## Learning to Infer Social Ties in Large Networks

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## Real social networks are complex...

- Nobody exists only in one social network.
- Public network vs. private network
- Business network vs. family network
- However, existing networks (e.g., Facebook and Twitter) are trying to lump everyone into one big network
- FB tries to solve this problem via lists/groups
- However...
- Google+

which circle? Users do not take time to create it.



## Even complex than we imagined!

- Only $16 \%$ of mobile phone users in Europe have created custom contact groups
- users do not take the time to create it
- users do not know how to circle their friends
- The fact is that our social network is black-white... How to infer social ties?


## Example: Mobile network



## Example: Coauthor networks



Advisor-Advisee
Advisee-Advisor
Coauthor

## Challenges

1. Relationships in Mobile Network


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## Challenges:

3.     - A generalized framework for inferring social ties?
$\mathrm{Co}_{0}$

- A scalable, efficient method?



## Problem Formulation

Input: $G=\left(V, E^{L}, E^{U}, R^{L}, W\right)$


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## Problem Formulation Input: $G=\left(V(E) E^{U}\right.$, (R) $\left.w\right)$



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## Basic Idea



## Partially Labeled Pairwise Factor Graph Model (PLP-FGM)



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Map relationship to nodes in model

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Example:
Call frequency between two users?

## Partially Labeled Pairwise Factor Graph Model (PLP-FGM)



Map relationship to nodes in model

## Example:

A makes call to B immediately after the call to C.

# Partially Labeled Pairwise Factor Graph Model (PLP-FGM) 



Map relationship to nodes in model

# Partially Labeled Pairwise Factor Graph Model (PLP-FGM) 



## Problem:

Ma
For each relationship, identify which type has the highest probability?

## Solutions $_{\left(\text {con't }^{\prime}\right)}$

- Different ways to instantiate factors
- We use exponential-linear functions
- Attribute Factor:

$$
f\left(y_{i}, \mathbf{x}_{i}\right)=\frac{1}{Z_{\lambda}} \exp \left\{\lambda^{T} \boldsymbol{\Phi}\left(y_{i}, \mathbf{x}_{i}\right)\right\}
$$

- Correlation / Constraint Factor:

$$
\begin{aligned}
& g\left(y_{i}, G\left(y_{i}\right)\right)=\frac{1}{Z_{\alpha}} \exp \left\{\sum_{y_{j} \in G\left(y_{i}\right)} \alpha^{T} \mathbf{g}\left(y_{i}, y_{j}\right)\right\} \\
& h\left(y_{i}, H\left(y_{i}\right)\right)=\frac{1}{Z_{\beta}} \exp \left\{\sum_{y_{j} \in H\left(y_{i}\right)} \beta^{T} \mathbf{h}\left(y_{i}, y_{j}\right)\right\}
\end{aligned}
$$

- $\quad \theta=[\lambda, \alpha, \beta], s=\left[\Phi^{T}, g^{T}, h^{T}\right]^{T}$
- Log-Likelihood of labeled data:

$$
\mathcal{O}(\theta)=\log \sum_{Y \mid Y^{L}} \exp \left\{\theta^{T} \mathbf{S}\right\}-\log \sum_{Y} \exp \left\{\theta^{T} \mathbf{S}\right\}
$$

## Learning Algorithm

- Maximize the log-likelihood of labeled relationships

```
Input: learning rate \(\eta\)
Output: learned parameters \(\theta\)
Initialize \(\theta\);
repeat
    Calculate \(\mathbb{E}_{p_{\theta}\left(Y \mid Y^{L}, G\right)} \mathbf{S}\) using LBP ;
    Calculate \(\mathbb{E}_{p_{\theta}(Y \mid G)} \mathbf{S}\) using LBP ;
    Calculate the gradient of \(\theta\) according to Eq. 7:
    \(\nabla_{\theta}=\mathbb{E}_{p_{\theta}\left(Y \mid Y^{L}, G\right)} \mathbf{S}-\mathbb{E}_{p_{\theta}(Y \mid G)} \mathbf{S}\)
    Update parameter \(\theta\) with the learning rate \(\eta\) : Expectation Computing
    \(\theta_{\text {new }}=\theta_{\text {old }}-\eta \cdot \nabla_{\theta}\) Loopy Belief Propagation
until Convergence;
```

Algorithm 1: Learning PLP-FGM.

## Gradient Decent Method

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## Distributed Learning



## Data Sets

- Coauthor Network (Publication)
- To infer Advisor-Advisee relationship
- Papers from DBLP
- Email Network (Email)
- To infer Manger-Subordinate relationship
- Using Enron Email Dataset
- Mobile Network (Mobile)
- To infer Friendship
- 107 users (ten-month). Published by MIT

| Data Set | Users | Unlabeled <br> Relationships | Labeled <br> Relationships |
| :---: | :---: | :---: | :---: |
| Publication | $1,036,990$ | $1,984,164$ | 6,096 |
| Email | 151 | 3,424 | 148 |
| Mobile | 107 | 5,122 | 314 |

## Baselines

- Baselines:
- SVM:
- Use the same features defined in our model to train a classification model
- TPFG:
- An unsupervised method to identify advisor-advisee relationships
- PLP-FGM-S
- Do not use partially-labeled property
- Train parameters on the labeled sub-graph


## Performance Analysis

| Data Set | Method | Precision | Recall | F $_{\mathbf{1}}$-score |
| :---: | :---: | :---: | :---: | :---: |
| Publication | SVM | 72.5 | 54.9 | 62.1 |
|  | TPFG | 82.8 | $\mathbf{8 9 . 4}$ | 86.0 |
|  | PLP-FGM-S | 77.1 | 78.4 | 77.7 |
|  | PLP-FGM | $\mathbf{9 1 . 4}$ | 87.7 | $\mathbf{8 9 . 5}$ |
| Email | SVM | 79.1 | $\mathbf{8 8 . 6}$ | 83.6 |
|  | PLP-FGM-S | 85.8 | 85.6 | 85.7 |
|  | PLP-FGM | $\mathbf{8 8 . 6}$ | 87.2 | $\mathbf{8 7 . 9}$ |
| Mobile | SVM | $\mathbf{9 2 . 7}$ | 64.9 | 76.4 |
|  | PLP-FGM-S | 88.1 | 71.3 | 78.8 |
|  | PLP-FGM | 89.4 | $\mathbf{7 5 . 2}$ | $\mathbf{8 1 . 6}$ |

SVM: Use the same feature to train a classification model
TPFG: An unsupervised method to identify advisor-advisee relationships
PLP-FGM-S:Train PLP-FGM model on the labeled sub-graph

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## Factor Contribution Analysis (Email)



- Co-Recipient : $a \rightarrow(b, c)$ more than 10 mails
- Co-Manager : ( $a, b$ ) - $(a, c)$
- Co-Subordinate: (b, a) - (c, a)


## Factor Contribution Analysis (Email)



## Distributed Learning Performance




## System cs: Armecrimer



## Conclusion

- Formulate the problem of inferring the types of social ties
- Propose the PLP-FGM model to solve this problem, and present a distributed learning algorithm
- Validate the approach in different real data sets


## Future work

- Make online social networks colorful
- How to involve user into learning process?
- Connect with social theories?


## Thank you!

Any Questions?

## Correlation Definition

- Mobile Dataset:
- Co-location
- 3 users in the same location.
- Related-call
- A Make a call to B\&C at the same place/time
- For more information, please refer to the paper©


## Feature Definition

| Data set | Factor | Description |
| :---: | :---: | :---: |
| Publication | Paper count | $\left\|P_{i}\right\|, \mid P_{j}$ |
|  | Paper ratio | $P_{i}\left\|/\left\|P_{j}\right\|\right.$ |
|  | Coauthor ratio | $P_{i} \cap P_{j}\left\|/\left\|P_{i}\right\|,\left\|P_{i} \cap P_{j}\right\| /\left\|P_{j}\right\|\right.$ |
|  | Conference coverage | The proportion of the conferences which both $v_{i}$ and $v_{j}$ attended among conferences $v_{j}$ attended. |
|  | First-paper-year-diff | The difference in year of the earliest publication of $v_{i}$ and $v_{j}$. |
| Email | Traffics | Sender $\quad$ Recipients Include |
|  |  | $v_{i} \quad v_{j}$ |
|  |  | $v_{j} \quad \square v_{i}$ |
|  |  | $v_{i} \quad v_{k}$ and not $v_{j}$ |
|  |  | $v_{j} \quad v_{k}$ and not $v_{i}$ |
|  |  | $v_{k} \quad v_{i}$ and not $v_{j}$ |
|  |  | $v_{k} \quad v_{j}$ and not $v_{i}$ |
|  |  | $v_{k} \quad v_{i}$ and $v_{j}$ |
| Mobile | \#voice calls | The total number of voice call logs between two users. |
|  | \#messages | Number of messages between two users. |
|  | Night-call ratio | The proportion of calls at night (8pm to 8am). |
|  | Call duration | The total duration time of calls between two users. |
|  | \#proximity | The total number of proximity logs between two users. |
|  | In-role proximity ratio | The proportion of proximity logs in "working place" and in working hours ( 8 am to 8 pm ). |

## Existing Methods...

- [Diehl:07] try to identify the relationships by learning a ranking function in Email network.
- Wang et al. [Wang:10] propose an unsupervised algorithm for mining the advisor-advisee relationships from the Publication network.
- Both algorithms focus on a specific domain
- not easy to extend to other problems.

