



Suggesting Friends Using the Implicit Social Graph

SIGKDD 2010

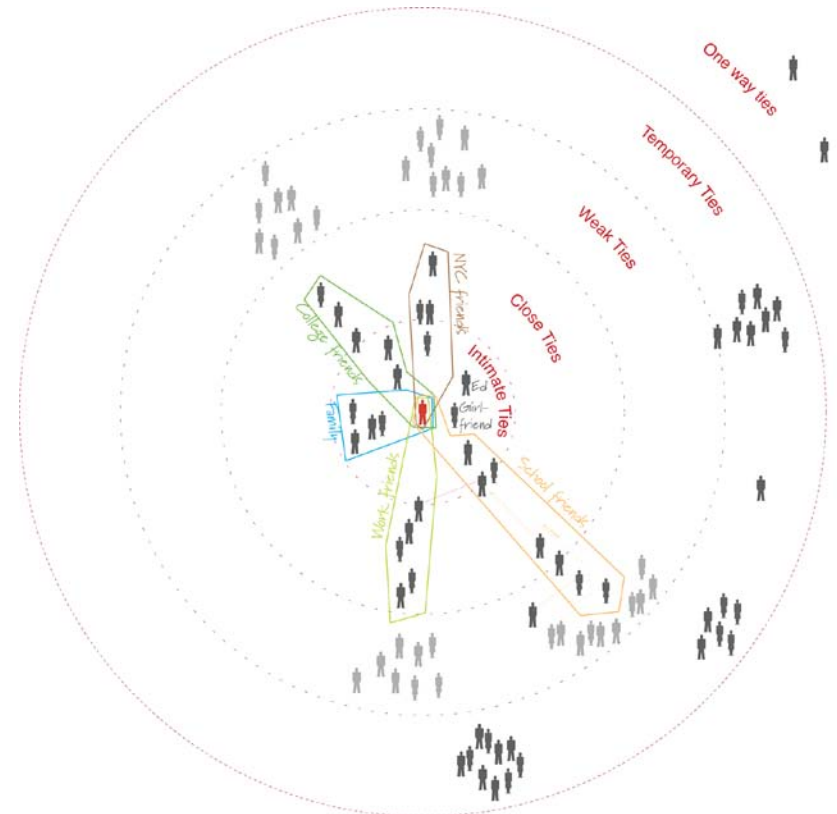
**Maayan Roth, Assaf Ben-David, David Deutscher, Guy Flysher,
Ilan Horn, Ari Leichtberg, Naty Leiser, Yossi Matias, Ron Merom**

Israel R&D Center, Google

Motivation



- People have 3-5 non-intersecting groups in their social networks
- Users interact with groups
 - Send emails, share photos, plan events
- Tools exist to create persistent contact groups... **but** no one uses them
 - Users say creating groups is “tedious”, “time-consuming”
 - Groups change over time

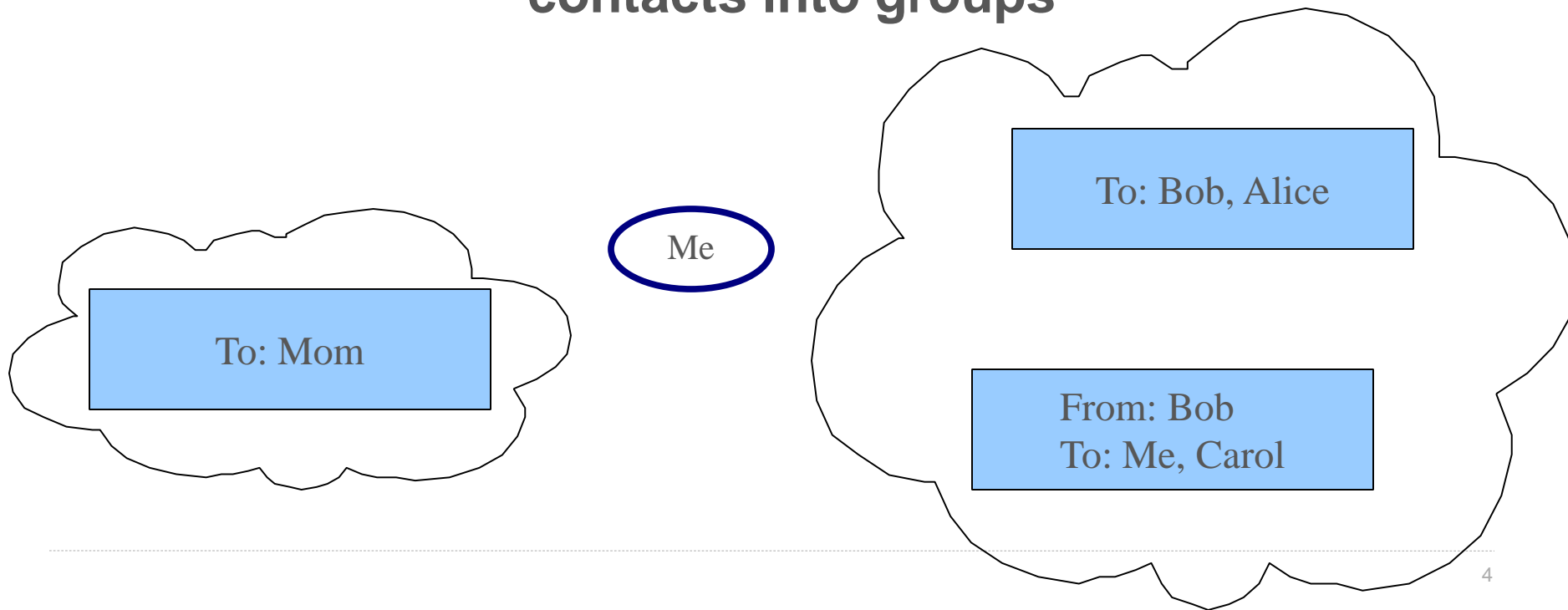


Credit: Paul Adams, Google UX Research

- **Automatically detect users' contact groups** – help users interact with groups, without forcing them to manually categorize their contacts
- Previous approaches
 - Graph clustering on global social graph – users are likely to belong to the same group if they have many friends in common
 - Kuhn and Wirz “Cluestr: Mobile Social Networking for Enhanced Group Communication” (GROUP '09)
 - Content analysis – users are likely to belong to a group if their interactions contain the same keywords
 - Pal and McCallum “CC Prediction with Graphical Models” (CEAS '06)
 - Carvalho and Cohen “Preventing Information Leaks in Email” (SDM '07)

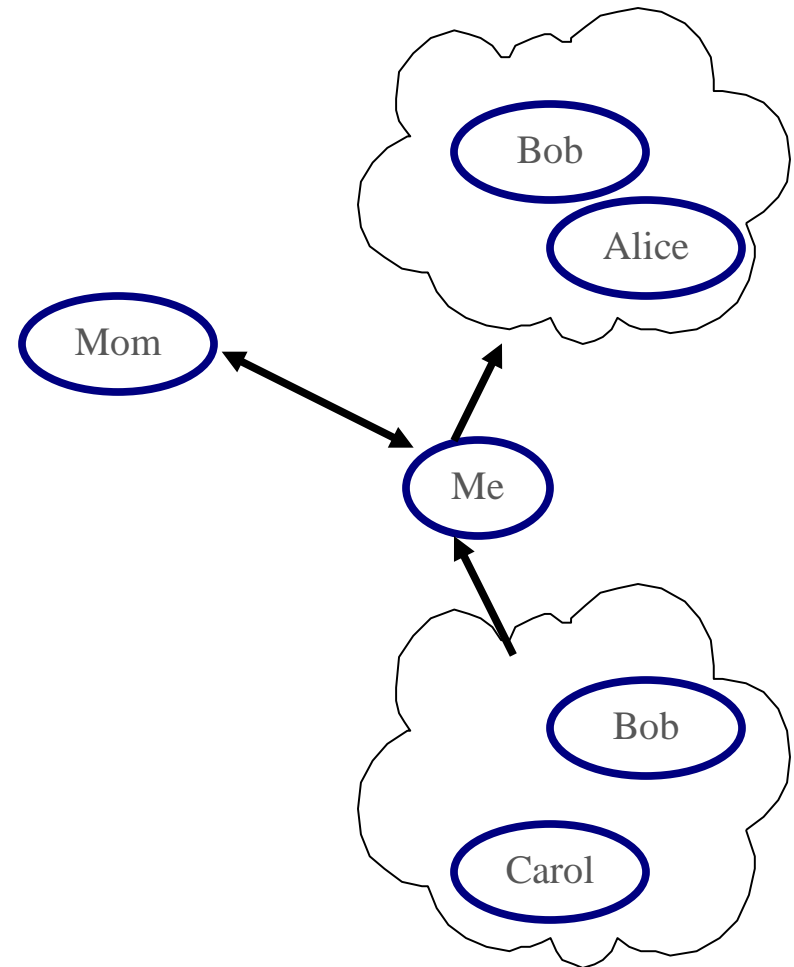
- Email is a group communication medium
- Recipient lists are carefully curated
- Contacts from different groups are unlikely to appear as recipients in the same email

Users' interactions *implicitly* cluster their contacts into groups



Implicit social graph

- Formed by users' interactions with their contacts
- Extracted from email headers
- Weighted, directed hypergraph
- Each email forms a hyper-edge or *implicit group*
- Egocentric
- For each user, analyze the subgraph that contains only his direct interactions
- Addresses privacy concerns



- A user may interact with hundreds of groups, thousands of contacts
 - Identify the contacts and groups that are the most important to the user
- Group importance depends on:
 - Frequency – More interactions means higher importance
 - Recency – Recent interactions more important than those in the past
 - Direction – Interactions initiated by the user indicate higher importance
- Summarize all the interactions a user had with a contact or group into a single score, called ***Interactions Rank***
 - Weighted count of interactions, where each interaction's weight depends on its timestamp and direction

- Given a set of email interactions between a user and a group g :

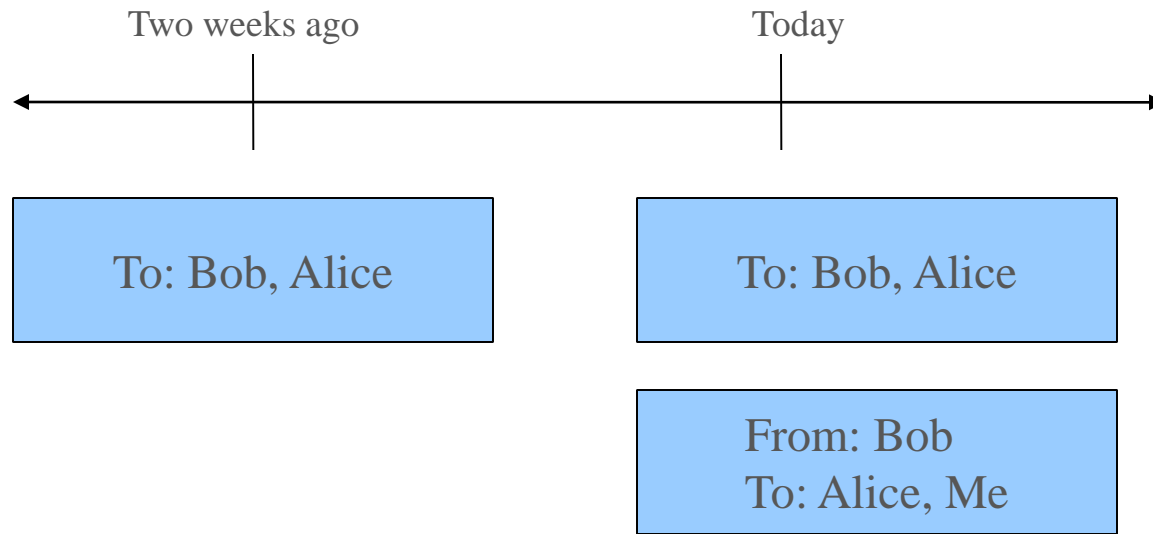
$$I_g = \{I_{outgoing}, I_{incoming}\}$$

- Define Interactions Rank (IR):

$$IR(g) \leftarrow \omega_{out} \sum_{i \in I_{out}} \left(\frac{1}{2}\right)^{\frac{t_{now} - t(i)}{\lambda}} + \sum_{i \in I_{in}} \left(\frac{1}{2}\right)^{\frac{t_{now} - t(i)}{\lambda}}$$

- $t(i)$ – timestamp of interaction i
- λ – halflife, determines speed at which an interaction's importance decays
- ω_{out} – weight that determines relative importance of outgoing interaction vs. incoming interaction

Edge Weights

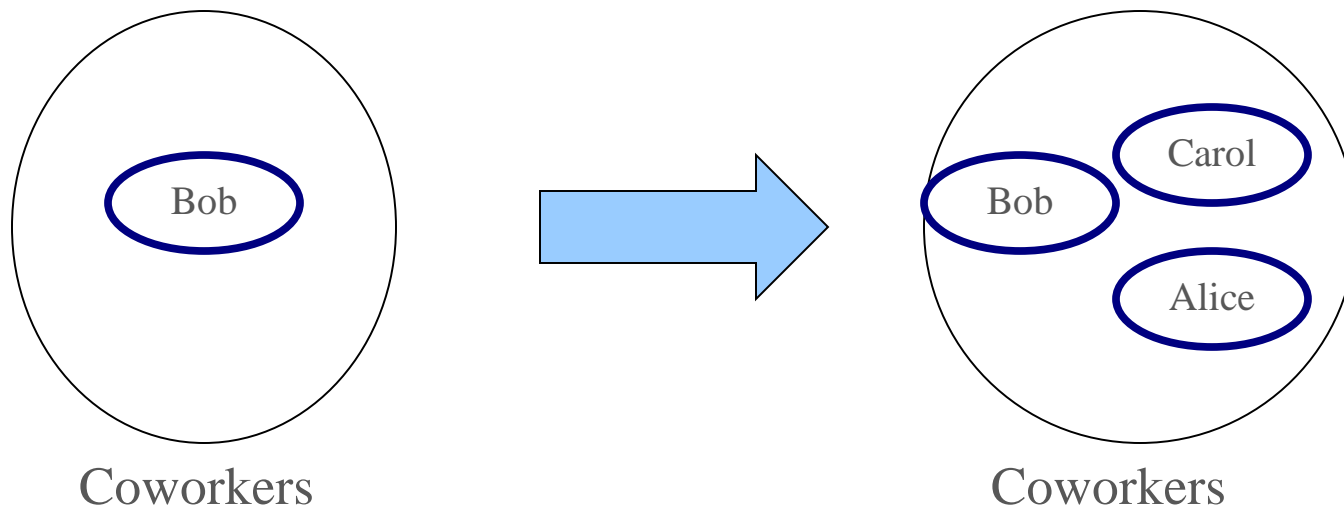


- If $\lambda = 2$ weeks, $\omega_{\text{out}} = 4$:
- Interaction from now has weight 1, then interaction from 2 weeks ago has weight of 0.5
- Outgoing interaction has 4 times the weight of incoming interaction from the same time

$$\text{IR}(\text{Alice}, \text{Bob}) = \omega_{\text{out}}(1 + 0.5) + (1) = 7$$

Finding related contacts

- Given each user's egocentric network, identify groups of related contacts
- Labeling a whole group is time-consuming and tedious... **but** if the user labels a few contacts, maybe we can do the rest
- **Seed group** – A small set of contacts, identified by the user as belonging to a semantically meaningful group



- Given a user u and a seed group S
 - S is a small set of contacts identified by u as belonging to the same group
 - Return F , a set of friend suggestions for contacts that are related to those in S
- $G(u)$ is the set of all groups in u 's egocentric network, with their interactions ranks
- For each group g in G :
 - Iterate over each contact c in the group g
 - Skip contacts that are already in S
 - Compute a suggestion score for the contact c , given g 's similarity to the seed group S , and the interactions rank of the implicit group g
- $F(c)$ stores the sum of c 's suggestion scores over all the implicit groups that c belongs to
- Return the contacts with the highest scores in F

- For each contact c that belongs to a group g , we know:
 - How similar is the group g to the seed group S ?
 - What is the Interactions Rank of g ?
- Measure group similarity by looking at the intersection of the group members
 - g is similar to S if they have contacts in common
 - Similarity increases with intersection size
- We want to know:
 - What is the impact of Interactions Rank on friend suggestion quality?
 - How much does similarity matter?
 - Maybe the user's most important contacts are always good suggestions

- Top Contact
- Considers Interactions Rank, does not consider group similarity

$$w(c) \leftarrow \sum_{g \in \mathcal{G}} \text{IR}(g) \mid c \in g$$

- Intersecting Group Count
- Considers group similarity, does not consider Interactions Rank

$$w(c) \leftarrow \sum_{g \in \mathcal{G}} 1 \mid c \in g, |g \cap s| > 0$$

- Intersecting Group Score
- Takes into account both group similarity and Interactions Rank

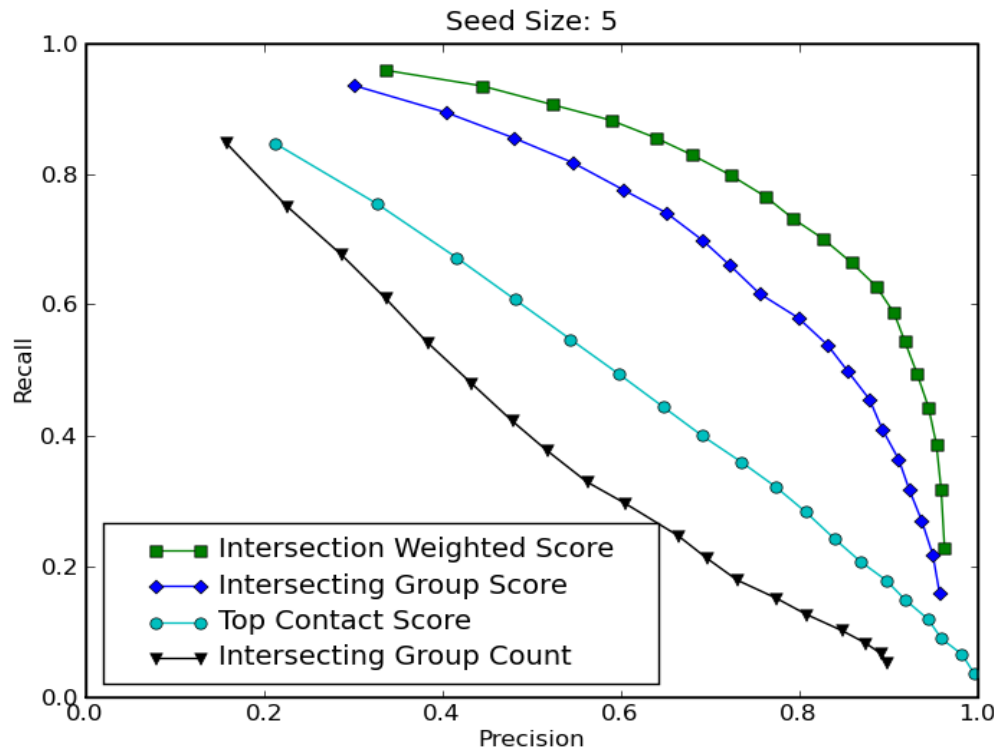
$$w(c) \leftarrow \sum_{g \in \mathcal{G}} \mathcal{IR}(g) \mid c \in g, |g \cap s| > 0$$

- Weighted Intersecting Group Score
- Takes into account amount of group similarity, and Interactions Rank

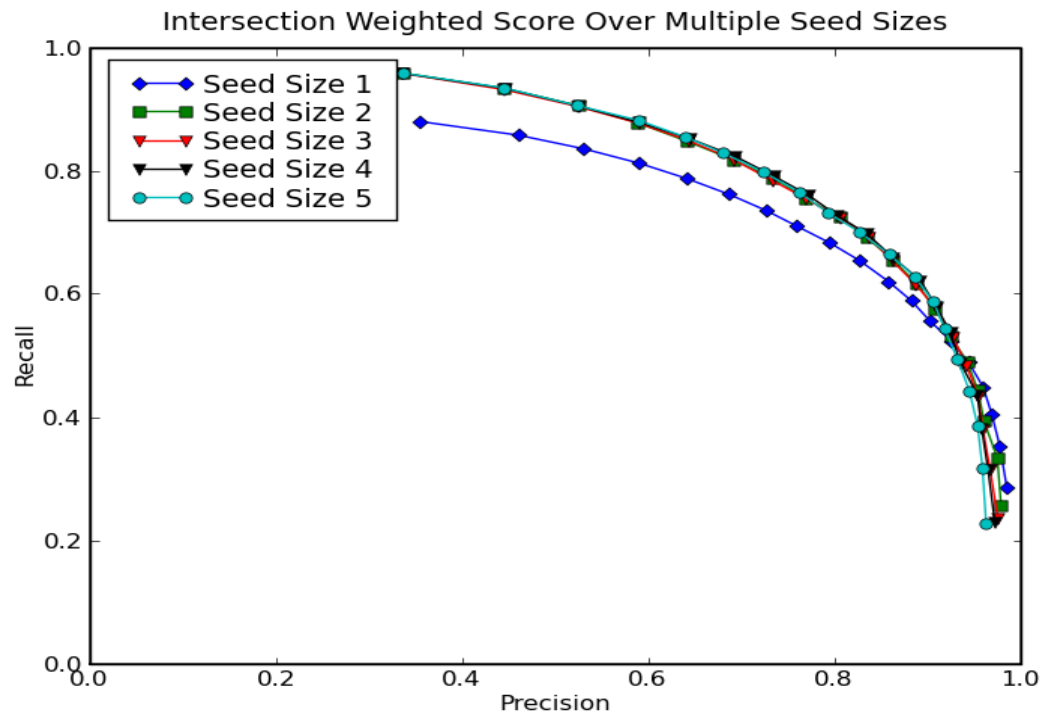
$$w(c) \leftarrow \sum_{g \in \mathcal{G}} \mathcal{IR}(g) \times |g \cap s| \mid c \in g$$

All analysis is done in aggregate. We never look at content. We never look at one person's data.

- Build egocentric networks for all users up to time t
- Randomly sample 100000 new messages with 3-25 recipients, after time $t+1$
- Generate a set of 10000 message headers from emails likely to have been sent by a real person
- For each email:
 - Treat the first k recipients as the seed set
 - Given the seed and the sender's egocentric network, use ExpandSeed to generate seed expansions
 - Measure correctness by ability of algorithm to generate remaining recipients




- Taking into account both group weight (Interactions Rank) and group similarity to seed leads to significantly better performance
- Best performance also takes into account degree of similarity



- For best-performing suggestion score metric, impact of seed size is negligible
- Indicates that groups are well-separated
- Open question for future research

Application - "Don't Forget Bob!"





Send **Save Now** **Discard** Draft autosaved at 6:01 PM (1 minute ago) 

To: "Dopey" <hikingfan@gmail.com>, "Grumpy" <farnsworthpt@gmail.com>, "Doc" <surfingfan@gmail.com>


[Add Cc](#) | [Add Bcc](#) Also include: [Happy](#), [Sneezy](#), [Sleepy](#)

Subject: New in Labs: Suggest more recipients

 [Attach a file](#)  [Add event invitation](#)



Application - "Got the wrong Bob?"



Send **Save Now** **Discard** Draft autosaved at 2:40 PM (0 minutes ago) 

To: "Tim" <hikingfan@gmail.com>, "Angela" <farnsworthpt@gmail.com>, "Bob Jones" <surfingfan@gmail.com>,
[Add Cc](#) | [Add Bcc](#) **Did you mean:** [Bob Smith](#) instead of Bob Jones

Subject: New in Labs: Got the wrong Bob?

 [Attach a file](#)  [Add event invitation](#)

- Given a user u and L , the list of recipients of an email
 - Return a pair of contacts $\{c_i, c_j\}$ such that:
 - c_i is a contact in L that is likely to be a mistake
 - c_j is a suggested replacement for c_i
- For each contact in c_i in L :
 - Create a seed group s by removing c_i from L
 - Generate suggested replacements by running $\text{ExpandSeed}(u, s)$
 - If c_i is in the suggestion set, it is unlikely to be a mistake
 - Else, compare c_i to the contacts in the suggestion set
 - If there is a contact c_j that is similar to c_i , and has a high suggestion score, keep the pair $\{c_i, c_j\}$ as a candidate
- Return the pair $\{c_i, c_j\}$ for which c_j has the highest suggestion score

- Contacts are considered similar if they share a prefix
- Similarity indicates that one of the contacts may have been an autocomplete mistake
- For example, if I send an email to Bob, Alan, and Carol
 - Wrong Bob will suggest “Did you mean to send to Alice instead of Alan?”
 - Alice is a good replacement for Alan because:
 - Alice is a good expansion for the group {Bob, Carol}
 - Alice and Alan share a prefix
- Overall positive user feedback, lots of adoption

- The *implicit social graph* is the graph formed by a user's interactions with his contacts and *implicit groups*
 - Weighted, directed, egocentric hypergraph
 - Weights based on recency, frequency, and direction of interactions
- Expand a user-specified seed of contacts by looking at similarity to implicit group in user's egocentric network
- Seed-expansion algorithm forms the basis for two successful Gmail Labs, “Don't forget Bob!” and “Got the wrong Bob?”


```
function EXPANDSEED( $u$ ,  $\mathcal{S}$ ):  
  input:  $u$ , the user  
            $\mathcal{S}$ , the seed  
  returns:  $\mathcal{F}$ , the friend suggestions  
  
  1.  $\mathcal{G} \leftarrow \text{GETGROUPS}(u)$   
  2.  $\mathcal{F} \leftarrow \emptyset$   
  3. for each group  $g \in \mathcal{G}$ :  
  4.   for each contact  $c \in g$ ,  $c \notin \mathcal{S}$ :  
  5.     if  $c \notin \mathcal{F}$ :  
  6.        $\mathcal{F}[c] \leftarrow 0$   
  7.        $\mathcal{F}[c] \leftarrow \text{UPDATESCORE}(c, \mathcal{S}, g)$ 
```

Application - “Got the wrong Bob?”

function WRONGBOB(u, L):

input: u , the user

L , a list of the recipients of an email

returns: a pair $\{c, s\}$ where

c is a contact $\in L$

s is a suggested contact to replace c

1. $\text{score}_{max} \leftarrow 0$
2. $\text{wrongRecipient} \leftarrow \mathbf{null}$
3. $\text{suggestedContact} \leftarrow \mathbf{null}$
4. **for each** contact $c_i \in L$:
5. $\text{seed} \leftarrow L \setminus c_i$
6. $\text{results} \leftarrow \text{EXPANDSEED}(u, \text{seed})$
7. **if** $c_i \in \text{results}$:
8. **continue**
9. **for each** contact $c_j \in \text{results}$:
10. **if** $\text{ISSIMILAR}(c_i, c_j)$ **and** $\text{score}(c_j) > \text{score}_{max}$:
11. $\text{score}_{max} \leftarrow \text{score}(c_j)$
12. $\text{wrongRecipient} \leftarrow c_i$
13. $\text{suggestedContact} \leftarrow c_j$
14. **return** $\{\text{wrongRecipient}, \text{suggestedContact}\}$