

Link-Based  
Spam Detection

L. Becchetti,  
C. Castillo,  
D. Donato,  
S. Leonardi and  
R. Baeza-Yates

Motivation

Degree-based  
measures

PageRank

TrustRank

Truncated  
PageRank

Counting  
supporters

Conclusions

# Using Rank Propagation and Probabilistic Counting for Link-based Spam Detection

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## Web spam (keywords + links)

### Link-Based Spam Detection

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side effects, at strength of erection viagra levitra cialis, discount viagra buy viagra buy viagra viagradrugs.net, to cialis lawsuit, dirt cheap viagra, in sex discount cialis generic cialis bluepilled.com, herbal alternative viagra, for cialis marijuana, sublingual viagra.

Viagra users, will viagra facts cialis line prescription, buy viagra online viagra side effects natural alternative viagra, has cialis generic viagra generic cialis cialis cum-with-us.com, viagra discount, this brand name cialis, herbal viagra alternative free viagra buying deal viagradrugs.net cheapest price viagra cheap viagra uk free viagra viagra online pills pills viagradrugs.net, silagra weight loss generic viagra cialis cum-with-us.com, viagra blindness viagra prescription.

Amsterdam viagra sexshops viagra prescription for woman viagra online pharmacy, is cialis ordering online, viagra suppliers cocaine and viagra sex experiences viagra generico impotencia, cialis official website, viagra cheap generic cheap viagra natural viagra, will ciali, whats the chemical name for the drug viagra, are cialis and grapefruit, homemade viagra, has herbal cialis, strength of erection viagra levitra cialis.

**Viagra for women, has viagra cost lowest prices viagra, at cialis eli lilly, non prescription viagra, am cialis on line, viagra for women viagra expiration cialis fda approval, compare viagra and levitra viagra discount viagra cialis levitra, viagra online cheap cialis no prescription, 180 mg viagra levitra vs viagra uk viagra viagra sample, am generic cialis minuteviagra cum-with-us.com, free viagra online.**

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## Web spam (mostly keywords)

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# Search engine?

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Bookmark Home  
Page Home

**SOFT SEARCH**

**Top Searches:**

- ✦ Acne
- ✦ Weight Loss Pills
- ✦ Debt Consolidation
- ✦ Loan
- ✦ Domain Names
- ✦ Advertising
- ✦ Online Pharmacy
- ✦ Home Loan
- ✦ Dedicated Server
- ✦ Car Rental
- ✦ Adipex
- ✦ Levitra
- ✦ Online Poker
- ✦ Work At Home
- ✦ Propecia
- ✦ Consolidate Debt
- ✦ Mortgage Rates
- ✦ Online Craps
- ✦ Vegas Casinos
- ✦ Buy Ionamin



lava soft    php script    top soft    java script    MP3

### Top Web Results

Results 1-16 containing "sports book"

1. **Place Your Bet with #1 Sports Betting Site Online**  
Kentucky Derby, NBA, MLB, NHL and all other sports betting and odds. Place a full range sportsbook in North America  
<http://www.sportsinteraction.com>
2. **AnteUp GamblingLinks.com - Safe Online Casinos**  
Links to safe and secure online casino gambling and sports betting including reviews, ne  
<http://gamblinglinks.com>
3. **Free Casino Bonuses. Links To the Best Casinos**  
Get \$20 - \$500 in Free Chips. Most popular casino games with great graphics. Play for free rules and strategy. Links to the Best Casinos  
<http://www.fastfreecash.net>
4. **AnteUp GamblingLinks.com - Safe Online Casinos**

# Fake search engine

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→ Bookmark → Home Page → Home

**SOFT SEARCH**

**Top Searches:**

- ✦ Canadian Pharmacy
- ✦ Debt Consolidation
- ✦ Online Loan
- ✦ Diet
- ✦ Credit Reports
- ✦ Online Poker
- ✦ Xenical
- ✦ Buy Ionamin
- ✦ Diet Pills
- ✦ Online Craps
- ✦ DirecTV
- ✦ Life Insurance
- ✦ Dedicated Server
- ✦ Car Insurance
- ✦ Buy Phentermine
- ✦ Debt
- ✦ Weight Loss Pills
- ✦ Pay Day Loans
- ✦ Home Loan
- ✦ Refinance



lava soft    php script    top soft    java script    MP3

### Top Web Results

Results 1-16 containing "1293kasd132ka0sd1kj239asd123"

1. **A Real Work At Home Business Opportunity!**  
Free Home Business Match Up Service! We have helped 1000's of people make \$5,000  
<http://gozing.directtrack.com/z/1198/CD2127/>
2. **Exotic Holiday - Find Your Love**  
Exotic holiday is great way how to find love when you travel. Meet new people. Meet  
<http://www.exotic-holiday.co.uk/>
3. **Image, Photo, Digital, Video and Movie software**  
Find quality image management & digital asset software for your business. Also see  
<http://www.enterprise-software.co.uk>
4. **Renting a Birthday Party Limousine is Sexy**  
What better way to surprise your loved one on their special day than with a birthday party  
<http://partybusrental.info>

# Problem: "normal" pages that are spam

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Conclusions

## Website design, management, marketing and promotion

If you are searching for any of the following topics:

- ◆ [Website design, management, marketing and promotion.](#)
- ◆ [Website design, management, marketing and promotion resources.](#)
- ◆ [Website design, management, marketing and promotion related topics.](#)
- ◆ [Website design, management, marketing and promotion services.](#)

Look No further. You'll find it at [Website design, management, marketing and promotion!](#)

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# Link farms

## Link-Based Spam Detection

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R. Baeza-Yates

## Motivation

Degree-based measures

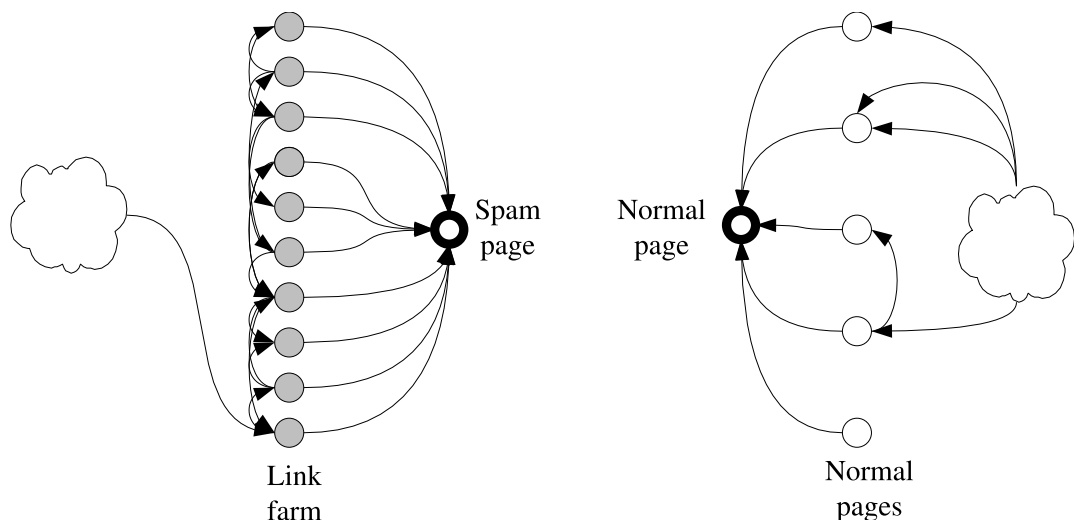
PageRank

TrustRank

Truncated PageRank

Counting supporters

Conclusions



Single-level farms can be detected by searching groups of nodes sharing their out-links [Gibson et al., 2005]

# Motivation

## Link-Based Spam Detection

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## Motivation

Degree-based measures

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Conclusions

[Fetterly et al., 2004] hypothesized that studying the distribution of statistics about pages could be a good way of detecting spam pages:

**“in a number of these distributions, outlier values are associated with web spam”**

## Research goal

Statistical analysis of link-based spam

# Metrics

## Link-Based Spam Detection

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Conclusions

### *Graph algorithms*

All shortest paths, centrality, betweenness, clustering coefficient...

### *Streamed algorithms*

Breadth-first and depth-first search

Count of neighbors

### *Symmetric algorithms*

(Strongly) connected components

Approximate count of neighbors

PageRank, Truncated PageRank, Linear Rank

HITS, Salsa, TrustRank

# Test collection

## Link-Based Spam Detection

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Conclusions

## U.K. collection

18.5 million pages downloaded from the .UK domain

5,344 hosts manually classified (6% of the hosts)

Classified entire hosts:

- ✓ **A few hosts are mixed:** spam and non-spam pages
- ✗ **More coverage:** sample covers 32% of the pages

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# Degree

## Link-Based Spam Detection

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Motivation

Degree-based measures

PageRank

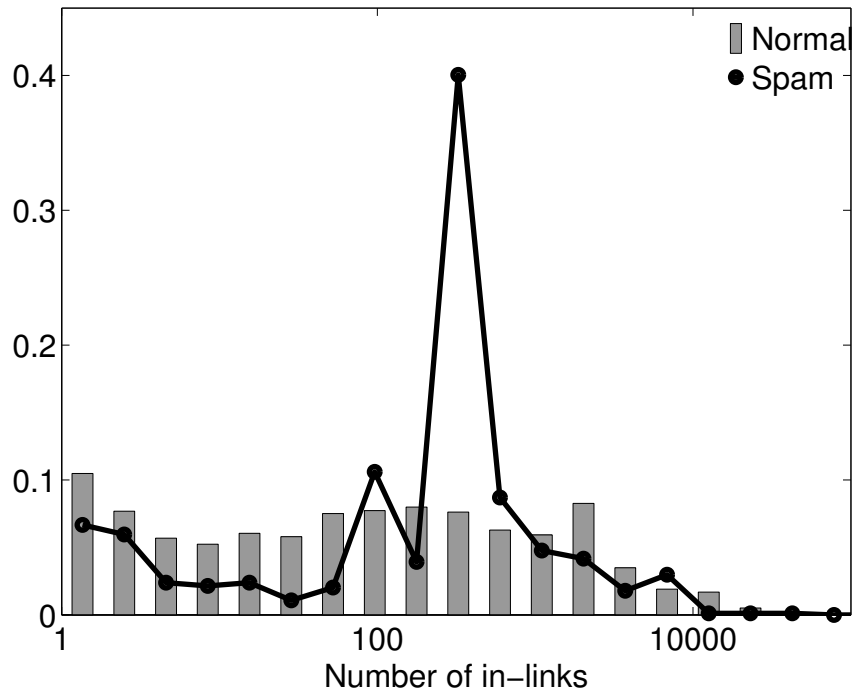
TrustRank

Truncated PageRank

Counting supporters

Conclusions

### In-degree $\delta = 0.35$



( $\delta = \text{max. difference in C.D.F. plot}$ )

# Degree

## Link-Based Spam Detection

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Motivation

Degree-based measures

PageRank

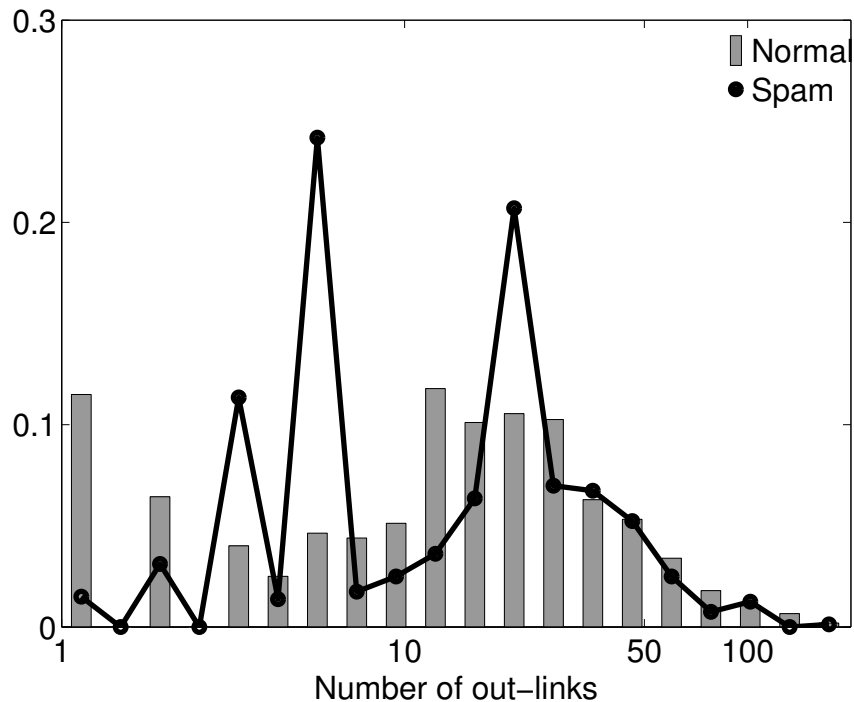
TrustRank

Truncated PageRank

Counting supporters

Conclusions

### Out-degree $\delta = 0.28$





# Edge reciprocity

## Link-Based Spam Detection

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Motivation

Degree-based measures

PageRank

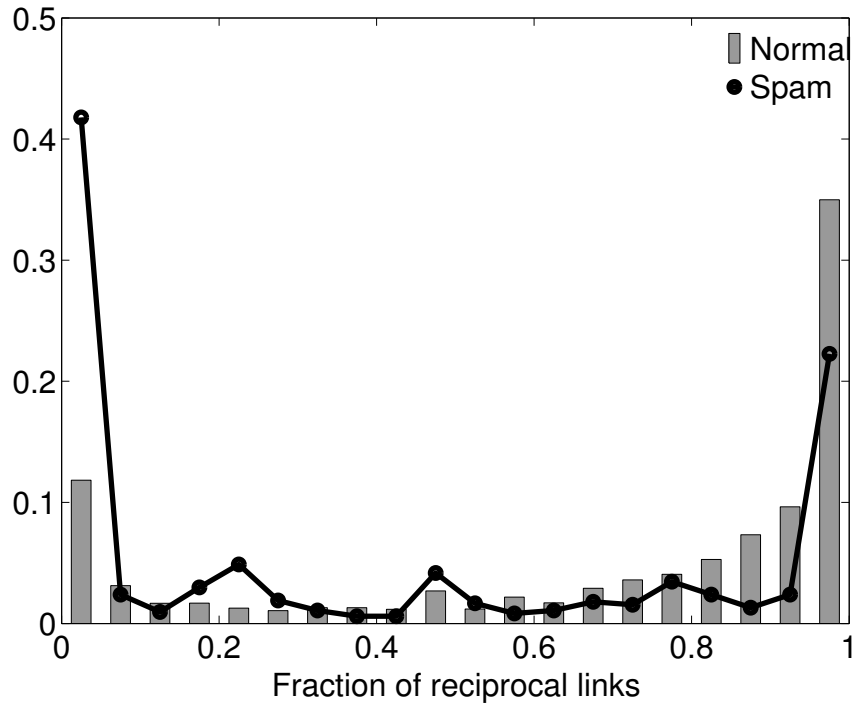
TrustRank

Truncated PageRank

Counting supporters

Conclusions

Reciprocity of max. PR page  $\delta = 0.35$



# Assortativity

## Link-Based Spam Detection

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Motivation

Degree-based measures

PageRank

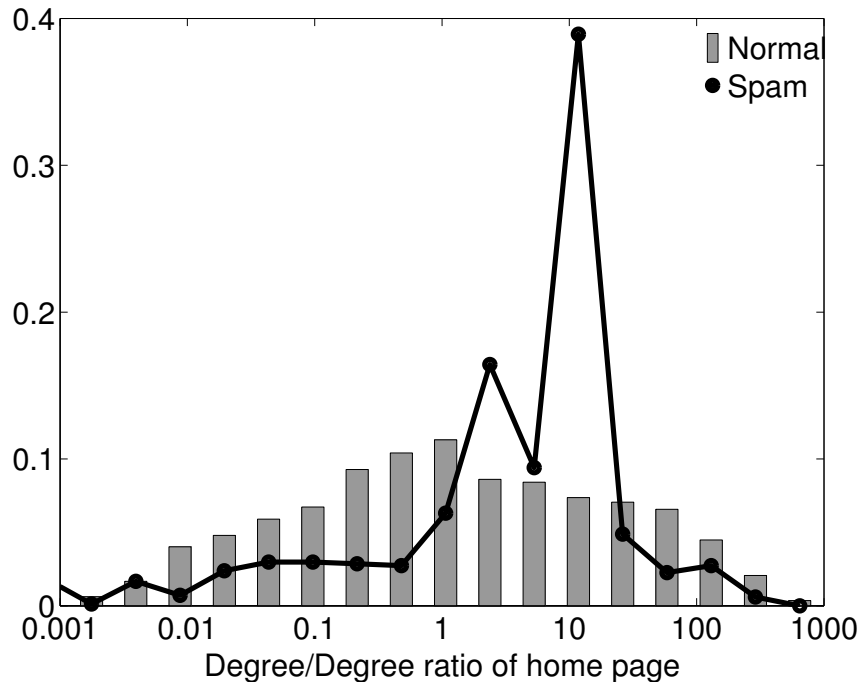
TrustRank

Truncated PageRank

Counting supporters

Conclusions

Degree / Degree of neighbors  $\delta = 0.31$



# Automatic classifier

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### Motivation

### Degree-based measures

### PageRank

### TrustRank

### Truncated PageRank

### Counting supporters

### Conclusions

All of the following attributes in the home page and the page with the maximum PageRank, plus a binary variable indicating if they are the same page:

- In-degree, out-degree
- Fraction of reciprocal edges
- Degree divided by degree of direct neighbors
- Average and sum of in-degree of out-neighbors
- Average and sum of out-degree of in-neighbors

## Decision tree

72.6% of detection rate, with 3.1% false positives

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# PageRank

## Link-Based Spam Detection

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## Motivation

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## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

Let  $\mathbf{P}_{N \times N}$  be the normalized link matrix of a graph

- Row-normalized
- No “sinks”

## Definition (PageRank)

Stationary state of:

$$\alpha \mathbf{P} + \frac{(1 - \alpha)}{N} \mathbf{1}_{N \times N}$$

- Follow links with probability  $\alpha$
- Random jump with probability  $1 - \alpha$

# Maximum PageRank in the Host

## Link-Based Spam Detection

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R. Baeza-Yates

## Motivation

## Degree-based measures

## PageRank

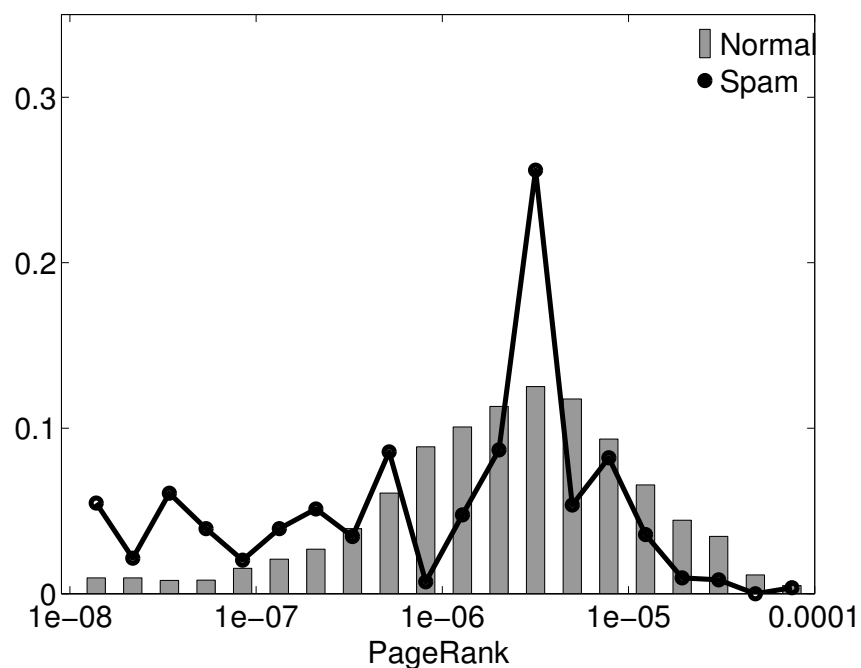
## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

Maximum PageRank of the site  $\delta = 0.23$



# Variance of PageRank

Suggested in [Benczúr et al., 2005]

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Motivation

Degree-based measures

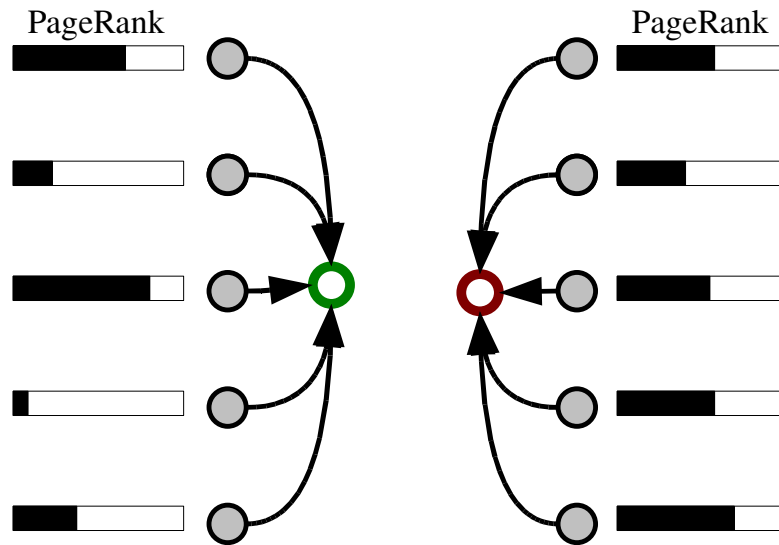
PageRank

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Conclusions



# Variance of PageRank of in-neighbors

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Degree-based measures

PageRank

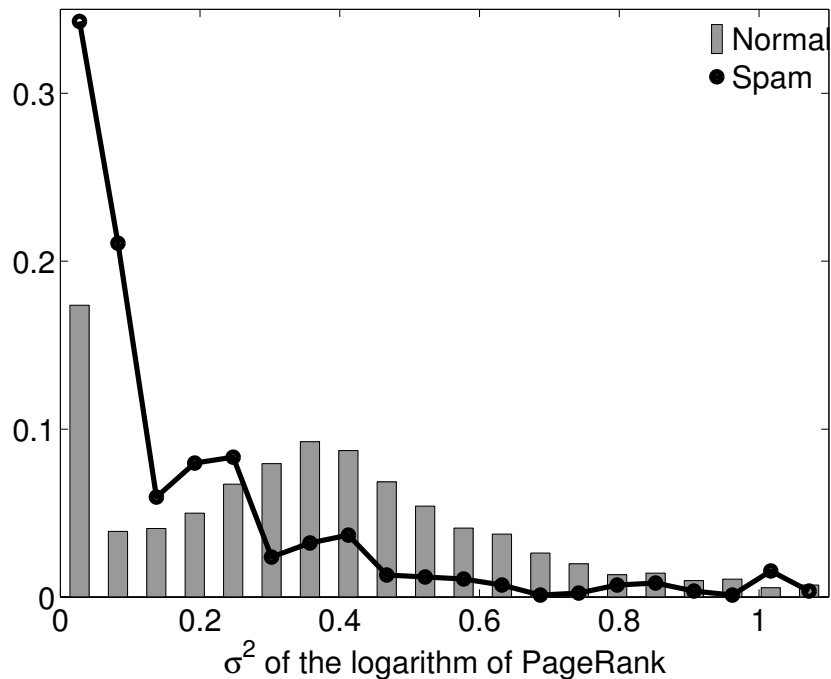
TrustRank

Truncated PageRank

Counting supporters

Conclusions

Stdev. of PR of Neighbors (Home)  $\delta = 0.41$



# Automatic classifier

## Link-Based Spam Detection

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## Motivation

## Degree-based measures

## PageRank

## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

Features: degree-based plus the following in the home page and the page with maximum PageRank:

- PageRank
- In-degree/PageRank
- Out-degree/PageRank
- Standard deviation of PageRank of in-neighbors =  $\sigma^2$
- $\sigma^2$ /PageRank

Plus the PageRank of the home page divided by the PageRank of the page with the maximum PageRank.

## Decision tree

74.4% of detection rate, with 2.6% false positives  
(Degree-based: 72.6% of detection, 3.1% false positives)

## Link-Based Spam Detection

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## Motivation

## Degree-based measures

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# TrustRank

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## Motivation

## Degree-based measures

## PageRank

## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

## TrustRank [Gyöngyi et al., 2004]

A node with high PageRank, but far away from a core set of “trusted nodes” is suspicious

Start from a set of trusted nodes, then do a random walk, returning to the set of trusted nodes with probability  $1 - \alpha$  at each step

 Trusted nodes: data from <http://www.dmoz.org/>

# TrustRank score

## Link-Based Spam Detection

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## PageRank

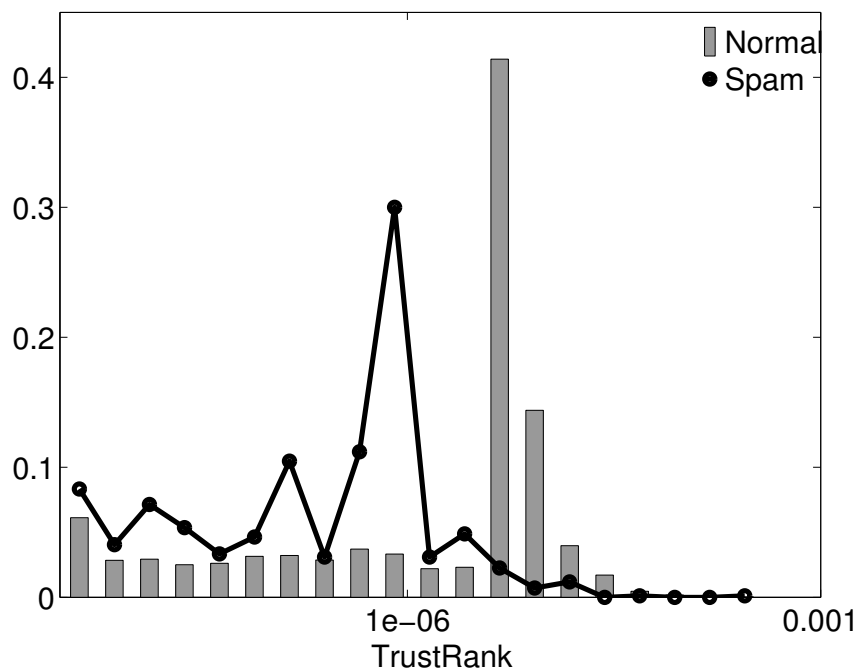
## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

## TrustRank score of home page $\delta = 0.59$



## TrustRank / PageRank

### Link-Based Spam Detection

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PageRank

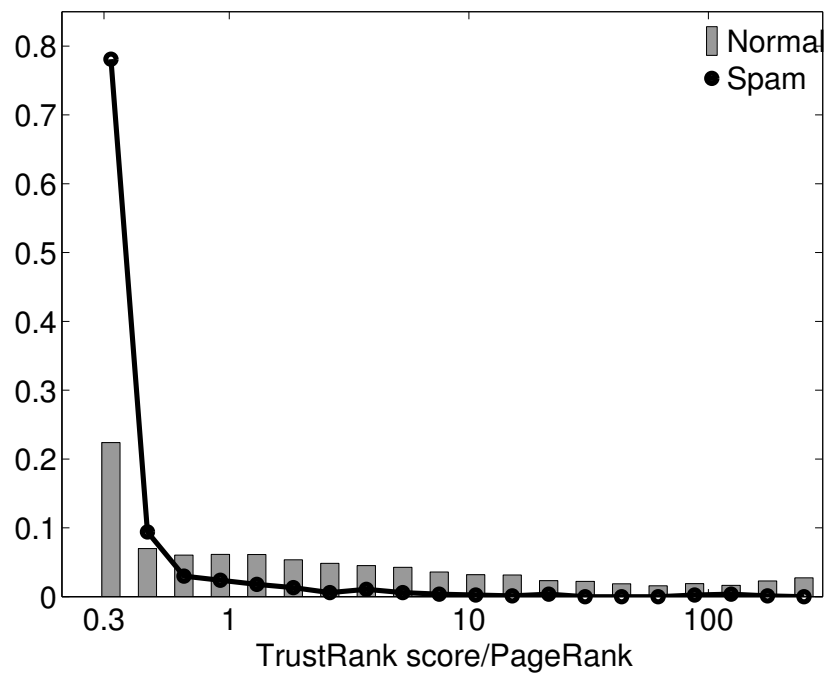
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Estimated relative non-spam mass  $\delta = 0.59$



## Automatic classifier

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Conclusions

PageRank attributes, plus the following in the home page and the page with maximum PageRank:

- TrustScore
- TrustScore/PageRank (estimated relative non-spam mass)
- TrustScore/In-degree

Plus the TrustScore in the home page divided by the TrustScore in the page with the maximum PageRank.

### Decision tree

77.3% of detection rate, with 3.0% false positives  
(PageRank-based: 74.4% of detection, 2.6% false positives)

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## Path-based formula for PageRank

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Given a path  $p = \langle x_1, x_2, \dots, x_t \rangle$  of length  $t = |p|$

$$\text{branching}(p) = \frac{1}{d_1 d_2 \cdots d_{t-1}}$$

where  $d_i$  are the out-degrees of the members of the path

**Explicit formula for PageRank [Newman et al., 2001]**

$$r_i(\alpha) = \sum_{p \in \text{Path}(-, i)} \frac{(1 - \alpha)\alpha^{|p|}}{N} \text{branching}(p)$$

$\text{Path}(-, i)$  are incoming paths in node  $i$

# General functional ranking

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In general:

$$r_i(\alpha) = \sum_{p \in \text{Path}(-, i)} \frac{\text{damping}(|p|)}{N} \text{branching}(p)$$

There are many choices for  $\text{damping}(|p|)$ , including simply a linear function that is as good as PageRank in practice [Baeza-Yates et al., 2006]

# Truncated PageRank

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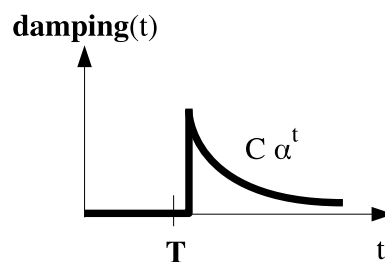
TrustRank

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Conclusions

Reduce the direct contribution of the first levels of links:



$$\text{damping}(t) = \begin{cases} 0 & t \leq T \\ C\alpha^t & t > T \end{cases}$$

✓ No extra reading of the graph after PageRank

# Truncated PageRank(T=2) / PageRank

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PageRank

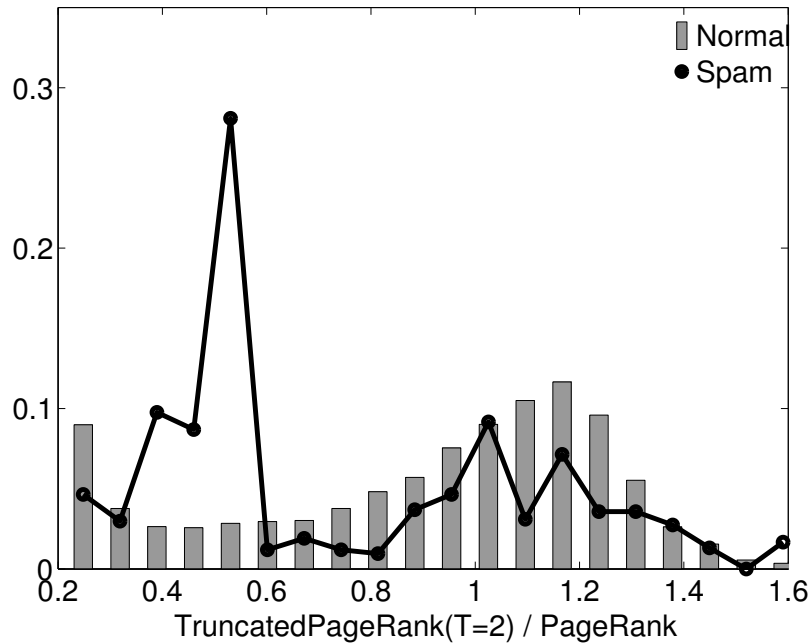
TrustRank

Truncated PageRank

Counting supporters

Conclusions

TruncatedPageRank T=2 / PageRank  $\delta = 0.30$



# Max. change of Truncated PageRank

Link-Based Spam Detection

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C. Castillo,  
D. Donato,  
S. Leonardi and  
R. Baeza-Yates

Motivation

Degree-based measures

PageRank

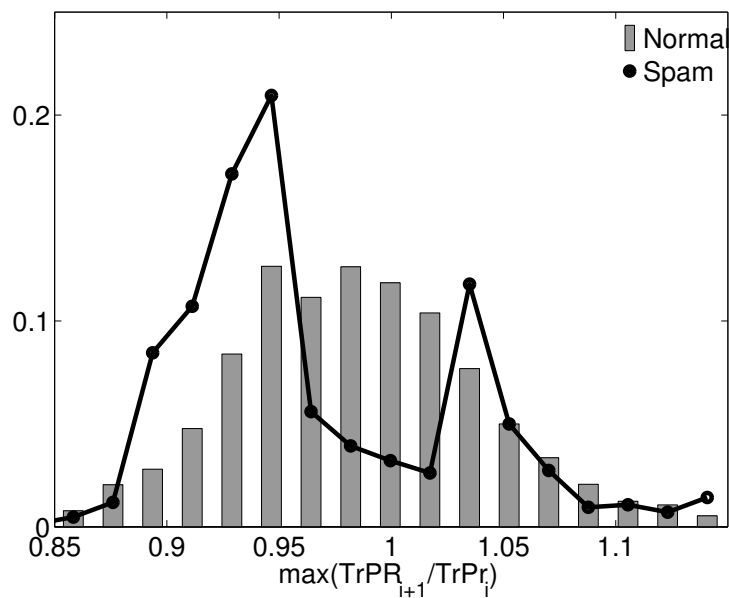
TrustRank

Truncated PageRank

Counting supporters

Conclusions

Maximum change of Truncated PageRank  $\delta = 0.29$





# Automatic classifier

## Link-Based Spam Detection

L. Becchetti,  
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D. Donato,  
S. Leonardi and  
R. Baeza-Yates

## Motivation

## Degree-based measures

## PageRank

## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

PageRank attributes, plus the following in the home page and the page with maximum PageRank:

- $\text{TruncPageRank}(T = 1 \dots 4)$
- $\text{TruncPageRank}(T = 4) / \text{TruncPageRank}(T = 3)$
- $\text{TruncPageRank}(T = 3) / \text{TruncPageRank}(T = 2)$
- $\text{TruncPageRank}(T = 2) / \text{TruncPageRank}(T = 1)$
- $\text{TruncPageRank}(T = 1 \dots 4) / \text{PageRank}$
- Minimum, maximum and average of:  
 $\text{TruncPageRank}(T = i) / \text{TruncPageRank}(T = i - 1)$

Plus the  $\text{TruncatedPageRank}(T = 1 \dots 4)$  of the home page divided by the same value in the page with the maximum PageRank.

## Decision tree

76.9% of detection rate, with 2.5% false positives  
(TrustRank-based: 77.3% of detection, 3.0% false positives)

## Link-Based Spam Detection

L. Becchetti,  
C. Castillo,  
D. Donato,  
S. Leonardi and  
R. Baeza-Yates

## Motivation

## Degree-based measures

## PageRank

## TrustRank

## Truncated PageRank

## Counting supporters

## Conclusions

- 1 Motivation
- 2 Degree-based measures
- 3 PageRank
- 4 TrustRank
- 5 Truncated PageRank
- 6 Counting supporters
- 7 Conclusions

# Idea: count “supporters” at different distances

## Link-Based Spam Detection

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D. Donato,  
S. Leonardi and  
R. Baeza-Yates

### Motivation

### Degree-based measures

### PageRank

### TrustRank

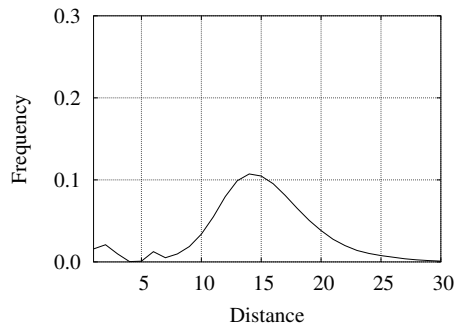
### Truncated PageRank

### Counting supporters

### Conclusions

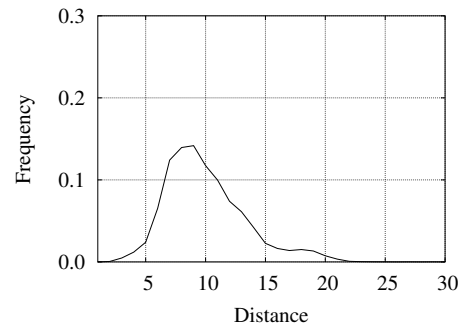
Number of different nodes at a given distance:

**.UK** 18 mill. nodes



Average distance  
14.9 clicks

**.EU.INT** 860,000 nodes



Average distance  
10.0 clicks

# High and low-ranked pages are different

## Link-Based Spam Detection

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S. Leonardi and  
R. Baeza-Yates

### Motivation

### Degree-based measures

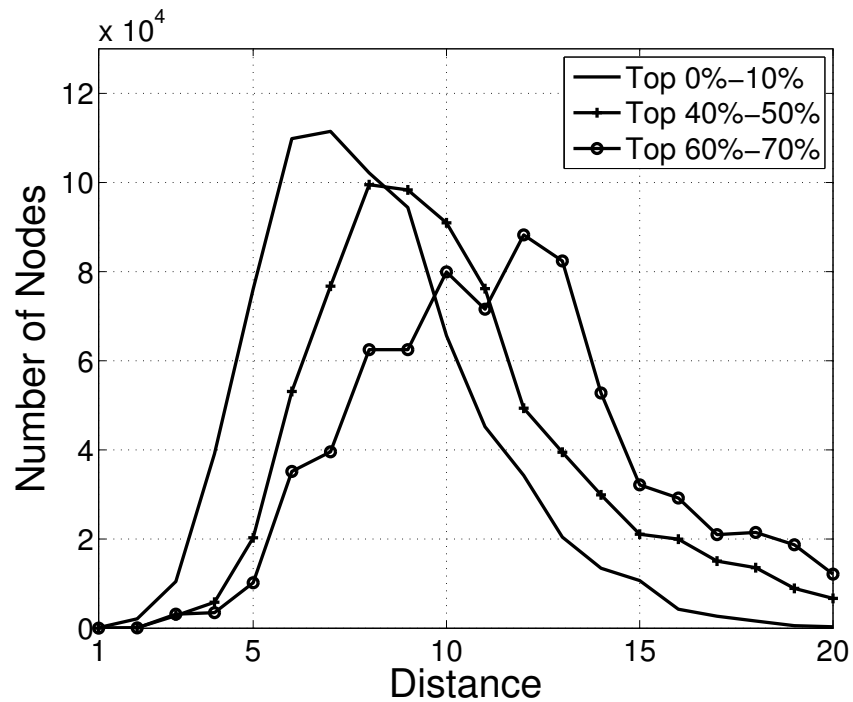
### PageRank

### TrustRank

### Truncated PageRank

### Counting supporters

### Conclusions



Areas below the curves are equal if we are in the same strongly-connected component

## Probabilistic counting

Link-Based  
Spam Detection

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S. Leonardi and  
R. Baeza-Yates

Motivation

Degree-based  
measures

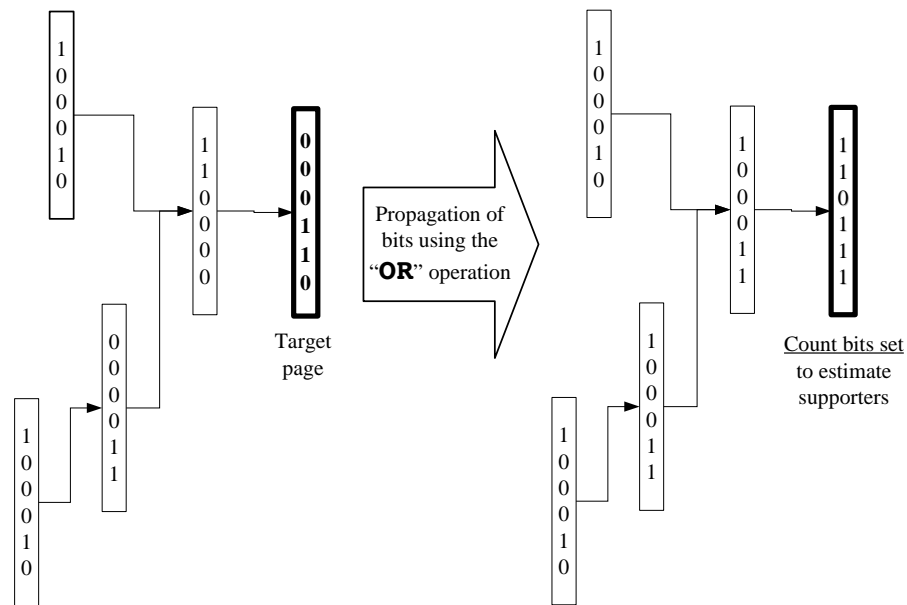
PageRank

TrustRank

Truncated  
PageRank

Counting  
supporters

Conclusions



Improvement of ANF algorithm [Palmer et al., 2002] based on probabilistic counting [Flajolet and Martin, 1985]

## General algorithm

Link-Based  
Spam Detection

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PageRank

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Conclusions

**Require:** N: number of nodes, d: distance, k: bits

- 1: **for** node : 1 ... N, bit: 1 ... k **do**
- 2:     INIT(node,bit)
- 3: **end for**
- 4: **for** distance : 1 ... d **do** {Iteration step}
- 5:     Aux  $\leftarrow \mathbf{0}_k$
- 6:     **for** src : 1 ... N **do** {Follow links in the graph}
- 7:         **for all** links from src to dest **do**
- 8:             Aux[dest]  $\leftarrow$  Aux[dest] OR V[src,.]
- 9:         **end for**
- 10:     **end for**
- 11:     V  $\leftarrow$  Aux
- 12: **end for**
- 13: **for** node: 1 ... N **do** {Estimate supporters}
- 14:     Supporters[node]  $\leftarrow$  ESTIMATE( V[node,.] )
- 15: **end for**
- 16: **return** Supporters

# Our estimator

## Link-Based Spam Detection

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### Motivation

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### PageRank

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### Truncated PageRank

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### Conclusions

Initialize all bits to one with probability  $\epsilon$

Estimator:  $\text{neighbors}(node) = \log_{(1-\epsilon)} \left( 1 - \frac{\text{ones}(node)}{k} \right)$

## Adaptive estimation

Repeat the above process for  $\epsilon = 1/2, 1/4, 1/8, \dots$ , and look for the transitions from more than  $(1 - 1/e)k$  ones to less than  $(1 - 1/e)k$  ones.

# Convergence

## Link-Based Spam Detection

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### Motivation

### Degree-based measures

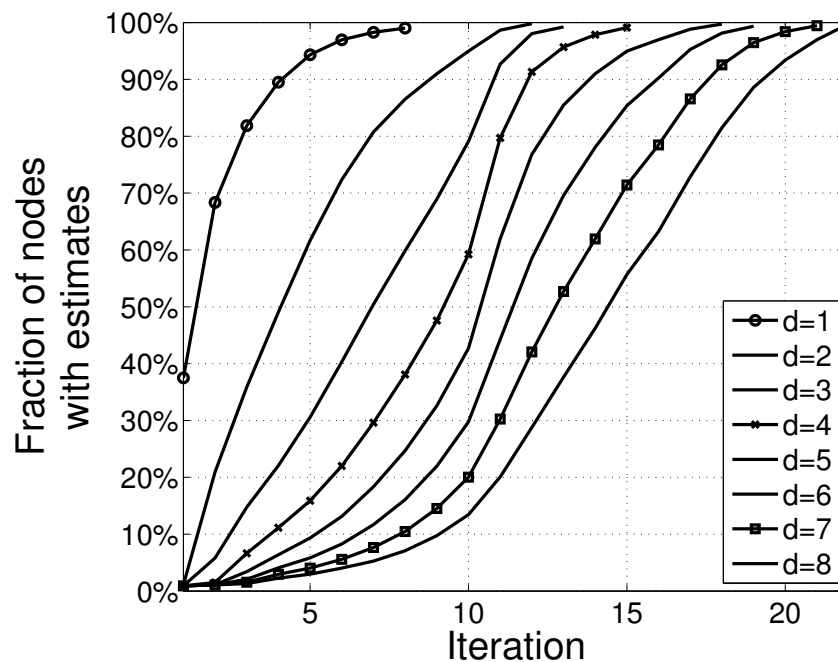
### PageRank

### TrustRank

### Truncated PageRank

### Counting supporters

### Conclusions



# Error rate

## Link-Based Spam Detection

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### Motivation

Degree-based measures

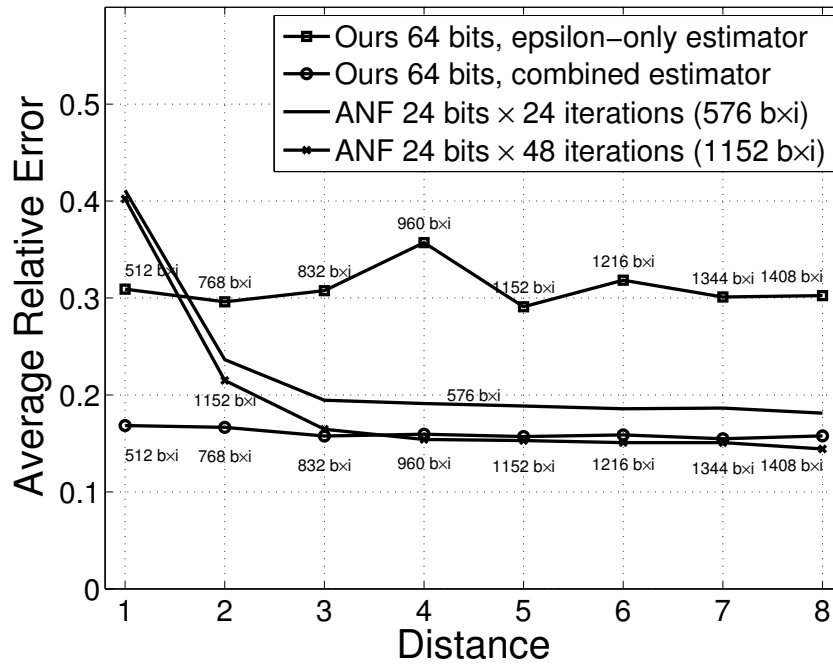
PageRank

TrustRank

Truncated PageRank

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Conclusions



# Hosts at distance 4

## Link-Based Spam Detection

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S. Leonardi and  
R. Baeza-Yates

### Motivation

Degree-based measures

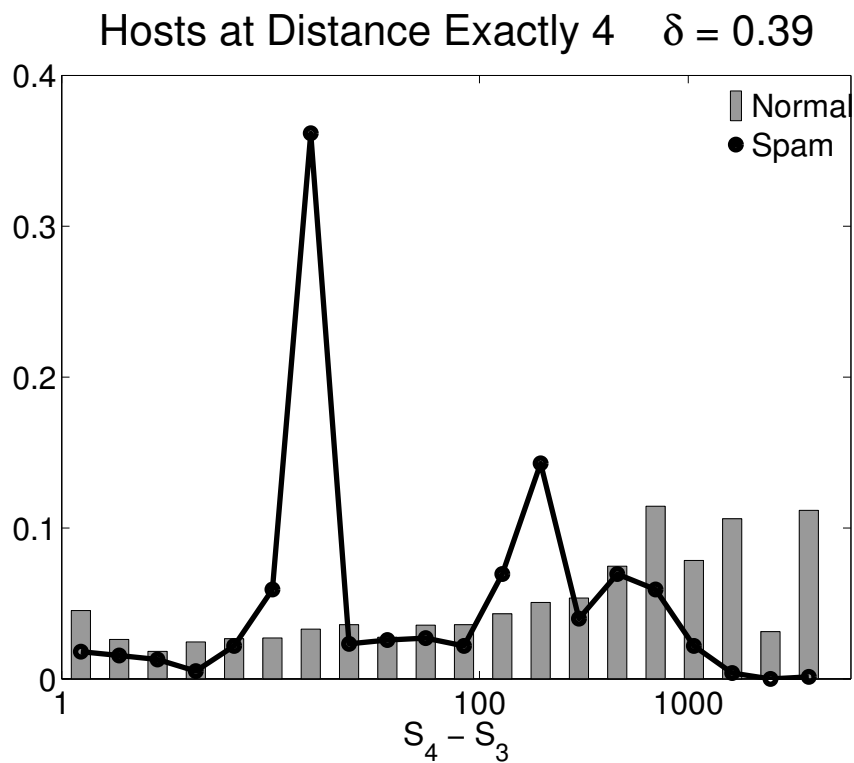
PageRank

TrustRank

Truncated PageRank

Counting supporters

Conclusions





## Minimum change of supporters

### Link-Based Spam Detection

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Motivation

Degree-based measures

PageRank

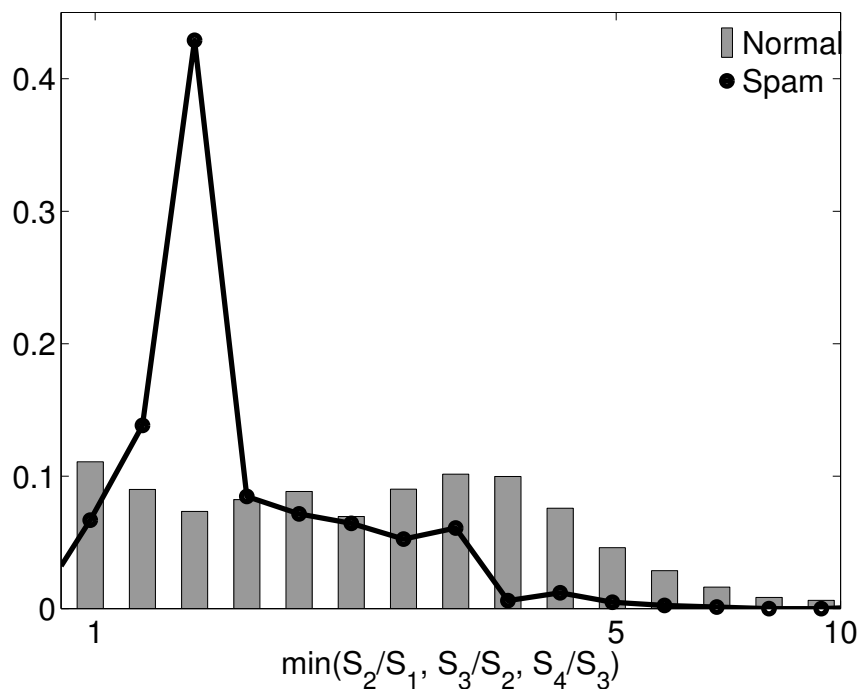
TrustRank

Truncated PageRank

Counting supporters

Conclusions

### Minimum change of supporters $\delta = 0.39$



## Automatic classifier

### Link-Based Spam Detection

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PageRank

TrustRank

Truncated PageRank

Counting supporters

Conclusions

PageRank attributes, plus the following in the home page and the page with maximum PageRank:

- Supporters at 2...4
- Supporters at 2...4 / PageRank
- Supporters at  $i$  / Supporters at  $i - 1$  (for  $i = 1..4$ )
- Minimum, maximum and average of: Supporters at  $i$  / Supporters at  $i - 1$  (for  $i = 1..4$ )
- (Supporters at  $i$  - Supporters at  $i - 1$ ) / PageRank

Plus the number of supporters at distance 2...4 in the home page divided by the same feature in the page with the maximum PageRank.

### Decision tree

78.9% of detection rate, with 2.5% false positives  
(TruncPR: 76.9% of detection, 2.5% false positives)  
(TrustRank: 77.7% of detection, 3.0% false positives)

## Link-Based Spam Detection

L. Becchetti,  
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## Summary of classifiers

### Link-Based Spam Detection

L. Becchetti,  
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Conclusions

Metrics	Detection rate	False positives
Degree (D)	72.6%	3.1%
D + PageRank (P)	74.4%	2.6%
D + P + TrustRank	77.7%	3.0%
D + P + Trunc. PageRank	76.9%	2.5%
D + P + Est. of Supporters	78.9%	2.5%
All attributes	81.4%	2.8%
All attributes (more rules)	80.8%	1.1%

### Comparison

Content-based analysis [Ntoulas et al., 2006] has shown 86.2% detection rate with 2.2% false positives

Single-attribute classifier with TrustRank

[Gyöngyi et al., 2004]: 51.1% detection rate, 3.4% error in our sample – SpamRank [Benczúr et al., 2005] reports similar detection rates

## Top 10 metrics

### Link-Based Spam Detection

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### Motivation

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### Truncated PageRank

### Counting supporters

### Conclusions

1. Binary variable indicating if homepage is the page with maximum PageRank of the site
2. Edge reciprocity
3. Different hosts at distance 4
4. Different hosts at distance 3
5. Minimum change of supporters (different hosts)
6. Different hosts at distance 2
7. TruncatedPagerank (T=1) / PageRank
8. TrustRank score divided by PageRank
9. Different hosts at distance 1
10. TruncatedPagerank (T=2) / PageRank

## Conclusions

### Link-Based Spam Detection

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### Motivation

### Degree-based measures

### PageRank

### TrustRank

### Truncated PageRank

### Counting supporters

### Conclusions

- Link-based statistics to detect 80% of spam
- No magic bullet in link analysis
- Precision still low compared to e-mail spam filters
- Measure both home page and max. PageRank page
- Host-based counts are important

Next step: combine link analysis and content analysis

## Link-Based Spam Detection

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Thank you!

## Link-Based Spam Detection

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supporters

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Baeza-Yates, R., Boldi, P., and Castillo, C. (2006).

Generalizing pagerank: Damping functions for link-based ranking algorithms.

In *Proceedings of SIGIR*, Seattle, Washington, USA. ACM Press.



Becchetti, L., Castillo, C., Donato, D., Leonardi, S., and Baeza-Yates, R. (2006).

Using rank propagation and probabilistic counting for link-based spam detection.

Technical report, DELIS – Dynamically Evolving, Large-Scale Information Systems.



Benczúr, A. A., Csalogány, K., Sarlós, T., and Uher, M. (2005).

Spamrank: fully automatic link spam detection.

In *Proceedings of the First International Workshop on Adversarial Information Retrieval on the Web*, Chiba, Japan.

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Fetterly, D., Manasse, M., and Najork, M. (2004).

Spam, damn spam, and statistics: Using statistical analysis to locate spam web pages.

In *Proceedings of the seventh workshop on the Web and databases (WebDB)*, pages 1–6, Paris, France.



Flajolet, P. and Martin, N. G. (1985).

Probabilistic counting algorithms for data base applications.

*Journal of Computer and System Sciences*, 31(2):182–209.



Gibson, D., Kumar, R., and Tomkins, A. (2005).

Discovering large dense subgraphs in massive graphs.

In *VLDB '05: Proceedings of the 31st international conference on Very large data bases*, pages 721–732. VLDB Endowment.

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Gyöngyi, Z., Molina, H. G., and Pedersen, J. (2004).

Combating web spam with trustrank.

In *Proceedings of the Thirtieth International Conference on Very Large Data Bases (VLDB)*, pages 576–587, Toronto, Canada. Morgan Kaufmann.



Newman, M. E., Strogatz, S. H., and Watts, D. J. (2001).

Random graphs with arbitrary degree distributions and their applications.

*Phys Rev E Stat Nonlin Soft Matter Phys*, 64(2 Pt 2).



Ntoulas, A., Najork, M., and Manasse, M. a. (2006).

Detecting spam web pages through content analysis.

In *To appear in proceedings of the World Wide Web conference*, Edinburgh, Scotland.

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Palmer, C. R., Gibbons, P. B., and Faloutsos, C. (2002).  
ANF: a fast and scalable tool for data mining in massive  
graphs.

*In Proceedings of the eighth ACM SIGKDD international  
conference on Knowledge discovery and data mining, pages  
81–90, New York, NY, USA. ACM Press.*