



# Probably the best itemsets

## *Bayesian approach for ranking itemsets*

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# Problem of Pattern Explosion



- Pattern explosion is the biggest setback in pattern mining.
- Rank/prune the itemsets by comparing the observed support against the expected value.
  - Large difference in supports = interesting pattern.
- An independence model is a popular choice.




# Why this is bad?

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- We discover the same information multiple times.
- Consider a data set with  $K$  items such that
  - $a_1 = a_2$
  - the rest of items are independent.
- Any itemset containing both  $a_1$  and  $a_2$  does not follow independence assumption.
- There will be  $2^{K-2}$  interesting itemsets.
- However, to explain the data we need to know only the frequencies of singletons and  $a_1 a_2$ .

# Pattern set mining



- Recent trend in pattern mining.
  - Score a pattern set as a whole instead of single pattern.
  - By doing so can remove redundancy more efficiently.
  - Statistical approach:
    - Build a statistical model from the current patterns.
    - Fit the model into data,  
model explains data well = current pattern set is good.
    - Pattern set selection = model selection.
  - Use heuristics to find a good collection.
- 



Can we use pattern set measures for scoring individual itemsets?



# Recipe for Scoring Itemsets

- You need
  - a set of statistical models, say  $M_1, \dots, M_K$ ,
  - a function *fam* mapping a model  $M_i$  to some *downward closed* itemset collection,  $F_i = \text{fam}(M_i)$ .
- $p(M_i \mid D)$  is the posterior probability of the *i*th model.
- Score of an itemset  $X$

$$sc(X) = \sum_{X \in F_i} p(M_i \mid D).$$

# Example

- Assume 3 models,

Model	Itemsets	$p(M   D)$
$M_1$	$a, b, c, d, ab, bc, cd$	0.5
$M_2$	$a, b, c, d, ab, ad$	0.3
$M_3$	$a, b, c, d, bc, cd$	0.2

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- The scores for singletons are

$$sc(a) = sc(b) = sc(c) = sc(d) = 1,$$

- The scores for non-singletons are

$$sc(ab) = 0.8, sc(bc) = 0.7, sc(ad) = 0.3, sc(cd) = 0.7.$$



# Scoring Itemsets

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- The score decreases monotonically but...

$$sc(X) = \sum_{X \in F_i} p(M_i | D).$$

# Scoring Itemsets

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- How to compute the probability  $p(M_i | D)$ ?
- How to compute the sum?

# Defining Model



- Use exponential models (a.k.a log-linear or maximum entropy models):
  - The mapping *fam* will be natural.
  - Connections with maximum entropy principle.
  - Connections with MDL theory.
  - Empirical demonstrations for being a good estimate.
- Posterior  $p(M | D)$  can be estimated for a large subset of exponential models.



# Why exponential model is so great

- If  $M$  is the simplest model (smallest  $|fam(M)|$ ) that explains the data, then
  - $sc(X) \rightarrow 1$  if  $X \in fam(M)$ .
  - $sc(X) \rightarrow 0$  if  $X \notin fam(M)$ .



# Computing the sum

- Instead of computing

$$sc(X) = \sum_{X \in F_i} p(M_i | D)$$

sample  $N$  models from  $p(M | D)$  and estimate

$$sc(X) \approx \frac{\text{number of models for which } X \in \text{fam}(M)}{N}.$$

- Use MCMC.

# Some examples

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- Course enrollment data for CS courses in Helsinki.
- 4 most interesting (non-singletons) itemsets
  - *Computer Architectures, Performance Analysis* (0.95)
  - *Design and Analysis of Algorithms, Principles of Functional Programming* (0.94)
  - *Database Systems II, Information Storage* (0.94)
  - *Three concepts: probability, Machine Learning* (0.92)

That's it!

