

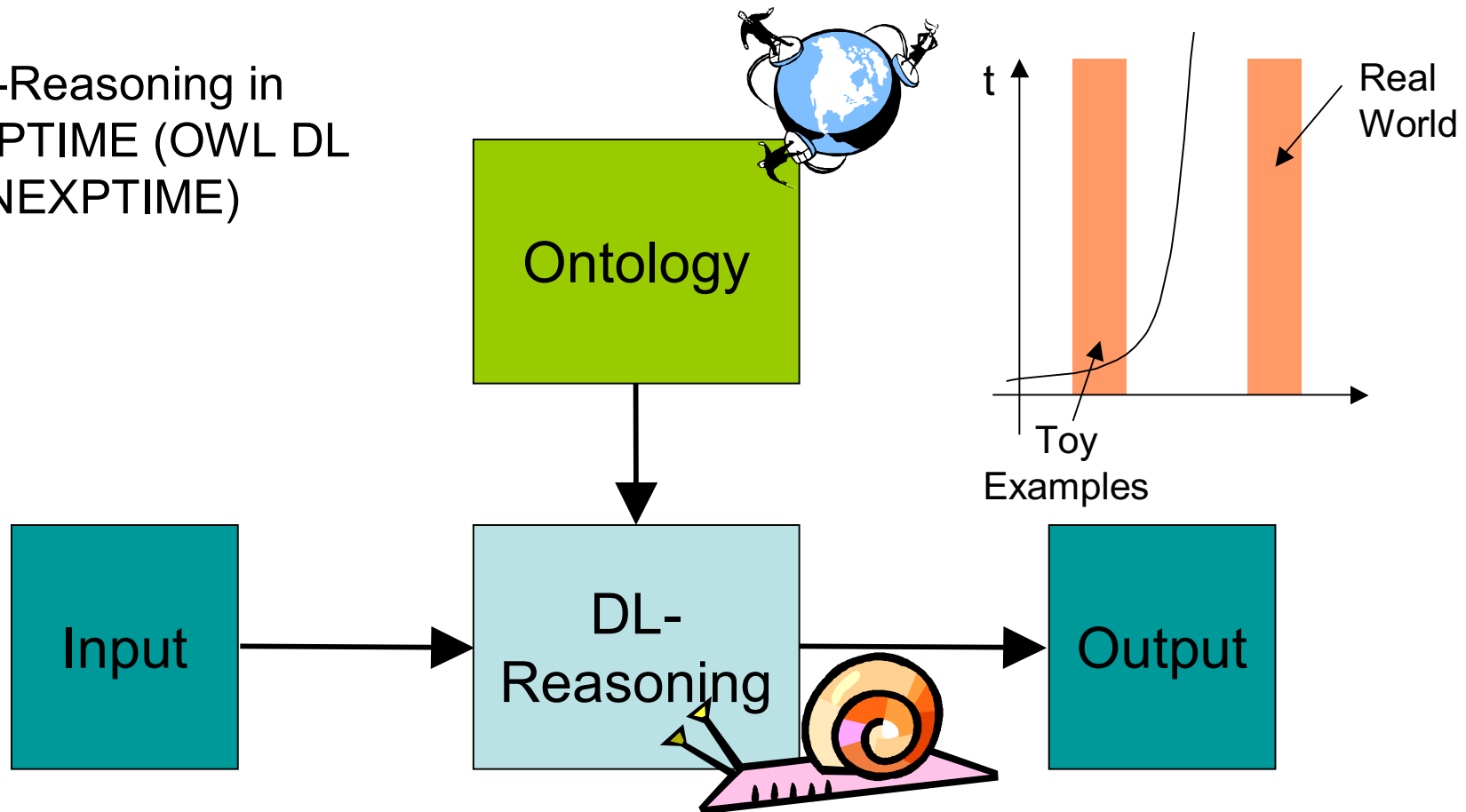
Approximate Deduction

This material by
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(VU, Knowledge Web)

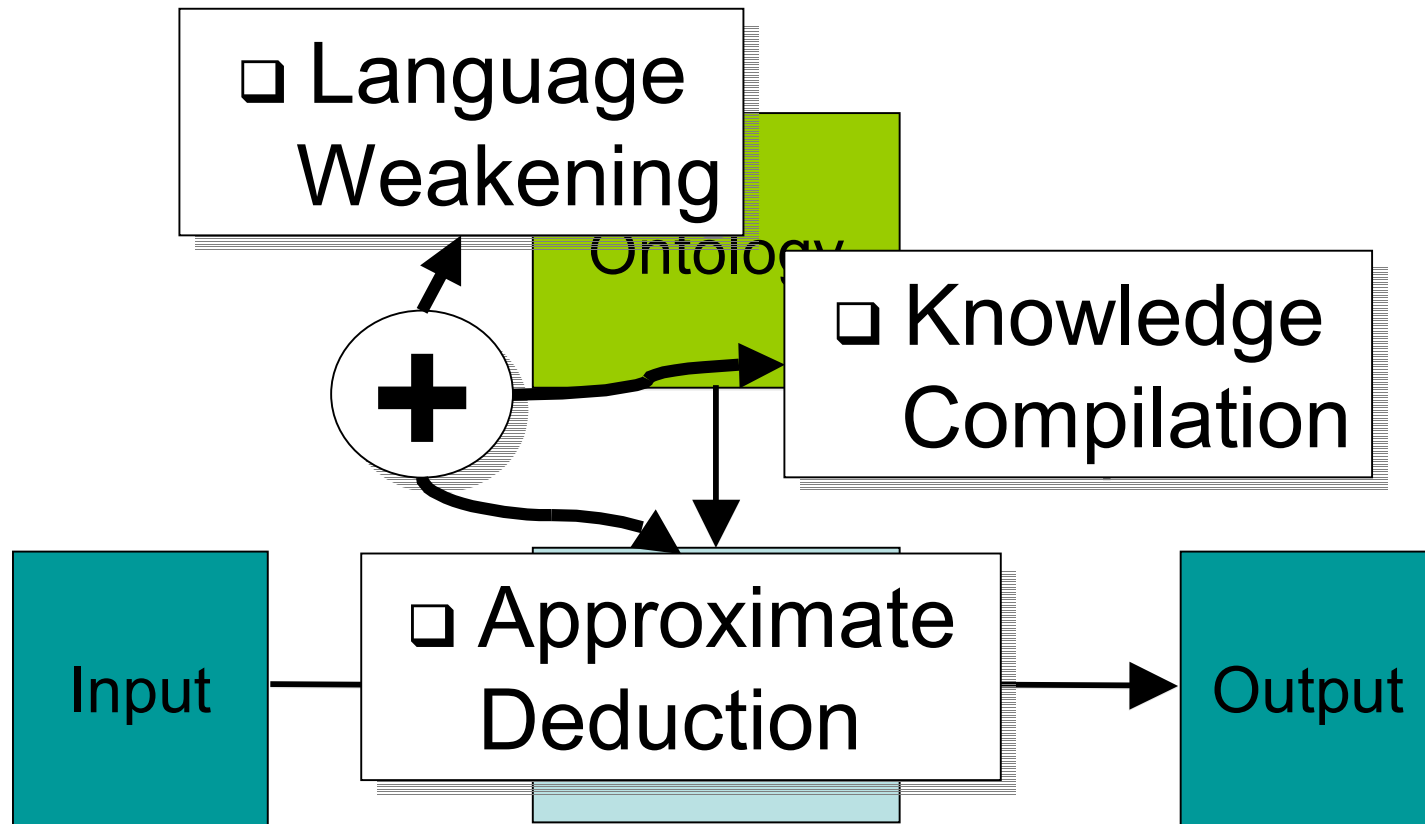


Approximation (in Semantic Web System)

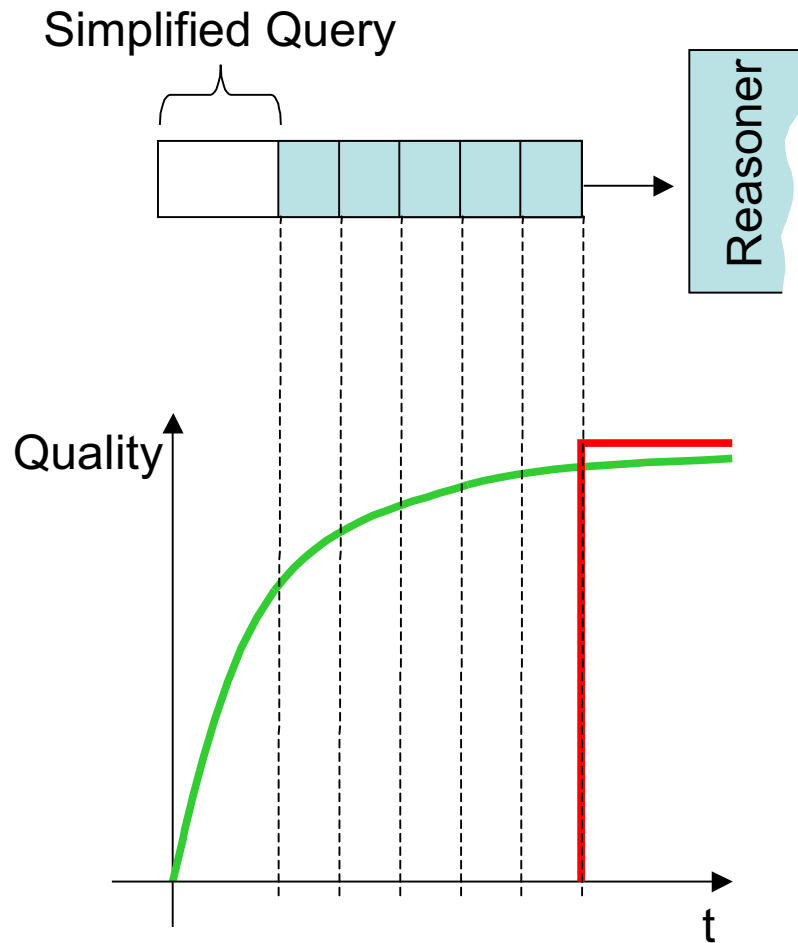
- DL-Reasoning in EXPTIME (OWL DL in NEXPTIME)



Approximation Approaches



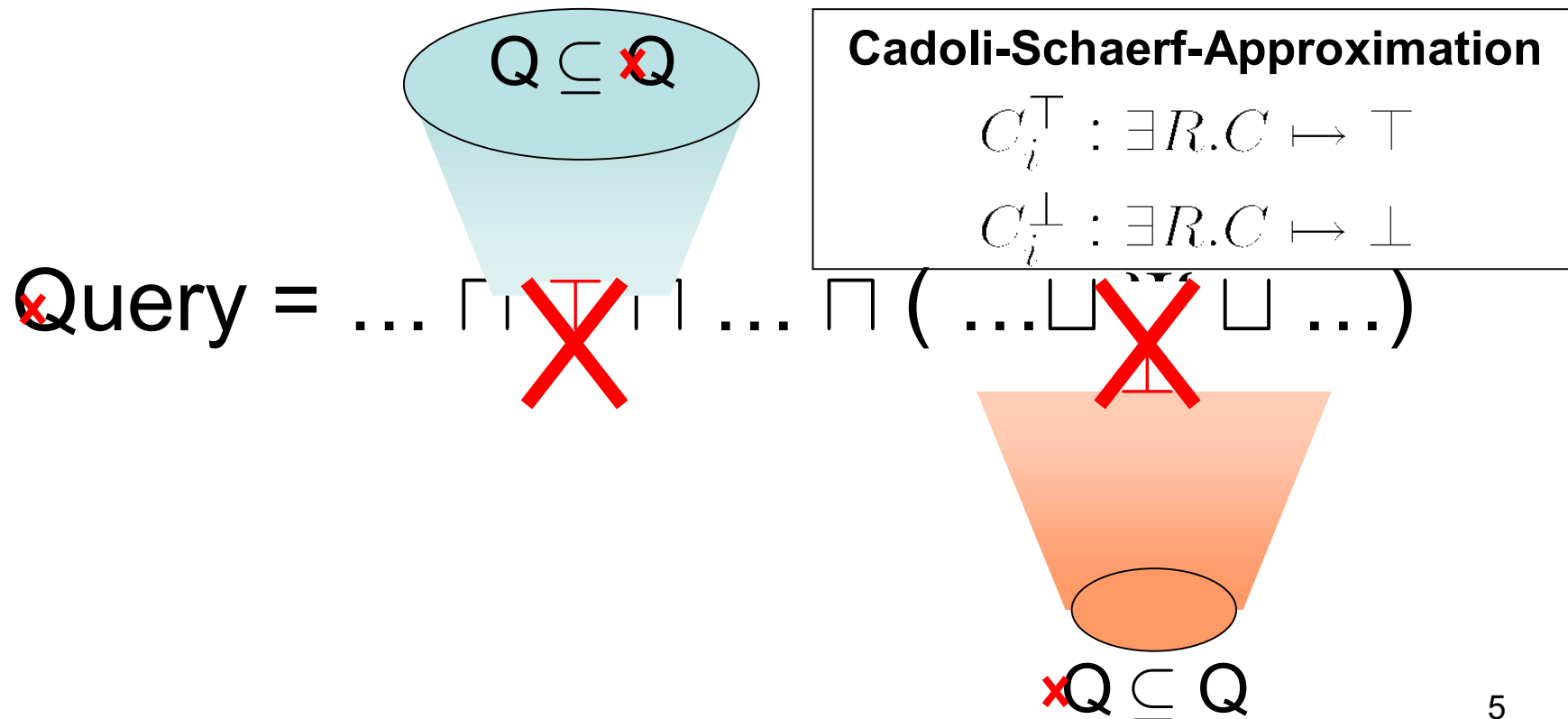
Approximate Deduction through Simplification



- ❑ Simplify query
- ❑ Simple query \Rightarrow fast query answering
- ❑ Simple query \Rightarrow approximated answers
- ❑ Incremental completion of the query
- ❑ Anytime behavior

How to simplify?

Rewrite some parts (e.g. Φ , Ψ)



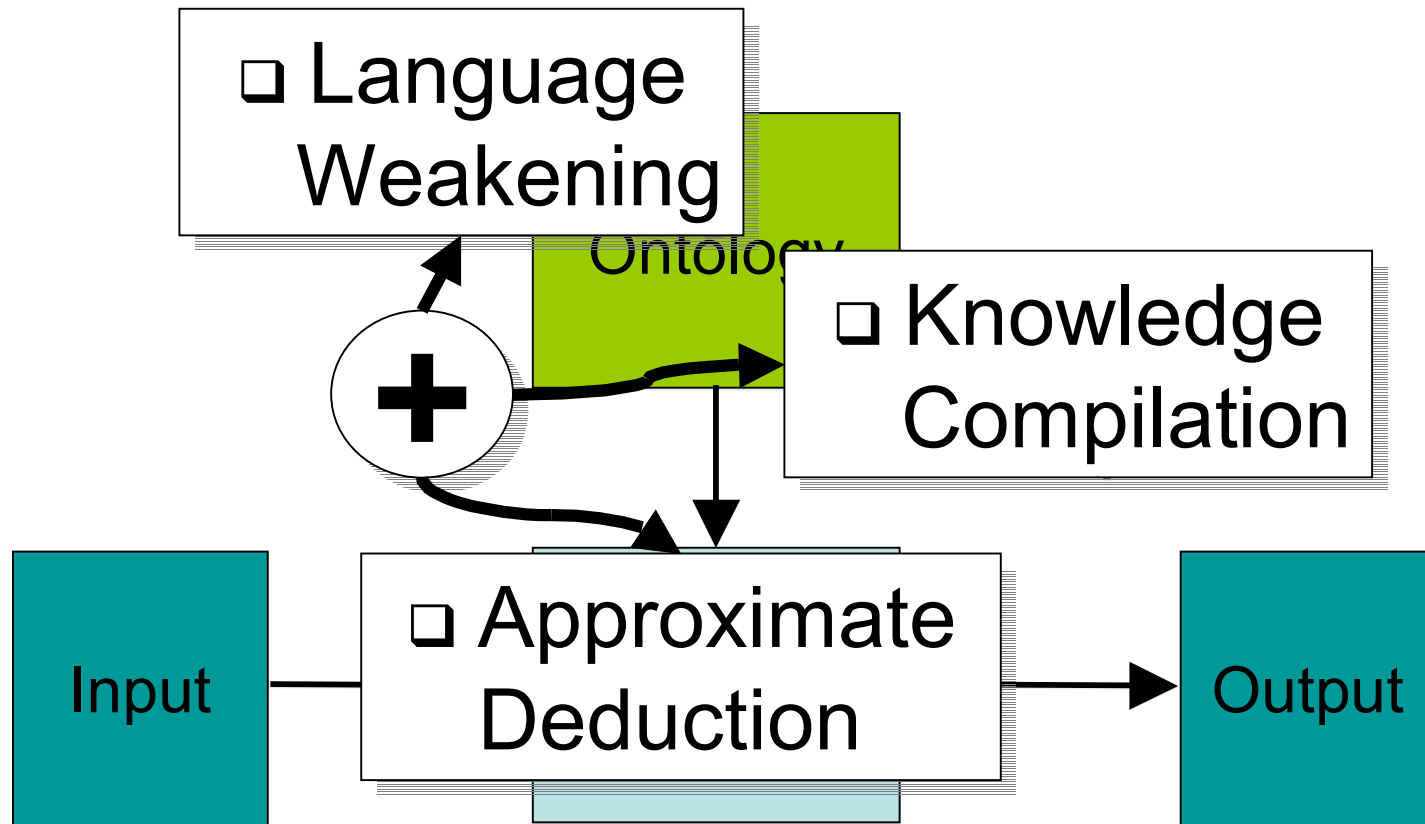
Cadoli-Schaerf- Approximation for DLs

$$\begin{array}{l}
 C_i^{\top} : \exists R.C \mapsto \top \\
 C_i^{\perp} : \exists R.C \mapsto \perp
 \end{array}$$

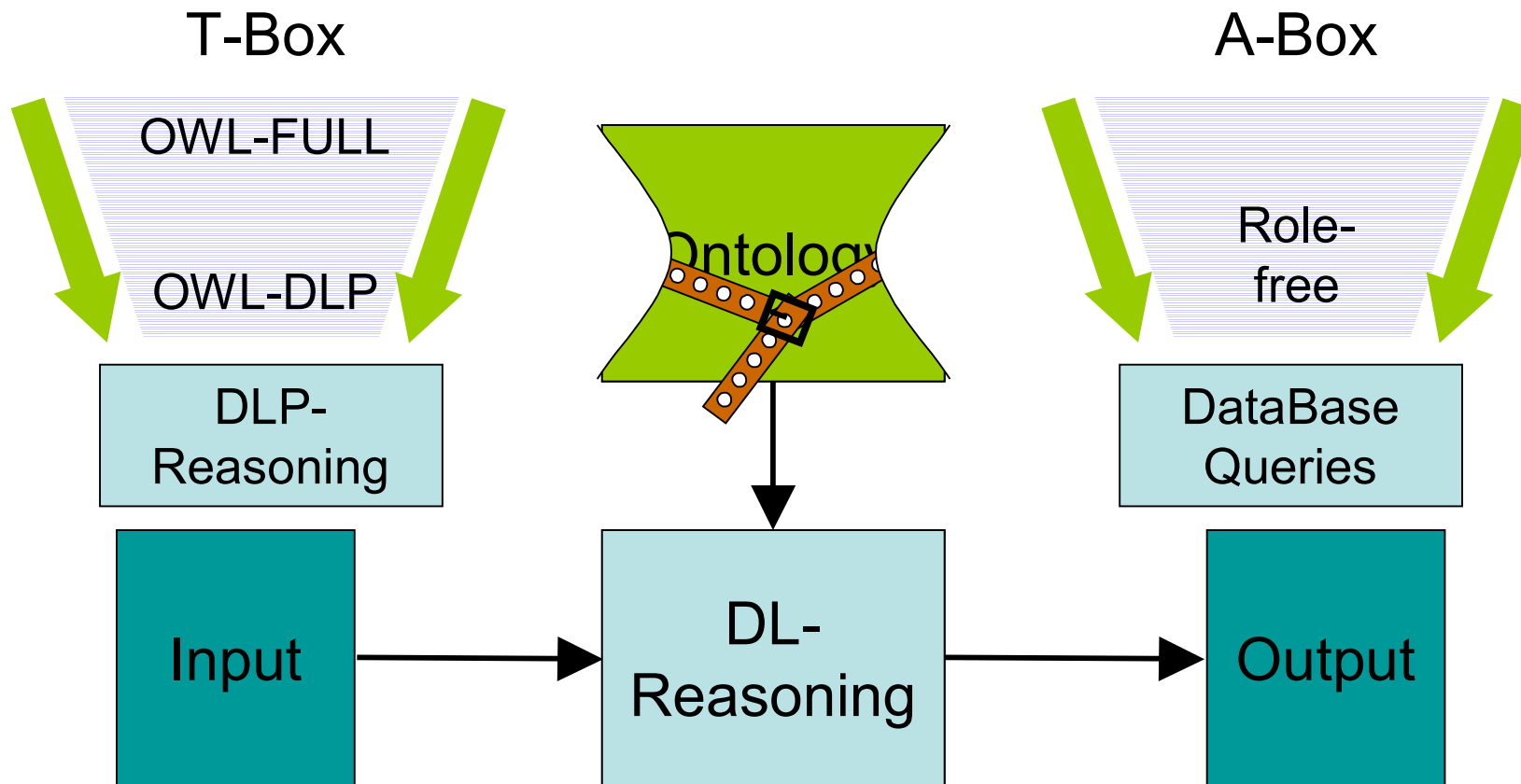
- Depth of subconcept D : number of universal quantifiers that have D in its scope.

$$(\underbrace{\exists \text{friend.tall}}_{\text{Depth: 0}}) \sqcap \forall \text{friend.} (\underbrace{(\forall \text{friend.doctor})}_{\text{Depth: 2}}) \sqcap \underbrace{\exists \text{friend.}\neg \text{doctor}}_{\text{Depth: 1}}$$

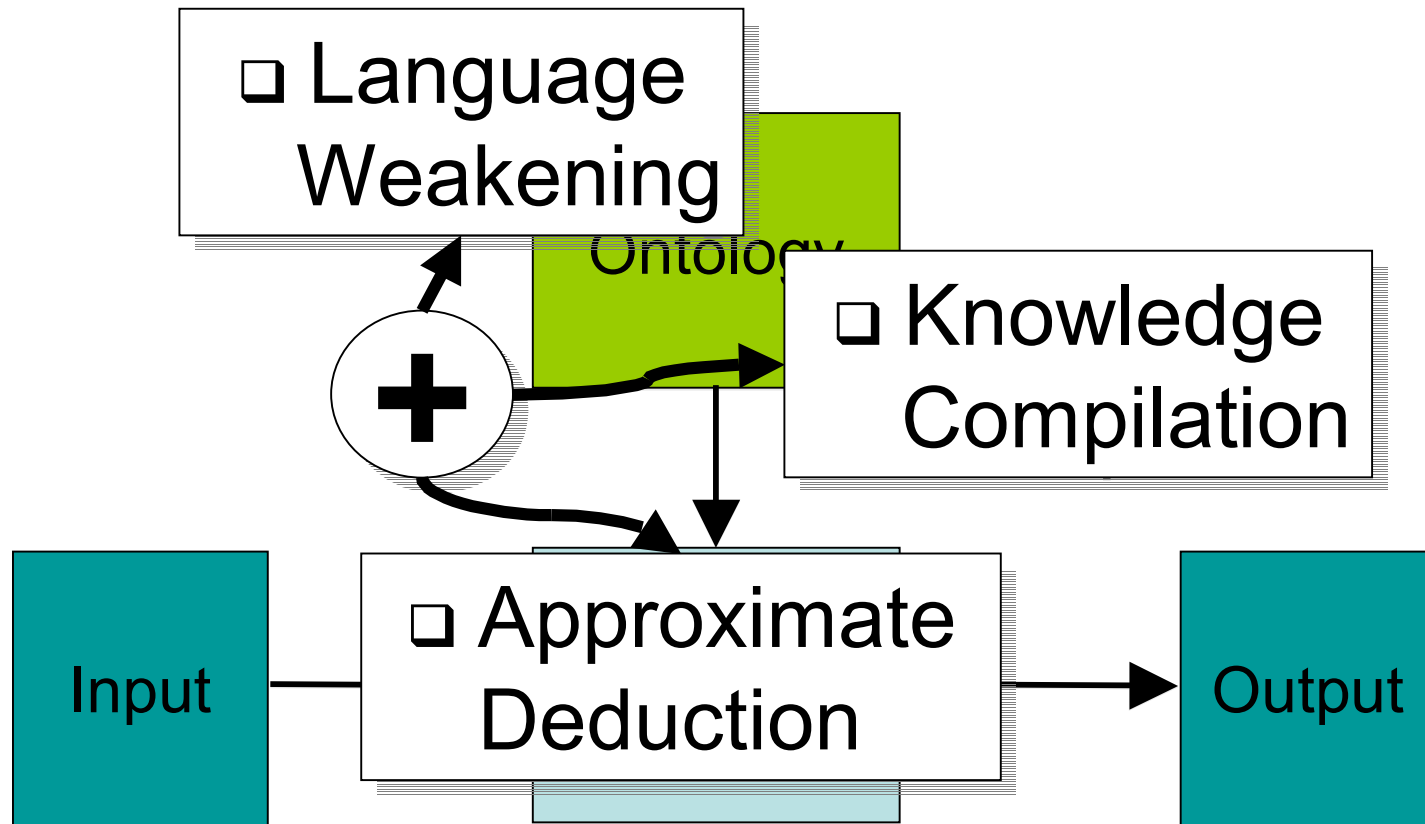
Approximation Approaches



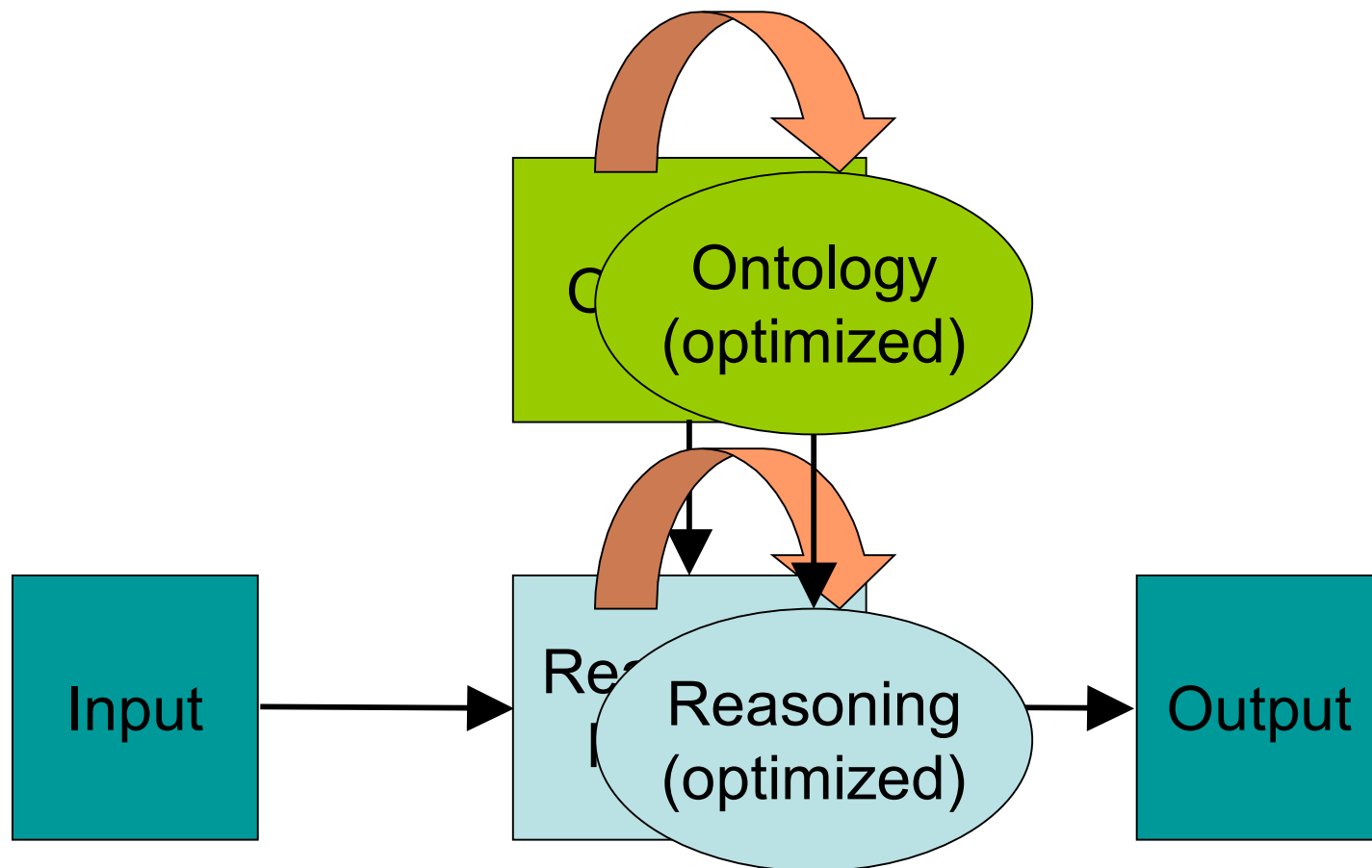
Approximation through Language Weakening



Approximation Approaches

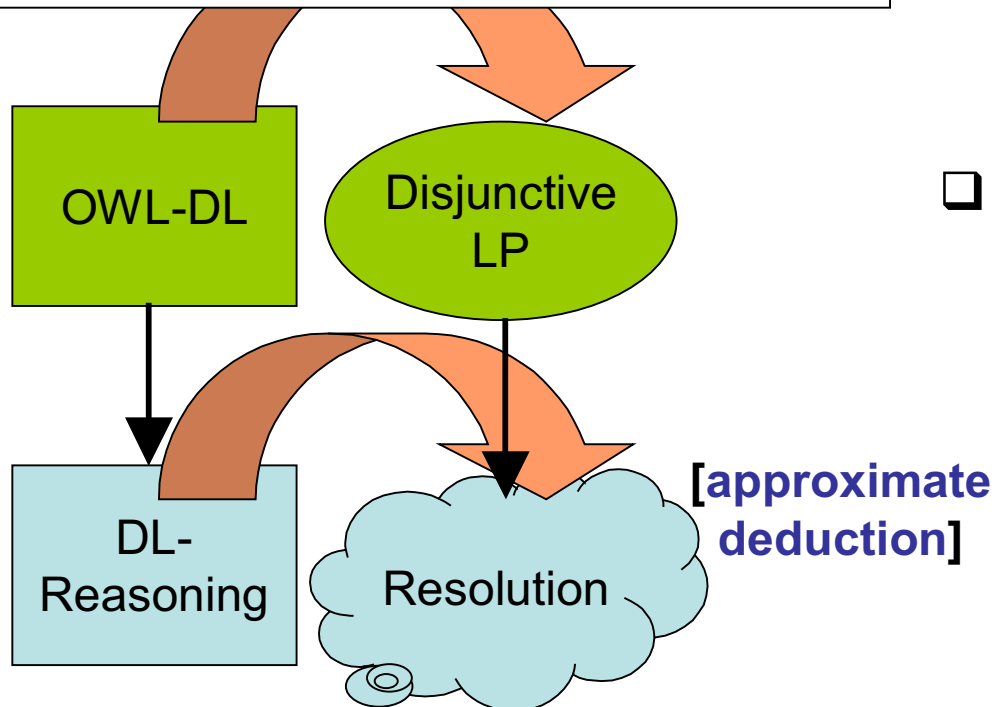


Approximation through Knowledge Compilation



Approximation through Knowledge Compilation

1. Get rid of nominals. [language weakening]
2. Translate into clausal form.
3. Saturate TBox+RBox by taking all consequences. [compilation]
4. Eliminate function symbols.



□ Compile

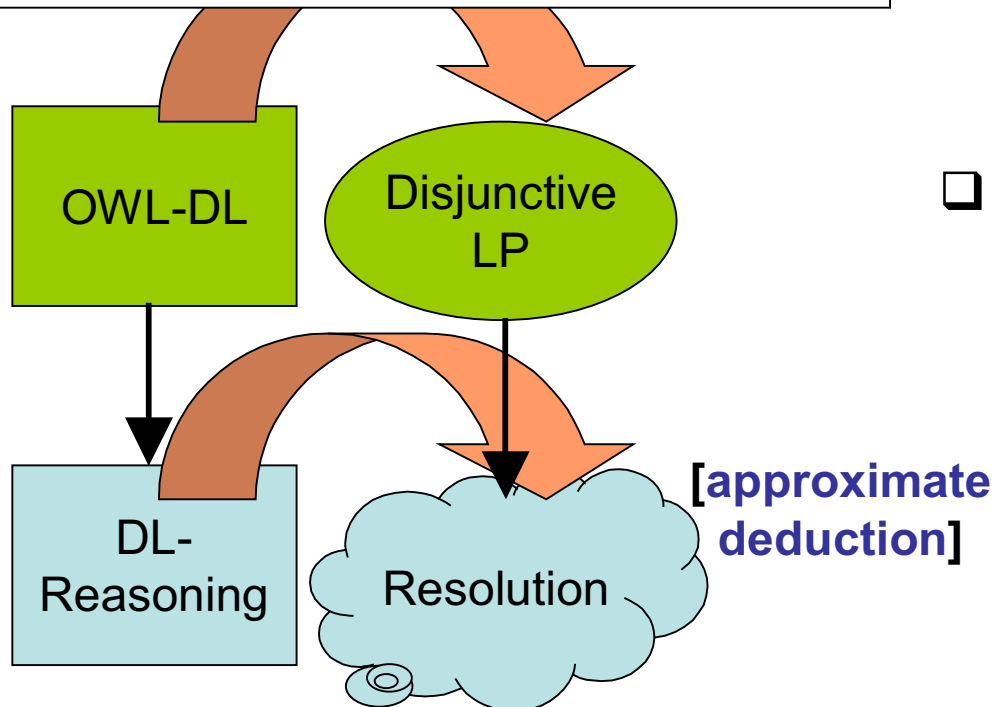
- OWL-DL \Rightarrow Disjunctive LP
- Complete but incorrect

□ Deduce

- regarding disjunctive heads of rules as conjunctions
- Use SLD resolution

Approximation through Knowledge Compilation

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