# Smooth Receiver Operating Characteristics Curves (smROC)

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### Contribution

We develop an evaluation method which:

- extends the ROC to include membership scores
- allows the visualization of individual scores
- depicts the combined performance of classification, ranking and scoring

Consider what information can be obtained from testing a given learning method.

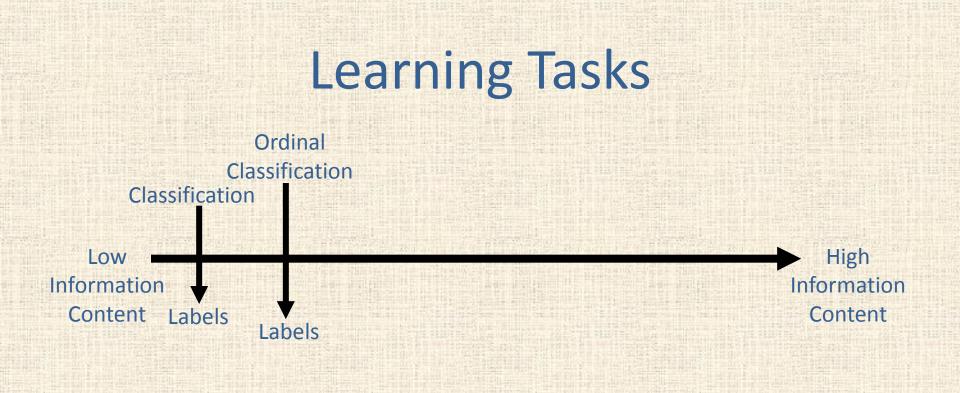
# Learning Tasks

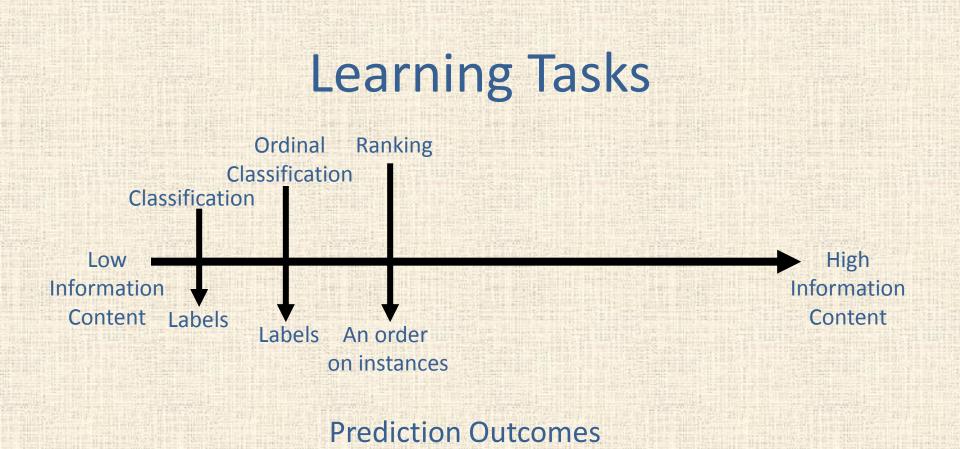
Low Information Content High Information Content

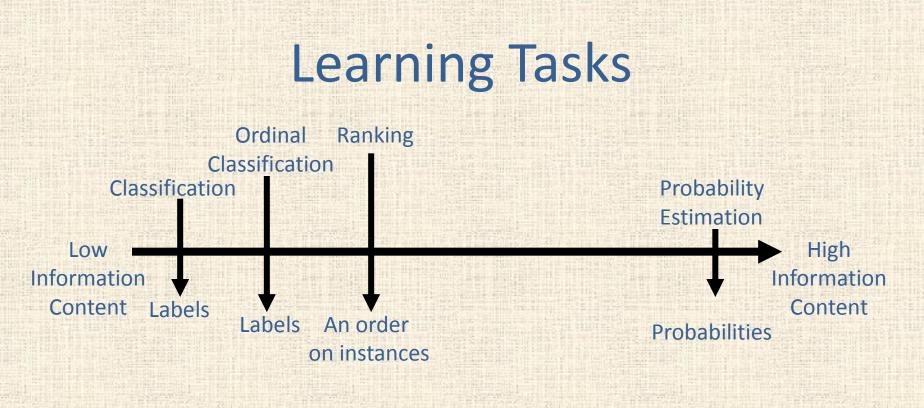
# Learning Tasks

#### Classification

Low Information Content Labels High Information Content







#### Learning Tasks Ordinal Ranking Classification Classification Probability Estimation Scoring low High Information Information Content Content Labels Labels An order **Probabilities** Scores on instances

- Imposing a threshold (on the scores then ignoring them) reduces the task into a classification.
- Sorting the data points (by scores then ignoring them) reduces the task into a ranking.

#### Motivation

- With scores, one can:
  - compare classifications in terms of decisions, ranking, and scores (confidence)
  - visualize the margins of scores
  - find gaps in scores
- Of course, probabilities tell us all this plus more (theoretical), but not all scores are good estimates of probabilities!

### Applications

- Comparing user preferences
- Assessing relevance scores in search engines
- Magnitude-preserving ranking (Cortes et. al ICML'07)
- Research Tool (PET / DT / Naïve Bayes)
- Bioinformatics (gene expression)

#### An Example: Movie Recommendation

#### Anna

ORD RINGS

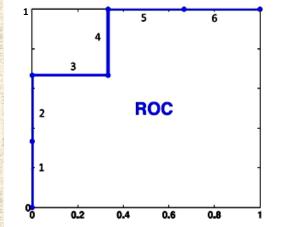




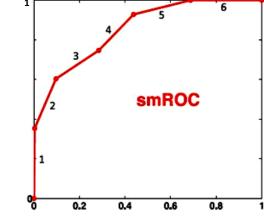






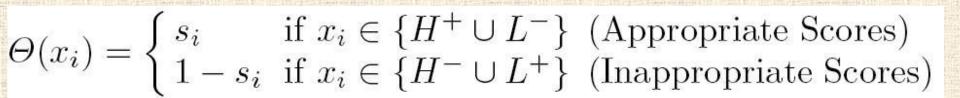


ORD & RINGS



Anna's Assessment									
i	Decision	Score							
1.	+	0.99							
2.	+	0.70							
3.	-	0.60							
4.	+	0.51							
5.	-	0.20							
6.	-	0.00							

### Methodology

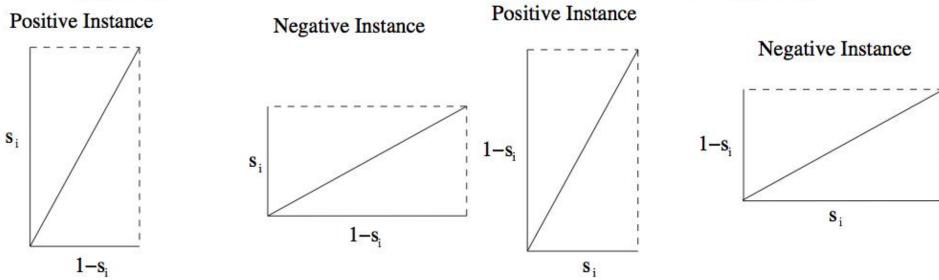


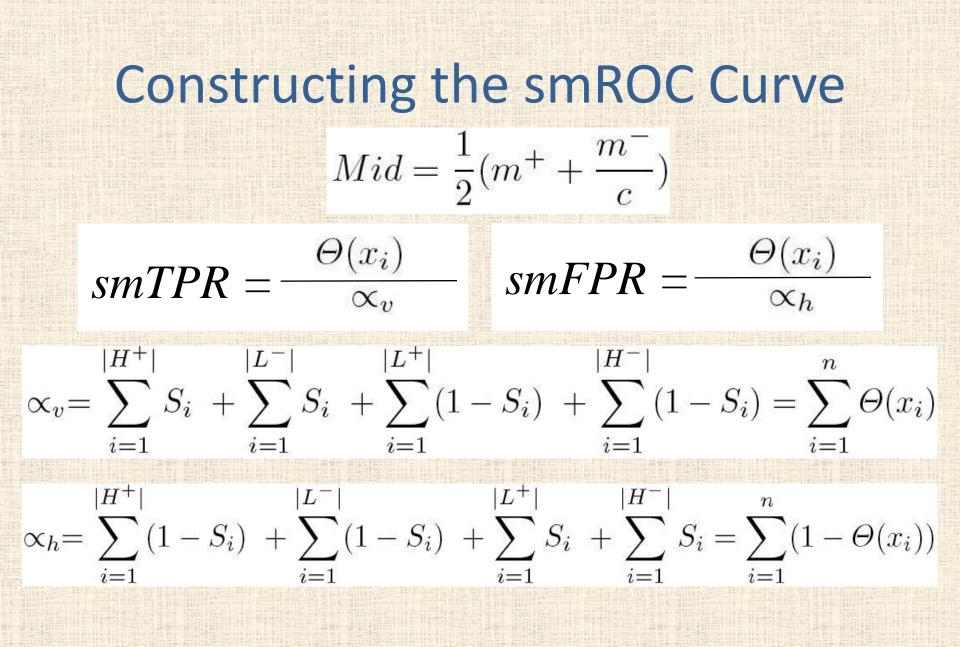
#### **Methodology: Score Appropriateness**

(Appropriateness of Scores)		(Accuracy of Appropriate Scores)			(Accuracy of Inappropriate Scores)					
Scores			Predicted				Predicted			
Label	l High	Low	Score I	Label	Y	N	Score I	Label	Y	N
+	yes	no	High	+	correct	incorrect	High	<u> </u>	incorrect	correct
1. <del></del>	no	yes	Low		incorrect	correct	Low	+	correct	incorrect

Inappropriate

#### Appropriate





# smAUC

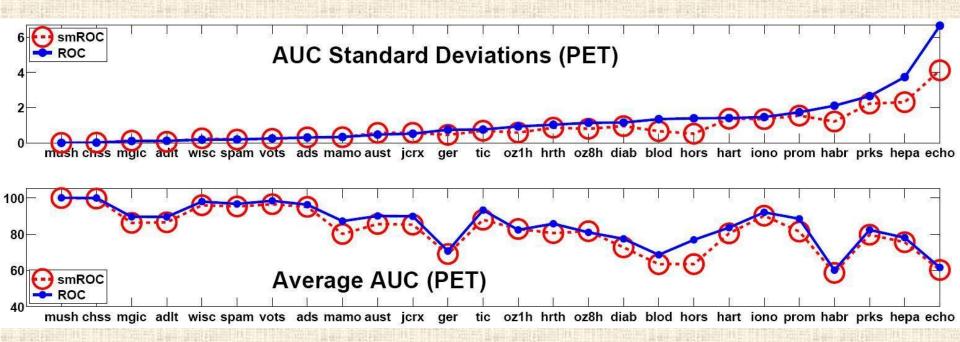
$$smAUC = \frac{1}{\alpha_v \alpha_h} \sum_{i=1}^n \sum_{j=1}^n \Theta(x_i) \Psi(x_i, x_j)$$

$$\Psi(x_i, x_j) = \begin{cases} 1 - \Theta(x_i) & \text{for } (S_i > S_j) \text{ and } (i \neq j) \\ \frac{1}{2}(1 - \Theta(x_i)) & \text{for } i = j \\ 0 & \text{otherwise} \end{cases}$$

### Experiment

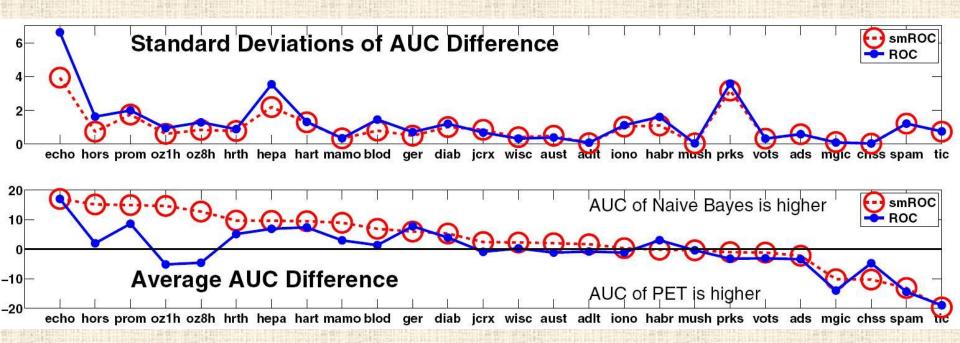
- Use 26 UCI data sets of binary classification problems.
- Classification by PET and Naïve Bayes.
- Test by 10-fold cross-validation repeated 10 times.
- Measure performance similarities among similar models (same learning method on various random splits of the same data).
- Verify well-documented performance differences of PET and NB (different methods on the same data).
- Record the average and standard deviation of smAUC and AUC.

#### **Similar PET Models**



Lower std. dev. for smAUC with increasing variations
smAUC is lower than AUC

### **PET & Naive Bayes Differences**



- smAUC measures a higher difference in favour of Naive Bayes scores.
  AUC = smAUC in favour of PET.
- Lower std. dev. of smAUC difference.

#### **Conclusions & Future Plans**

- smROC is sensitive to scores assigned to data points by the classifier but retains sensitivity to ranking performance.
- smROC is more sensitive to performance similarities and differences between scores.
- For similarities models, smAUC produces lower std. deviations, and for different ones, the difference in the smROC space is higher.
- smROC can be sensitive to changes in the underlying distribution of data and scores (sensitivity to the mid point?).