optimizing Offers

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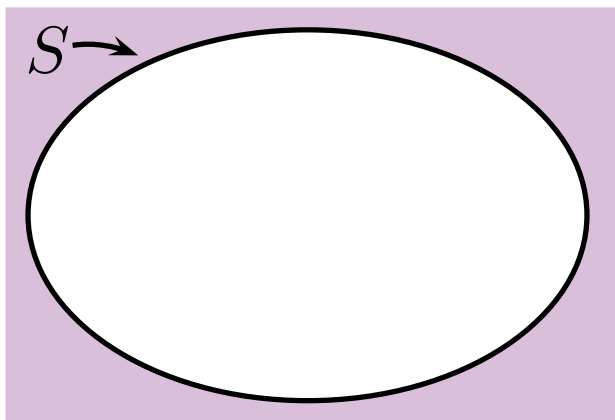
Incentive Challenge: advertisers can manipulate this optimal offer.

Can we design mech. where it is optimal to report true preferences?

Approach 1: Random Sampling Auction

Random Sampling Optimal Offer Auction, $RSOO_{\mathcal{G}}$

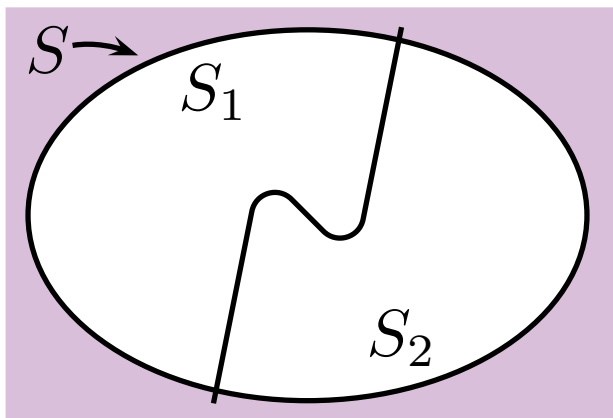
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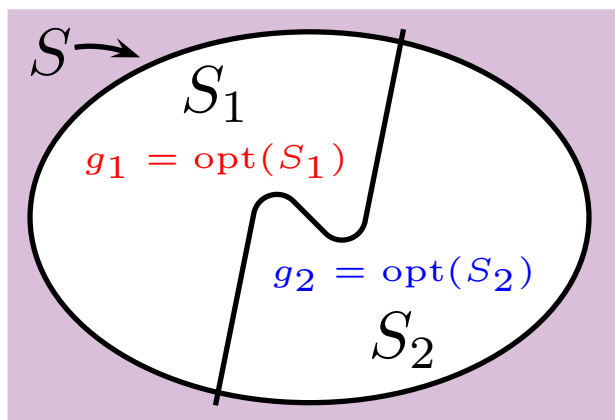
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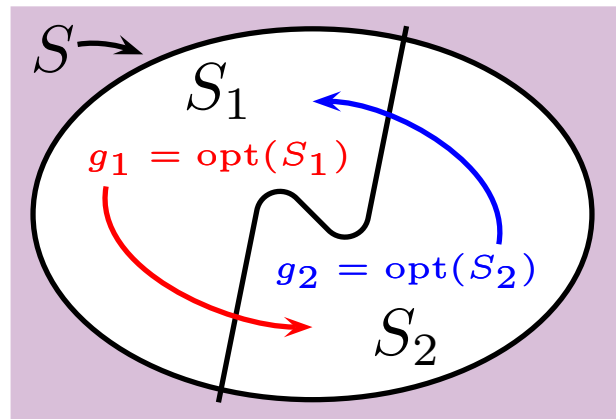
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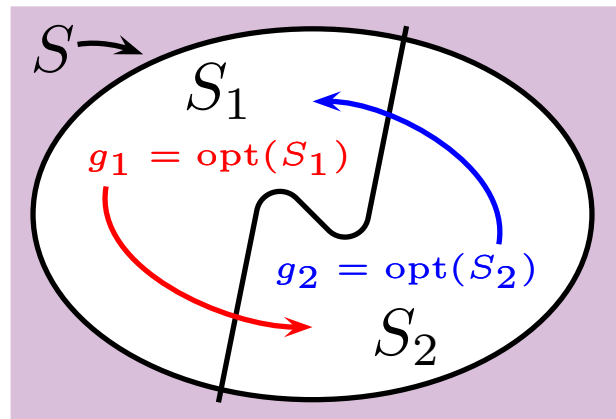
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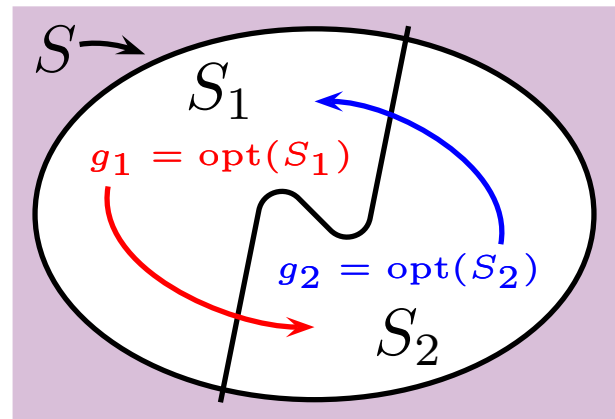


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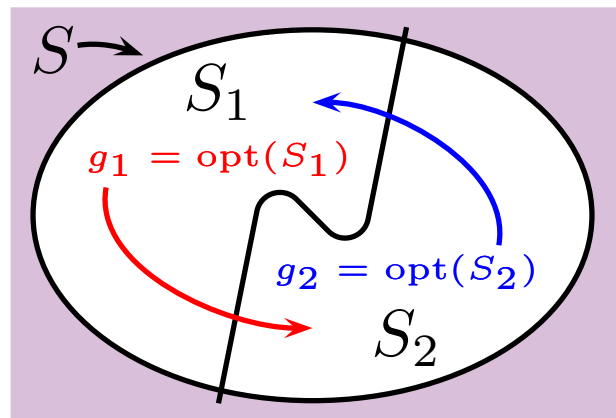
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Note: close connection to sample complexity and machine learning.

RSOO Performance

Theorem: (Approximately) For any linear objective (e.g., welfare or profit), class of offers \mathcal{G} , and ϵ ;

$$\mathbf{E}[\text{RSOO}_{\mathcal{G}}] \geq (1 - \epsilon) \text{OPT}_{\mathcal{G}}$$

as long as

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Interpretation: convergence rate is $O(h \log |\mathcal{G}|)$.

Example: tee shirts

Example: Selling tee shirts.

- Bidders with valuations in $[1, h]$ for a tee shirt.
- Reasonable offers: $\mathcal{G} = \{\text{price } 2^i \text{ for } i \in \{1, \dots, \log h\}\}$.
- Convergence Rate: $O(h \log |\mathcal{G}|) = O(h \log \log h)$

Extensions

Recall Interpretation: convergence rate is $O(h \log |\mathcal{G}|)$.

Extensions:

- use *covering* arguments to improve bounds.
- use *structural-risk-minimization* to penalize for “complex” offers.

Selected References:

- Pricing Algorithms: E.g., [Gurusuami et al., 2005]
- Unlimited Supply: [Balcan et al., 2005]
- Limited Supply: [Balcan et al., unpublished]

Approach 2: Differential Privacy

Definition: A function f satisfies *ϵ -differential privacy* if for S and S' differing in one coordinate and set R in range of f ,

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Note: if near optimal offer can be computed with ϵ -diff. privacy, advertisers cannot manipulate it.

Comment: in fact, perhaps all services that use private data should satisfy ϵ -differential privacy.

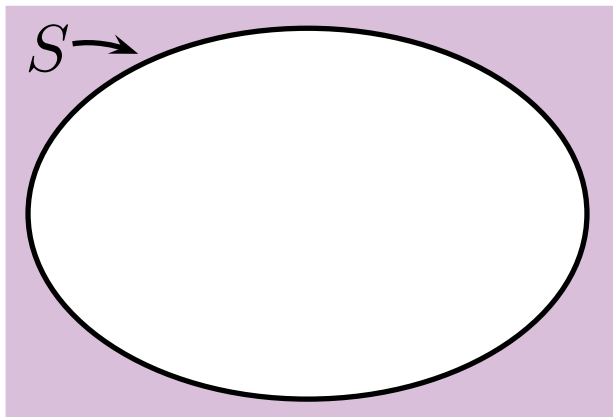
Selected References:

- Differential Privacy: [Dwork, 2006]
- Differential Privacy Auction: [McSherry and Talwar, 2007]

Approach 2: Differential Privacy Auction

Privacy Preserving Optimal Offer Auction, $DPOO_g$

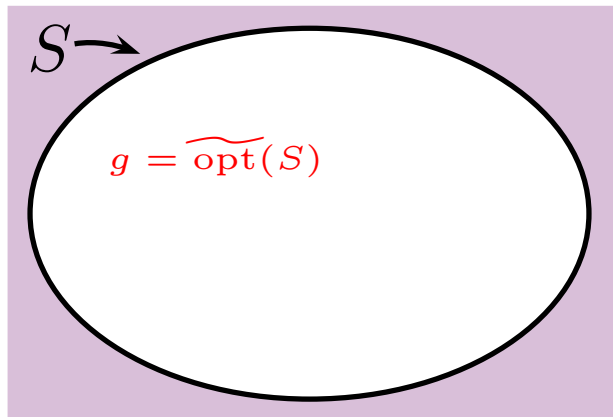
1. Compute approximately optimal offer g with ϵ -diff. privacy.
2. Offer g to all advertisers.



Approach 2: Differential Privacy Auction

Privacy Preserving Optimal Offer Auction, $DPOO_{\mathcal{G}}$

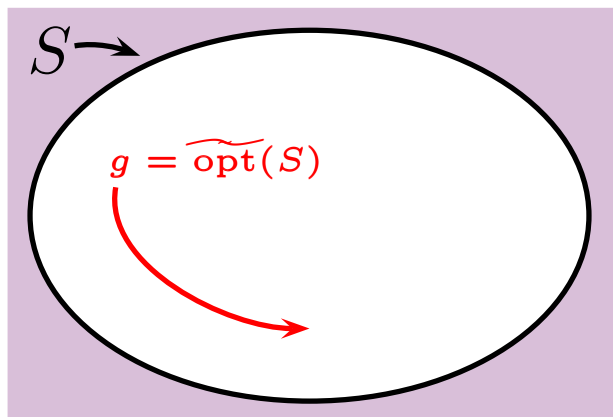
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Approach 2: Differential Privacy Auction

Privacy Preserving Optimal Offer Auction, $DPOO_{\mathcal{G}}$

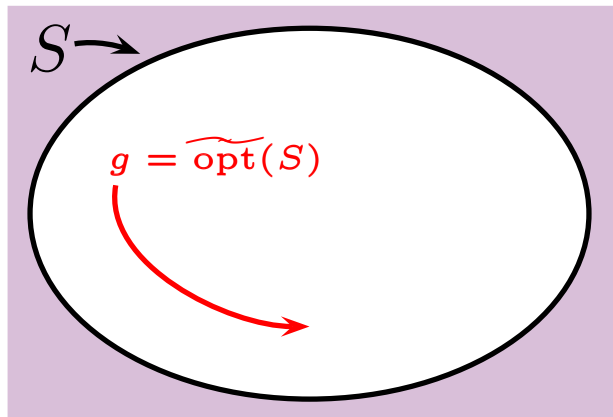
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Approach 2: Differential Privacy Auction

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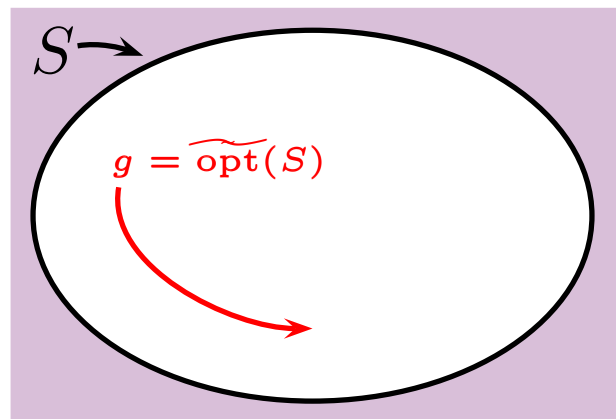


Claim: $DPOO_{\mathcal{G}}$ is has near optimal performance.

Approach 2: Differential Privacy Auction

Privacy Preserving Optimal Offer Auction, $\text{DPOO}_{\mathcal{G}}$

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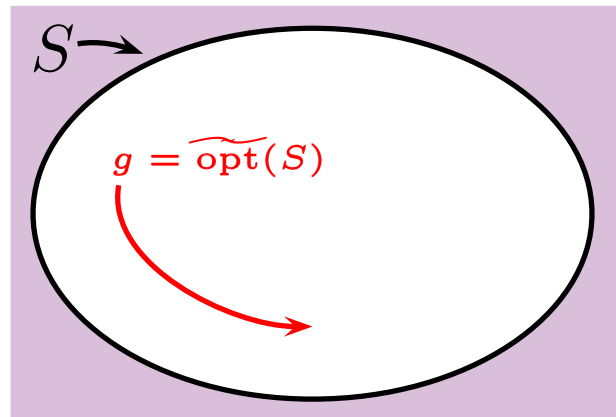
Claim: $\text{DPOO}_{\mathcal{G}}$ has near optimal performance.

Claim: With high probability in $\text{DPOO}_{\mathcal{G}}$, reporting true preferences is optimal.

Approach 2: Differential Privacy Auction

Privacy Preserving Optimal Offer Auction, $\text{DPOO}_{\mathcal{G}}$

1. Compute approximately optimal offer g with ϵ -diff. privacy.
2. Offer g to all advertisers.



Claim: $\text{DPOO}_{\mathcal{G}}$ has near optimal performance.

Claim: With high probability in $\text{DPOO}_{\mathcal{G}}$, reporting true preferences is optimal.

Note: “high probability” is as $\text{OPT} \gg h \log |\mathcal{G}|$.

Conclusions

1. GSP unlikely to optimize desired objectives.
2. ML can significantly help advertising market design.
 - predict supply.
 - learn preferences.
 - cluster tail.
 - pricing-based mechanisms.
3. advertising markets need pre-sale market.
4. pricing-based mechanisms may be right way to go.