

# Combined Distributional and Logical Semantics

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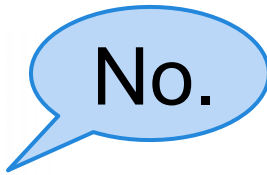
# Semantics



Was Obama born in Kenya?



*Obama's birthplace is not Kenya*



# Distributional Semantics

- Induce the meanings of words from corpora

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- Induce the meanings of words from corpora

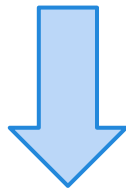
<b>X was born in Y</b>
(Obama, Hawaii)
(Shakespeare, Stratford)
(Obama, 1961)
...

<b>X's birthplace is Y</b>
(Obama, Hawaii)
(Shakespeare, Stratford)
(Jesus, Bethlehem)
...

(e.g. Lin & Pantel, 2001)

# Distributional Semantics

**$\text{sim}(X \text{ was born in } Y, X\text{'s birthplace is } Y) > t$**



*Obama was born in Hawaii*

$\Rightarrow$  *Obama's birthplace is Hawaii*

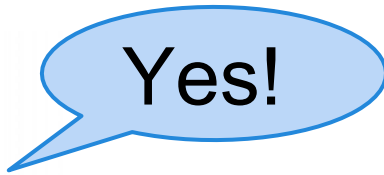
# Distributional Semantics



Was Obama born in Kenya?



*Obama's birthplace is not Kenya*



# Formal Semantics

Obama  
NP

was  
(S\NP)/(S\NP)

born in  
(S\NP)/NP

Hawaii  
NP

---

S\NP

---

S\NP

---

S

# Formal Semantics

Obama  
**NP**  
*obama*

was  
**(S\NP)/(S\NP)**  
 $\lambda p \lambda x . p(x)$

born in  
**(S\NP)/NP**  
 $\lambda y \lambda x . \text{born\_in}'(x, y)$

Hawaii  
**NP**  
*hawaii*

---

**S\NP**

---

**S\NP**

---

**S**



# Formal Semantics

Obama  
**NP**  
*obama*

was  
**(S\NP)/(S\NP)**  
 $\lambda p \lambda x . p(x)$

born in  
**(S\NP)/NP**  
 $\lambda y \lambda x . \text{born\_in}'(x, y)$

Hawaii  
**NP**  
*hawaii*

---

**S\NP**  
 $\lambda x . \text{born\_in}'(x, \text{hawaii})$

---

**S\NP**  
 $\lambda x . \text{born\_in}'(x, \text{hawaii})$

---

**S**  
 $\text{born\_in}'(\text{obama}, \text{hawaii})$

# Formal Semantics

Obama  
**NP**  
*obama*

wasn't  
**(S\NP)/(S\NP)**  
 $\lambda p \lambda x . \neg p(x)$

born in  
**(S\NP)/NP**  
 $\lambda y \lambda x . \text{born\_in}'(x, y)$

Kenya  
**NP**  
*kenya*

---

**S\NP**  
 $\lambda x . \text{born\_in}'(x, \text{kenya})$

---

**S\NP**  
 $\lambda x . \neg \text{born\_in}'(x, \text{kenya})$

---

**S**  
 $\neg \text{born\_in}'(\text{obama}, \text{kenya})$

# Formal Semantics

*Obama wasn't born in Kenya*

⇒

*Obama was born in Kenya*

# Formal Semantics

*Every US president was born in the United States*



*Obama wasn't born in Kenya*

# Formal Semantics

*Nicole Kidman and Barack Obama were born in Hawaii*



*Nicole Kidman was born in Hawaii and Barack Obama was born in Hawaii*

# Formal Semantics



Was Obama born in Kenya?



*Obama's birthplace is not Kenya*



Don't know.

# Formal Semantics

$\neg birthplace'(obama, kenya)$

$\Rightarrow ?$

$born\_in'(obama, kenya)$

# Formal Semantics

- + Models semantic operators ("not", "every", etc.)
- + Abstracts away from syntax (conjunctions, passive voice, relative clauses, etc)
- Doesn't model meaning of content words



# Combining Formal and Distributional Semantics

Existing approaches:

- Compositional vector space models
  - (e.g. Coecke et al., 2011, Baroni et al., 2012, Grefenstette 2013)
- Learn inference rules as logical axioms
  - (e.g. Garrette et al., 2011, Beltagy et al., 2013)

# Combining Formal and Distributional Semantics

***Obama was born in Hawaii***



*born\_in'(obama, hawaii)*

***Hawaii is Obama's birthplace***



*birth\_place'(obama, hawaii)*

# Combining Formal and Distributional Semantics

***Obama was born in Hawaii***



***relation53***(obama, hawaii)

***Hawaii is Obama's birthplace***



***relation53***(obama, hawaii)

# Combining Formal and Distributional Semantics

Learn lexical entries such that:

born             $\vdash$  **(S\NP)/PP[in]** :  $\lambda x \lambda y . \textit{relation53}(x,y)$   
birthplace  $\vdash$  **N/PP[of]**            :  $\lambda x \lambda y . \textit{relation53}(x,y)$

# Formal Semantics

Obama  
**NP**  
*obama*

was  
**(S\NP)/(S\NP)**  
 $\lambda p \lambda x . p(x)$

born in  
**(S\NP)/NP**  
 $\lambda y \lambda x . \text{relation53}(x, y)$

Hawaii  
**NP**  
*hawaii*

---

**S\NP**  
 $\lambda x . \text{relation53}(x, \text{hawaii})$

---

**S\NP**  
 $\lambda x . \text{relation53}(x, \text{hawaii})$

---

**S**  
 $\text{relation53}(\text{obama}, \text{hawaii})$

# Combining Formal and Distributional Semantics

Gather statistics on predicates in large corpus:

<b>born_in'(X, Y)</b>
(Obama, Hawaii)
(Shakespeare, Stratford)
(Obama, 1961)
...

<b>birthplace_of'(X, Y)</b>
(Obama, Hawaii)
(Shakespeare, Stratford)
(Jesus, Bethlehem)
...

# Combining Formal and Distributional Semantics

born\_in'(X, Y)

birth\_place(X,Y)

buy'(X, Y)

purchase'(X, Y)

acquisitionOf'(X, Y)

employeeOf'(X, Y)

workFor'(X, Y)

write'(X, Y)

authorOf'(X,Y)

# Combining Formal and Distributional Semantics

born\_in'(X, Y)

birth\_place(X, Y)

buy'(X, Y)

purchase'(X, Y)

acquisitionOf'(X, Y)

employeeOf'(X, Y)

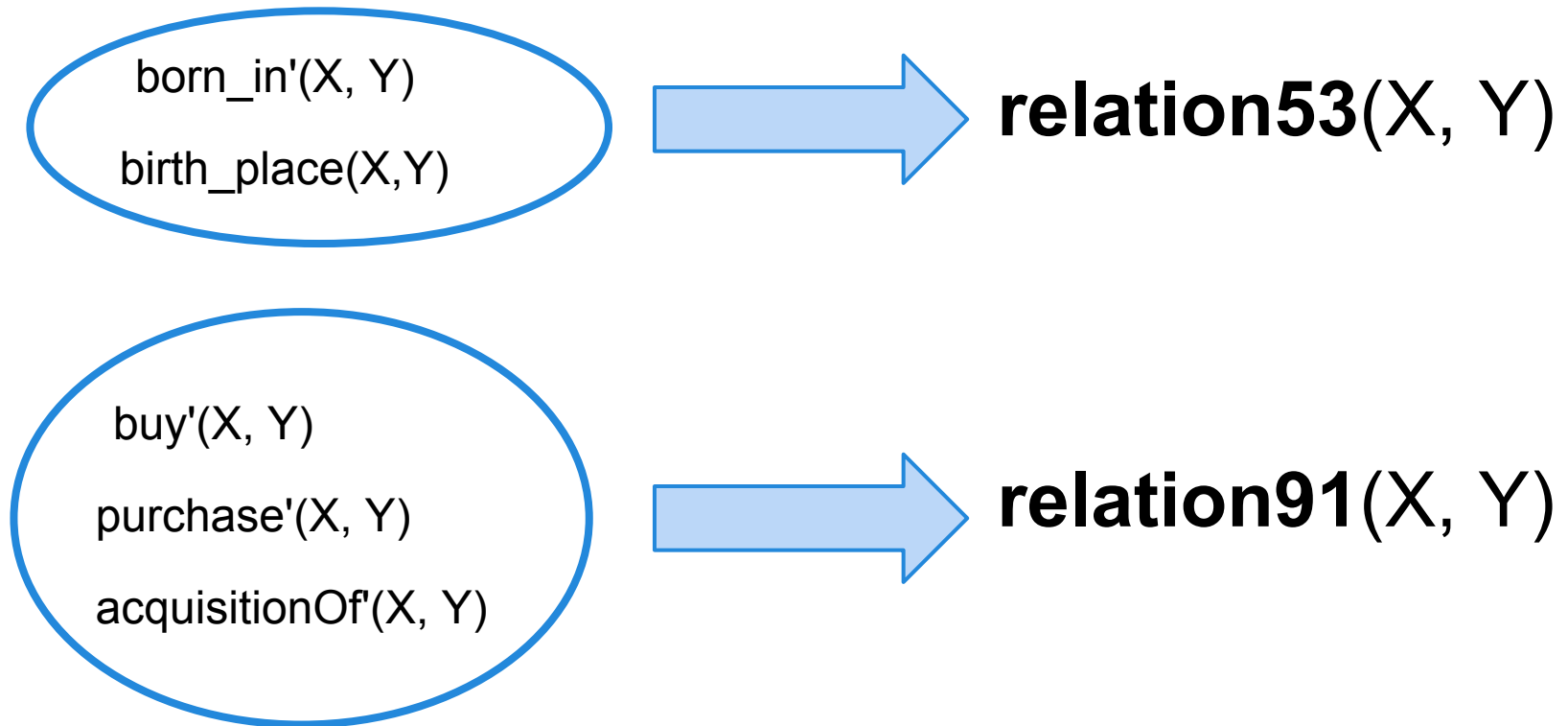
workFor'(X, Y)

write'(X, Y)

authorOf'(X, Y)



# Combining Formal and Distributional Semantics



Cluster using Chinese Whispers (Biemann, 2006)

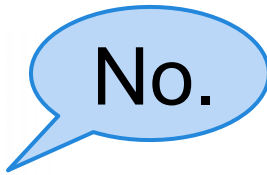
# Combining Formal and Distributional Semantics



Was Obama born in Kenya?



*Obama's birthplace is not Kenya*



# Ambiguity

*Obama was born in Hawaii*

*Obama was born in 1961*

# Ambiguity

*Obama was born in 1961*

⇒

*Obama's birthplace is 1961*

# Ambiguity

*Create multiple typed lexical entries:*

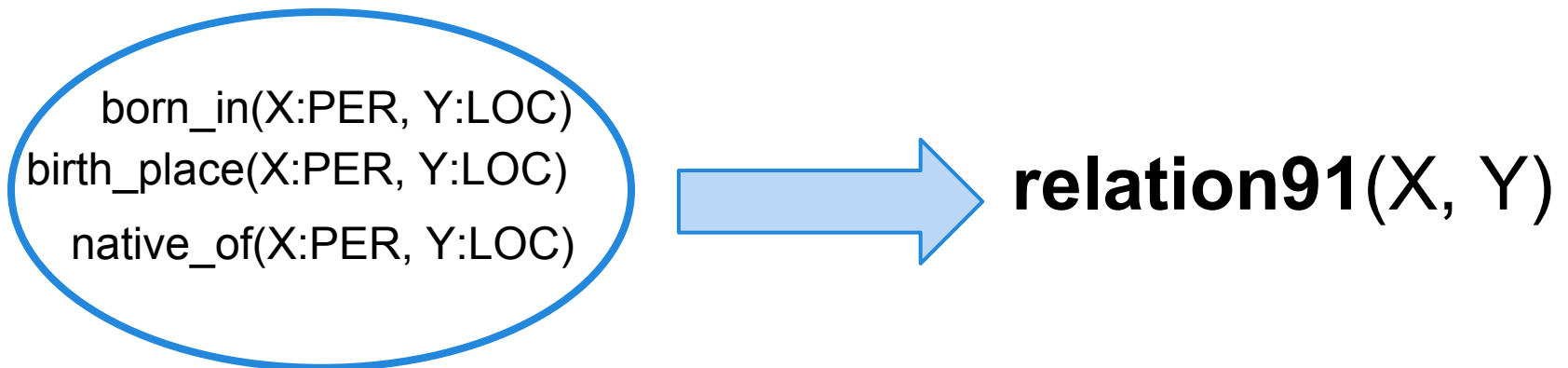
born  $\vdash$  (S\NP)/PP[in] :  $\lambda y_{\text{LOC}} \lambda x_{\text{PER}} . \text{birthPlace}(x,y)$

born  $\vdash$  (S\NP)/PP[in] :  $\lambda y_{\text{DAT}} \lambda x_{\text{PER}} . \text{birthDate}(x,y)$

(similar to: Schoenmackers et al., 2010; Berant et al., 2011)

# Clustering Typed Predicates

Only cluster predicates with the same type



# Topic Model

One 'document' per predicate

One 'word' per argument

<b>lives in X</b>
Hawaii
London
France

<b>year of X</b>
1564
2001
1945

<b>born in X</b>
Hawaii
2001
London
1564

# Topic Model

One 'document' per predicate

One 'word' per argument

<b>lives in X</b>
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<b>year of X</b>
1564
2001
1945

<b>born in X</b>
Hawaii
2001
London
1564

(see also: Melamud et al., 2013)



# Example Types

suspect, assailant, fugitive, accomplice, ...

author, singer, actress, actor, dad, ...

city, area, country, region, town, capital, ...

subsidiary, automaker, airline, Co., GM, ...

musical, thriller, sequel, special, ...

...

# Combining types

born in  
**(S\NP)/NP**

$\lambda y: \left\{ \begin{array}{l} \text{LOC} \sim 0.5 \\ \text{DATE} \sim 0.4 \\ \dots \end{array} \right\} \lambda x: \left\{ \begin{array}{l} \text{PER} \sim 0.9 \\ \text{IDEA} \sim 0.05 \\ \dots \end{array} \right\} \text{born\_in}(x, y)$

2001  
**NP**

$2001: \left\{ \begin{array}{l} \text{DATE} \sim 0.8 \\ \text{FILM} \sim 0.15 \\ \dots \end{array} \right\}$

# Combining types

born in  
**(S\NP)/NP**

2001  
**NP**

$\lambda y: \left\{ \begin{array}{l} \text{LOC} \sim 0.5 \\ \text{DATE} \sim 0.4 \\ \dots \end{array} \right\} \lambda x: \left\{ \begin{array}{l} \text{PER} \sim 0.9 \\ \text{IDEA} \sim 0.05 \\ \dots \end{array} \right\} \text{born\_in}(x, y)$

$2001: \left\{ \begin{array}{l} \text{DATE} \sim 0.8 \\ \text{FILM} \sim 0.15 \\ \dots \end{array} \right\}$

---

**S\NP**

$\lambda x: \left\{ \begin{array}{l} \text{PER} \sim 0.9 \\ \text{IDEA} \sim 0.05 \\ \dots \end{array} \right\}. \text{born\_in}(x, 2001: \left\{ \begin{array}{l} \text{DATE} \sim 0.95 \\ \text{LOC} \sim 0.02 \\ \dots \end{array} \right\})$

# Combining types

born in  
**(S\NP)/NP**

$\lambda y: \left\{ \begin{array}{l} \text{LOC} \sim 0.5 \\ \text{DATE} \sim 0.4 \\ \dots \end{array} \right\} \lambda x: \left\{ \begin{array}{l} \text{PER} \sim 0.9 \\ \text{IDEA} \sim 0.05 \\ \dots \end{array} \right\} \text{born\_in}(x, y)$

Washington  
**NP**

$\text{Wash}: \left\{ \begin{array}{l} \text{LOC} \sim 0.8 \\ \text{PER} \sim 0.15 \\ \dots \end{array} \right\}$

# Combining types

born in  
**(S\NP)/NP**

$\lambda y: \left\{ \begin{array}{l} \text{LOC} \sim 0.5 \\ \text{DATE} \sim 0.4 \\ \dots \end{array} \right\} \lambda x: \left\{ \begin{array}{l} \text{PER} \sim 0.9 \\ \text{IDEA} \sim 0.05 \\ \dots \end{array} \right\} \text{born\_in}(x, y)$

Washington  
**NP**

$\text{Wash}: \left\{ \begin{array}{l} \text{LOC} \sim 0.8 \\ \text{PER} \sim 0.15 \\ \dots \end{array} \right\}$

---

**S\NP**

$\lambda x: \left\{ \begin{array}{l} \text{PER} \sim 0.9 \\ \text{IDEA} \sim 0.05 \\ \dots \end{array} \right\} . \text{born\_in}(x, \text{Wash}: \left\{ \begin{array}{l} \text{LOC} \sim 0.95 \\ \text{PER} \sim 0.01 \\ \dots \end{array} \right\})$

# Compositional Semantics

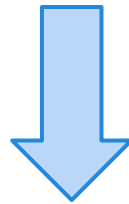
born  $\vdash$  **(S\NP)/PP[in]** :  $\lambda y_{\text{LOC}} \lambda x_{\text{PER}} . \textit{birthPlace}(x,y)$

born  $\vdash$  **(S\NP)/PP[in]** :  $\lambda y_{\text{DAT}} \lambda x_{\text{PER}} . \textit{birthDate}(x,y)$

# Compositional Semantics

born  $\vdash$  **(S\NP)/PP[in]** :  $\lambda y_{\text{LOC}} \lambda x_{\text{PER}} . \text{birthPlace}(x, y)$

born  $\vdash$  **(S\NP)/PP[in]** :  $\lambda y_{\text{DAT}} \lambda x_{\text{PER}} . \text{birthDate}(x, y)$



born  $\vdash$  **(S\NP)/PP[in]**:  $\lambda y \lambda x . \left\{ \begin{array}{l} (x:\text{LOC}, y:\text{PER}) \Rightarrow \text{birthPlace}(x, y) \\ (x:\text{DAT}, y:\text{PER}) \Rightarrow \text{birthDate}(x, y) \end{array} \right\}$

# Compositional Semantics

Output packed logical form capturing joint distribution:

***Obama was born in Hawaii in 1961***

$\left\{ \begin{array}{l} \textit{birthPlace} \sim 0.9 \\ \textit{birthDate} \sim 0.1 \end{array} \right\} (\text{Obama, Hawaii})$

$\wedge \left\{ \begin{array}{l} \textit{birthPlace} \sim 0.1 \\ \textit{birthDate} \sim 0.9 \end{array} \right\} (\text{Obama, 1961})$



# Training Details

- Train on English Gigaword
- Use C&C parser for syntax (Clark and Curran 2004)
- 15 entity types
- Lexicon includes manual entries for some function words ("every", "not", etc.)

# Evaluation

Automatically generate question set from corpus

Google bought YouTube



*Who bought YouTube?*

*What did Google buy?*

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Automatically generate question set from corpus

Google bought YouTube



*Who bought YouTube?*

*What did Google buy?*

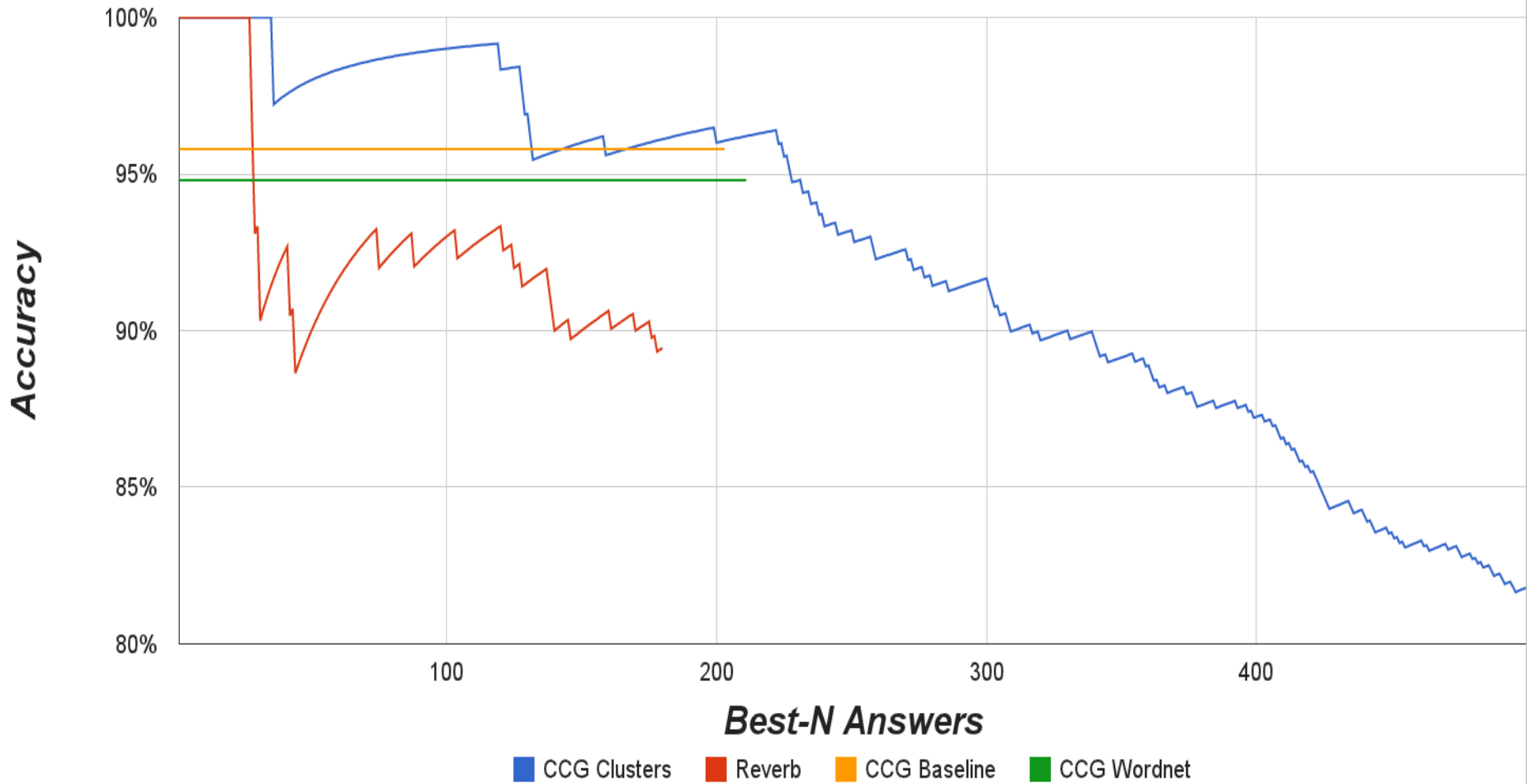
Generate 1000 questions

Manual evaluation

# Comparison Systems

- Reverb (Fader et al., 2011)
- Relational LDA (Yao et al., 2011)
- CCG Baseline
- CCG + WordNet
- **CCG using Distributional Clusters**

# QA Results



# Examples

**Question:** What did Delta merge with?

**Sentence:** The 747 freighters came with Delta's acquisition of Northwest

**Answer:** Northwest

# Evaluating Formal Semantics

Problems involving inference using quantifiers from the FraCaS Suite (Section 1):

***Premises:***

*Every European has the right to live in Europe.*

*Every European is a person.*

*Every person who has the right to live in Europe can travel freely within Europe.*

***Hypothesis:***

*Every European can travel freely within Europe*

# Evaluating Formal Semantics

	<b>Single Premise Sentence</b>	<b>Multiple Premise Sentences</b>
<b>Natural Logic 2007</b>	84%	-
<b>Natural Logic 2008</b>	98%	-
<b>CCG-Dist (parser)</b>	70%	50%
<b>CCG-Dist (gold syntax)</b>	89%	80%



# Conclusions

- Formal and distributional semantics complement each other
- Modelling content words using cluster identifiers gives the benefits of both

# Thanks!

Any questions?