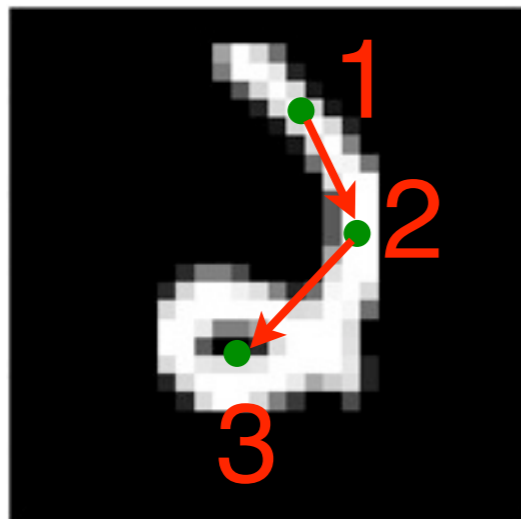


# **Learning to combine foveal glimpses with a third-order Boltzmann machine**

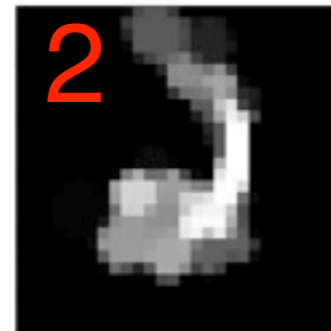
Hugo Larochelle and Geoffrey Hinton  
University of Toronto

# Introduction

- Human vision has the two following characteristics
  - ★ Uses an intelligent “fixation point strategy”
  - ★ Based on a retina with variable spatial resolution

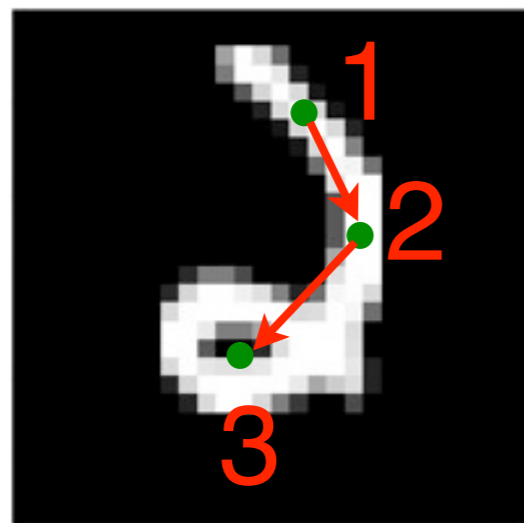


Foveated images

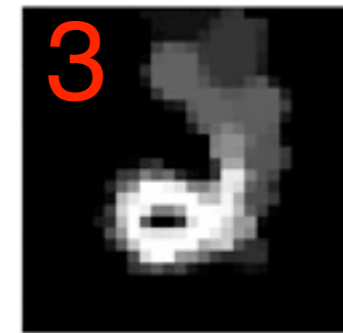
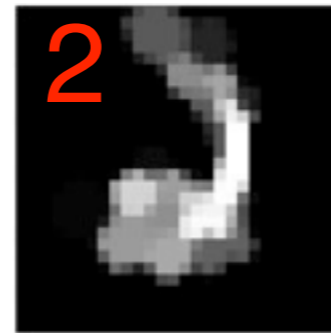


# Introduction

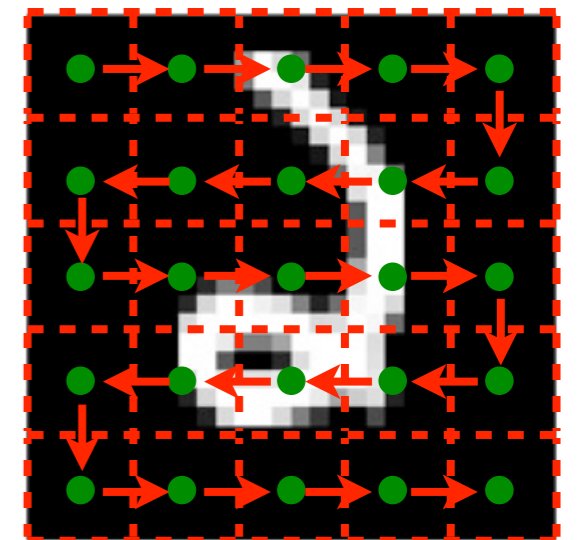
- Human vision has the two following characteristics
  - ★ Uses an intelligent “fixation point strategy”
  - ★ Based on a retina with variable spatial resolution



Foveated images

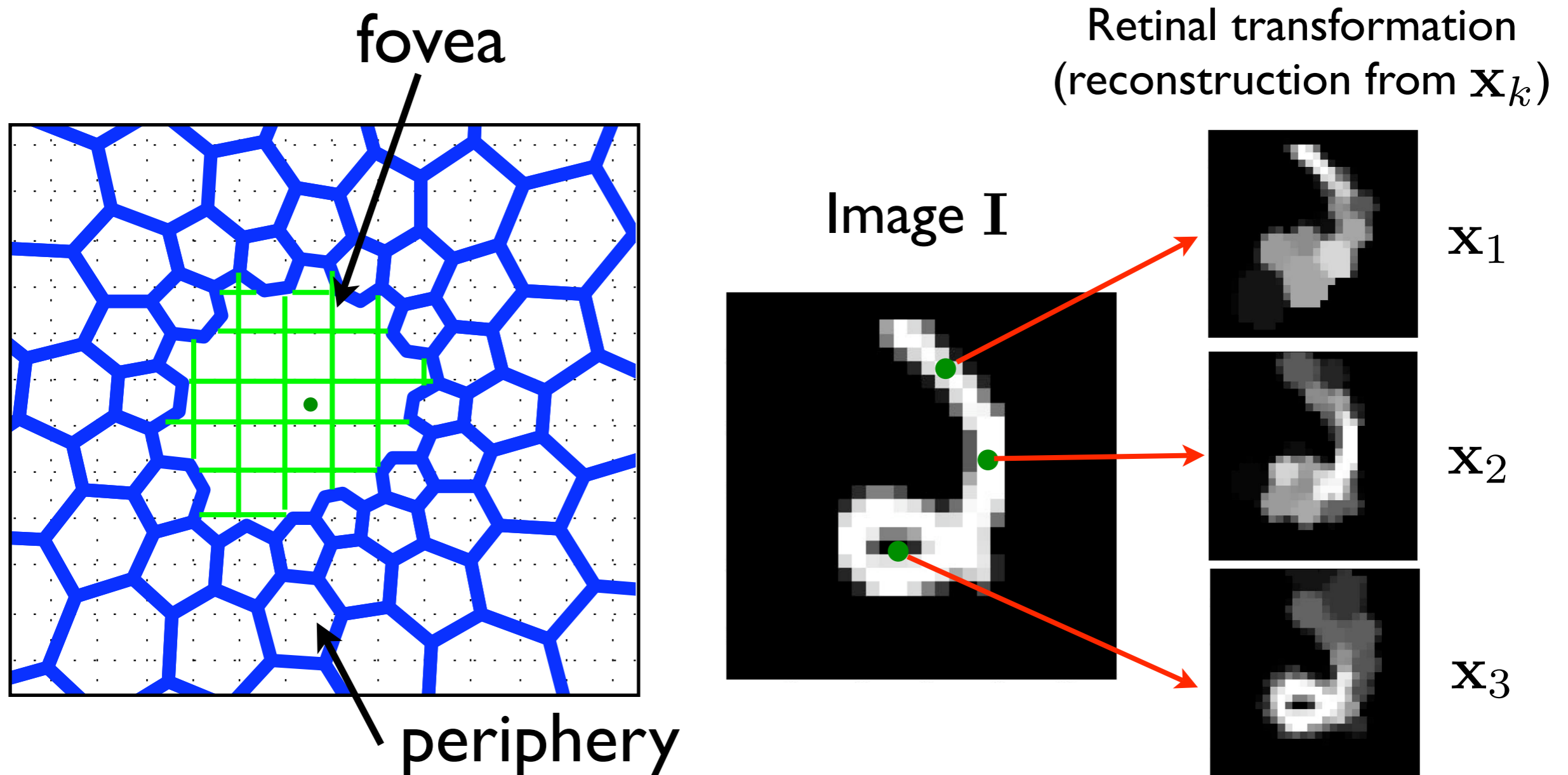


- Many vision systems are instead based on a uniform resolution retina and “fixate everywhere”



# How to look: retinal transformation

- Information from the input image is extracted based on a retinal transformation (“glimpse”)

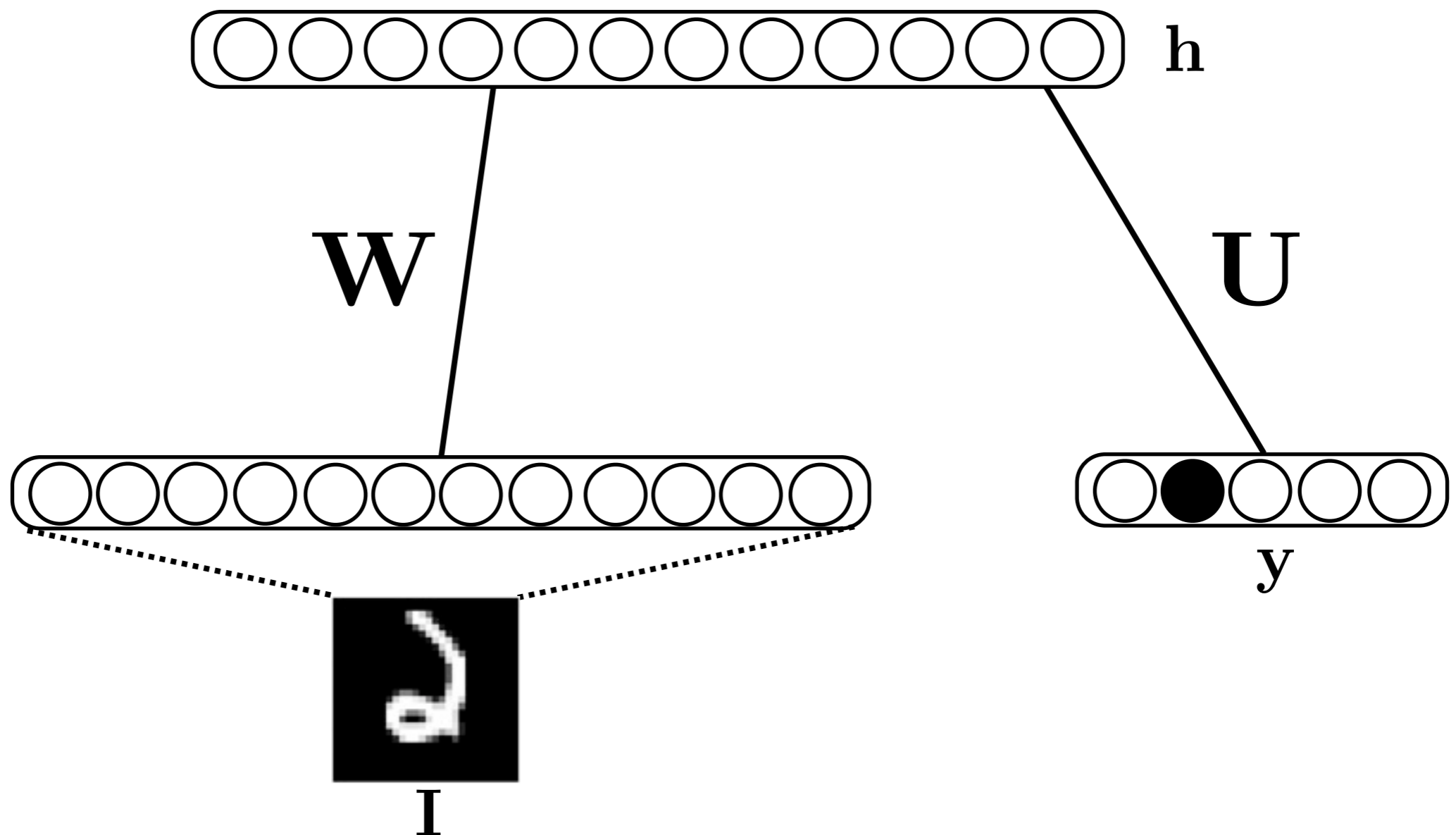


# Components of the system

- **Recognition component (RBM)**
- Attentional component (controller)

# Restricted Boltzmann Machine (RBM)

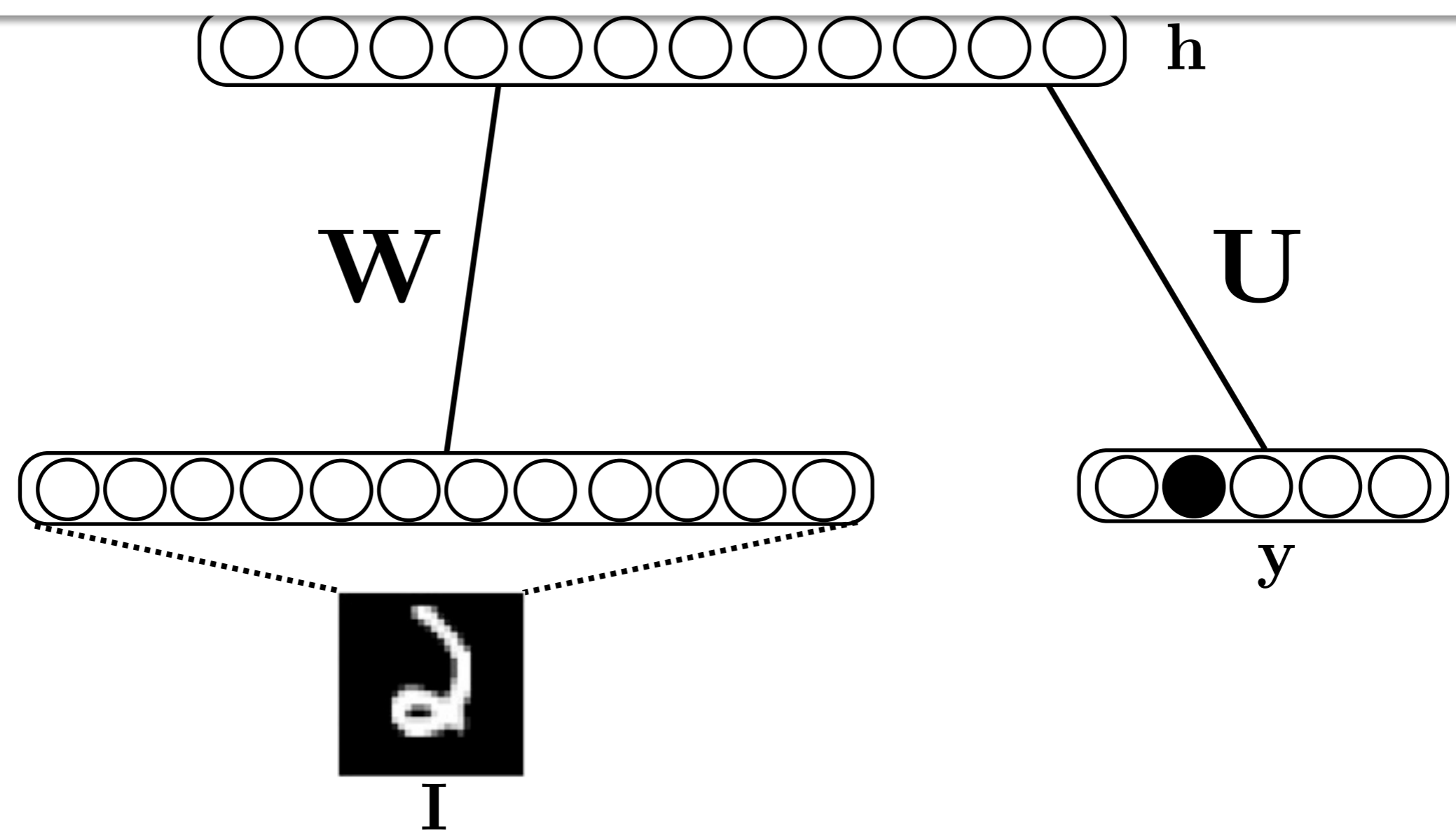
- Classification from the whole image  $\mathbf{I}$



# Key facts

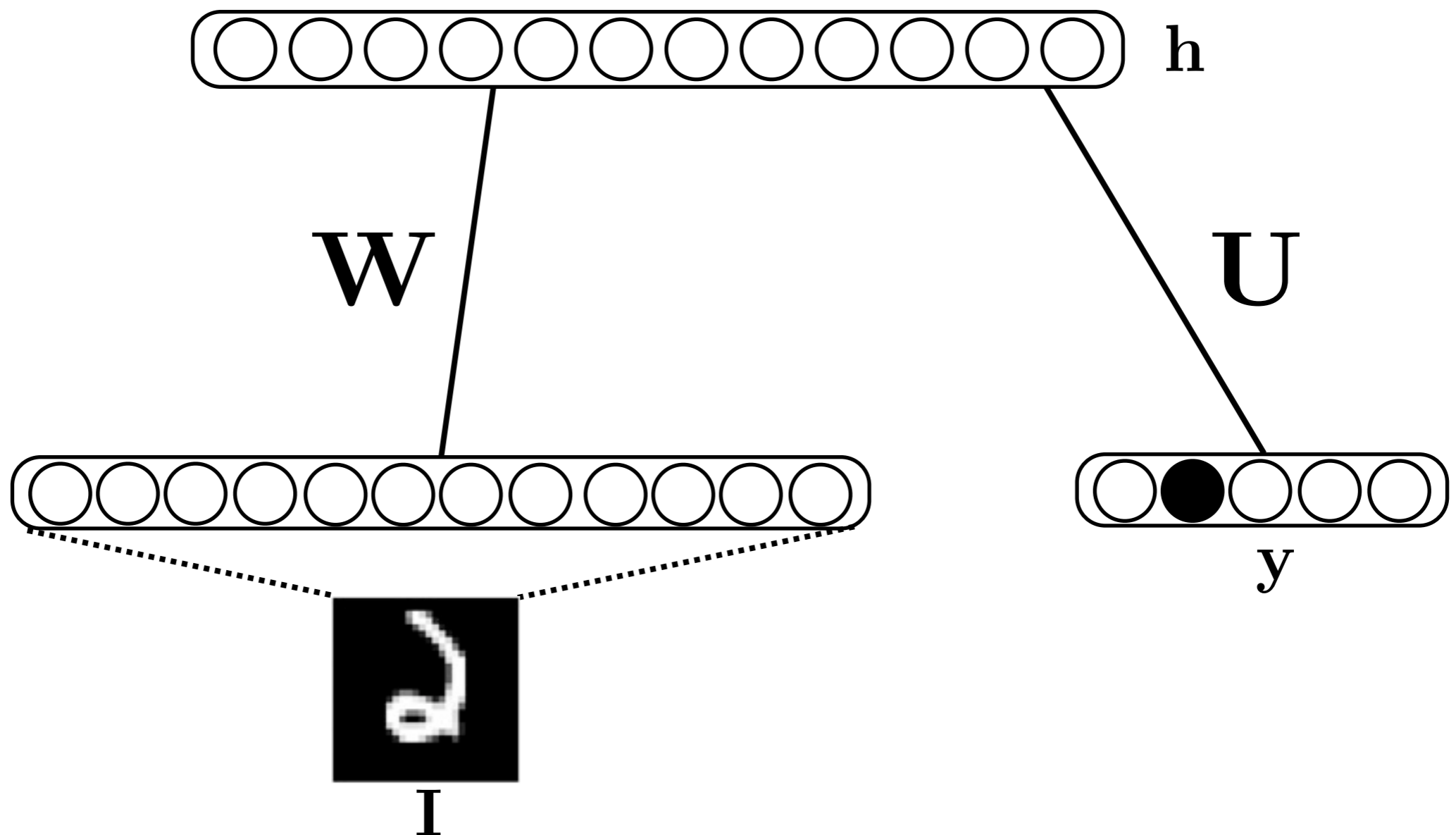
Energy function:  $E(\mathbf{y}, \mathbf{I}, \mathbf{h}) = -\mathbf{h}^\top \mathbf{W} \mathbf{I} - \mathbf{h}^\top \mathbf{U} \mathbf{y}$

Probability:  $p(\mathbf{y}, \mathbf{I}, \mathbf{h}) = \exp(-E(\mathbf{y}, \mathbf{I}, \mathbf{h})) / Z$



# Restricted Boltzmann Machine (RBM)

- Classification from the whole image  $\mathbf{I}$

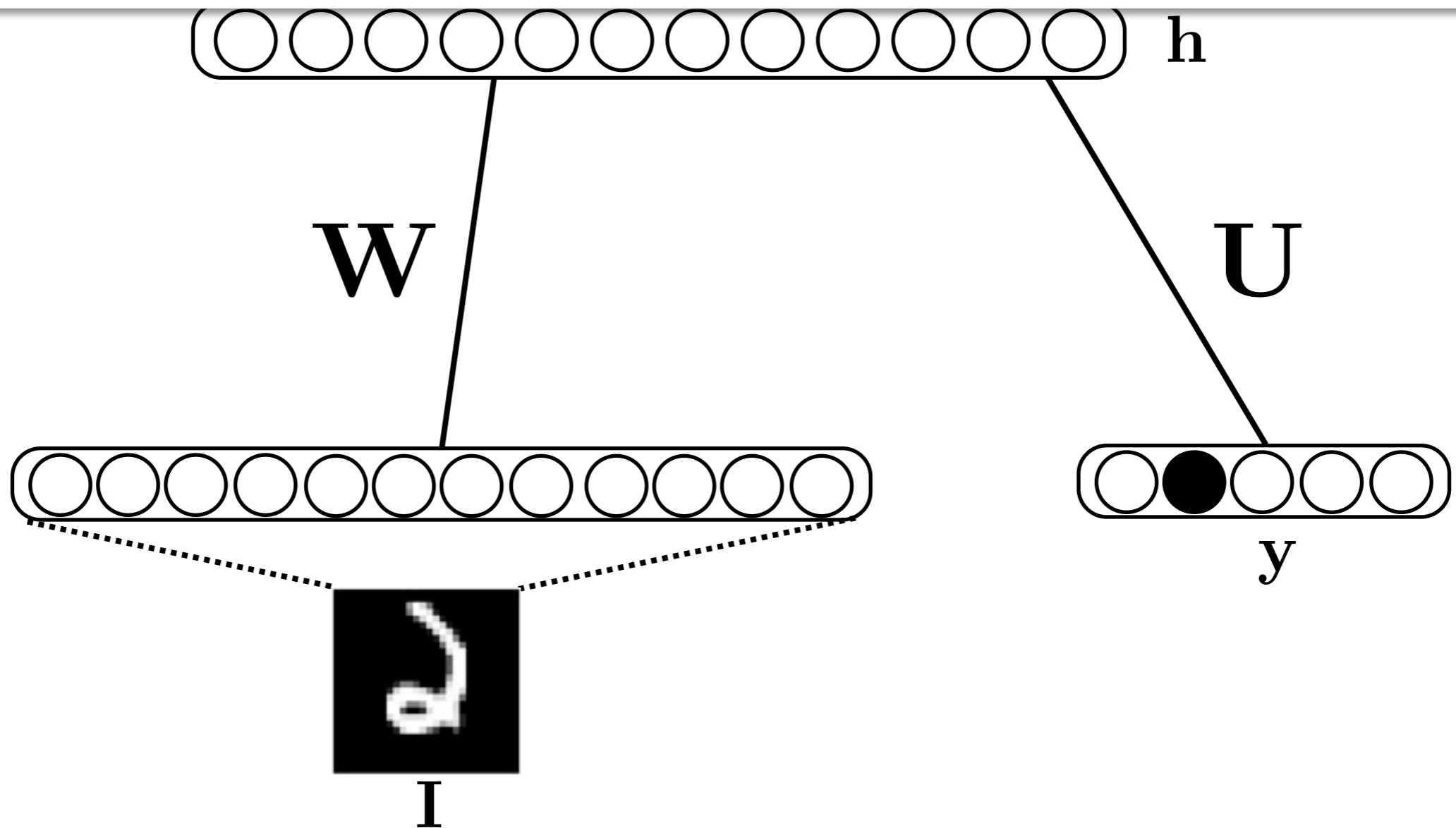




Inference is easy:

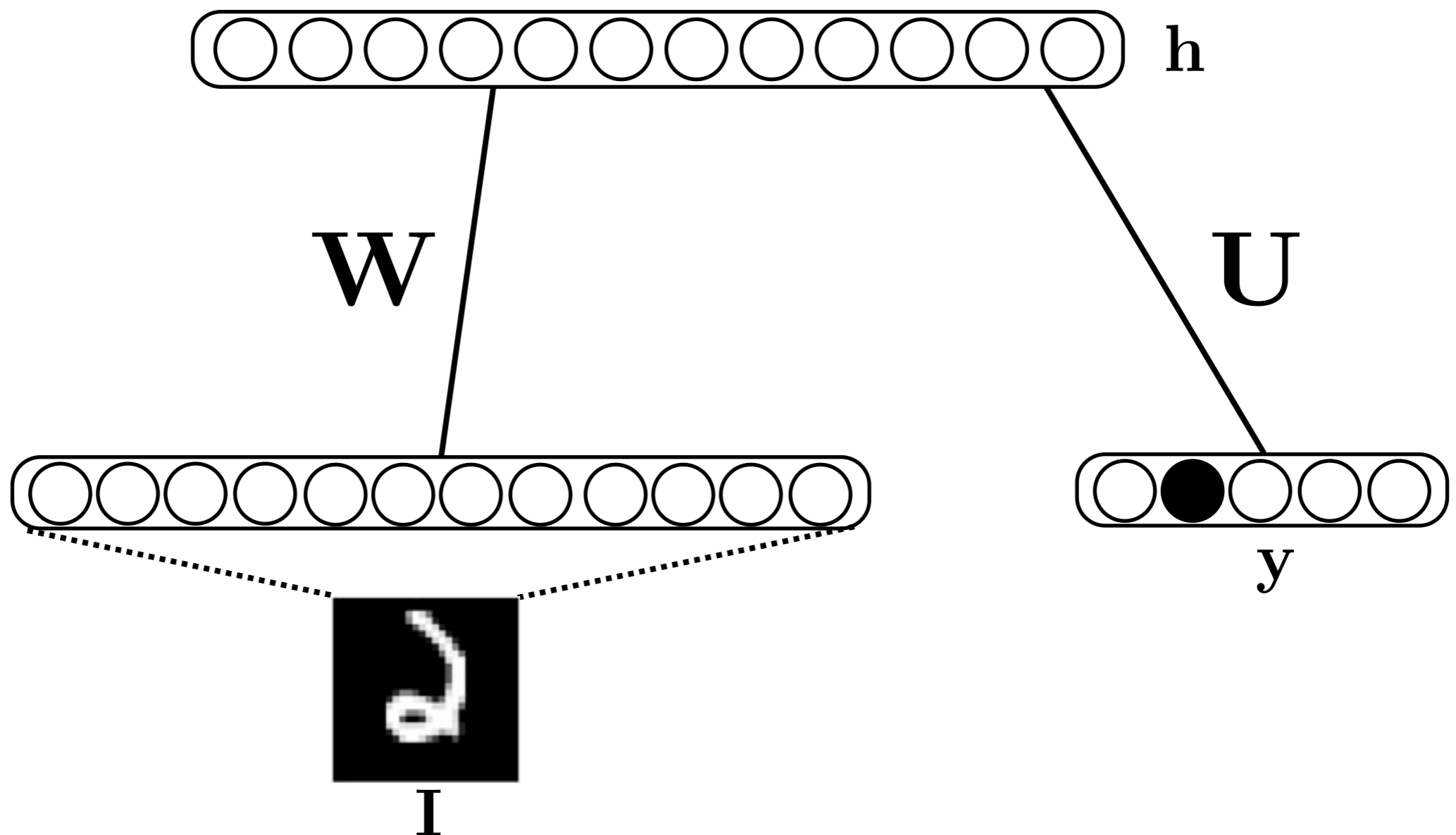
[up] 
$$p(\mathbf{h}|\mathbf{I}, \mathbf{y}) = \prod_j p(h_j|\mathbf{I}, \mathbf{y})$$

[down] 
$$p(\mathbf{I}, \mathbf{y}|\mathbf{h}) = p(\mathbf{y}|\mathbf{h}) \prod_i p(I_i|\mathbf{h})$$



# Restricted Boltzmann Machine (RBM)

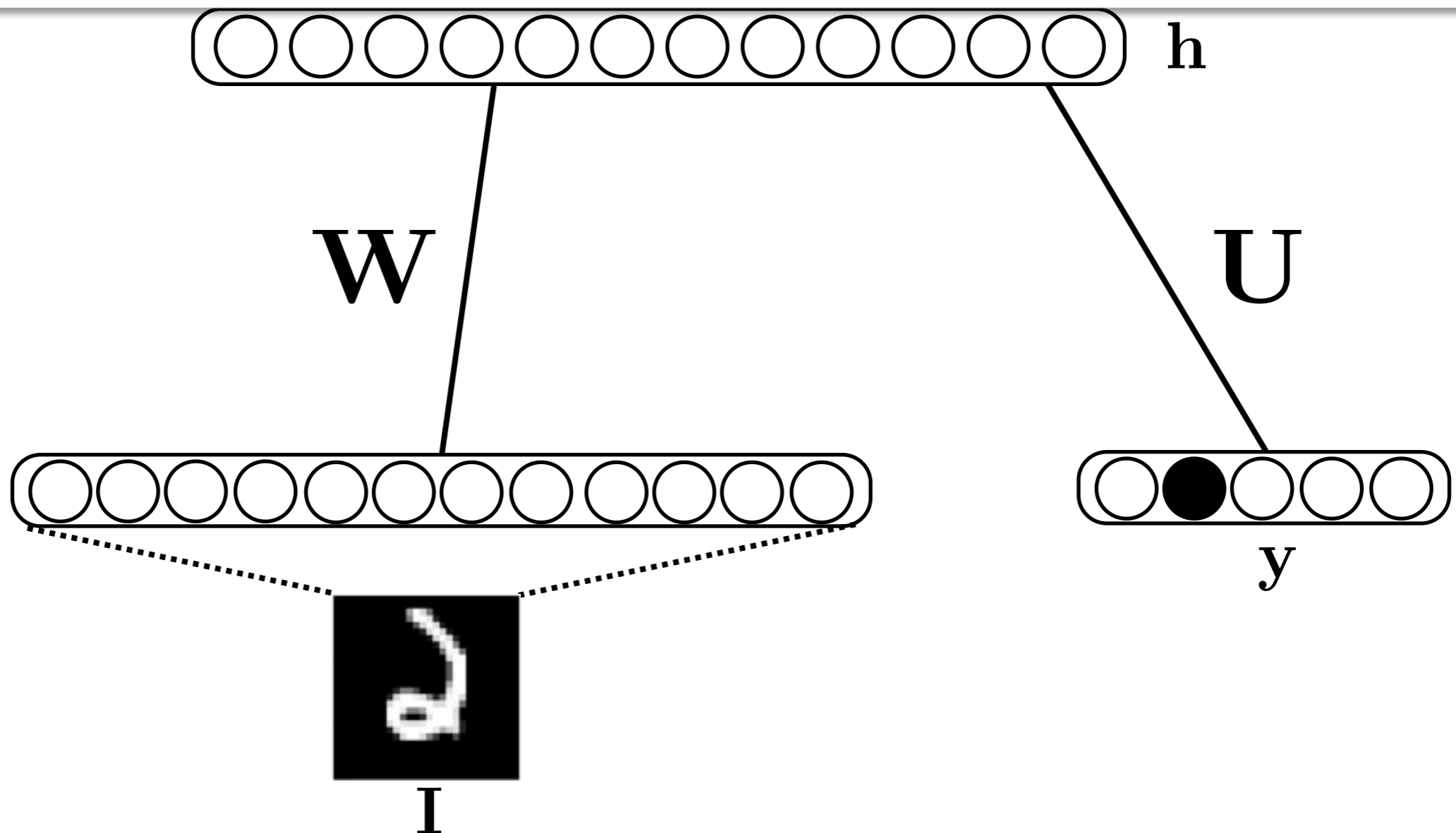
- Classification from the whole image  $\mathbf{I}$



Classification is easy:

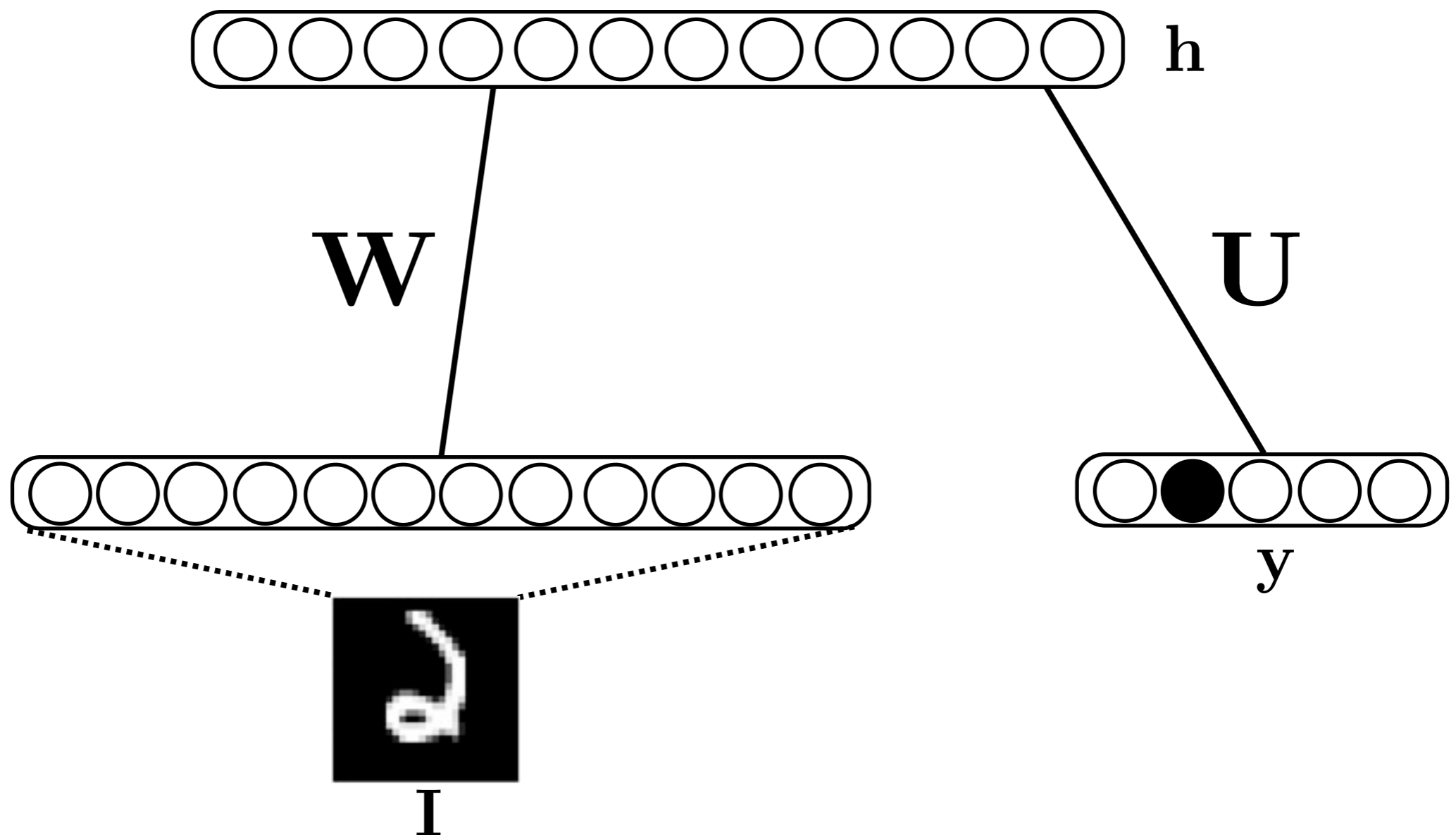
$$p(\mathbf{y}|\mathbf{I}) = \exp(-F(\mathbf{y}, \mathbf{I})) / \sum_{\mathbf{y}^*} \exp(-F(\mathbf{y}^*, \mathbf{I}))$$

$$F(\mathbf{y}, \mathbf{I}) = - \sum_j \log(1 + \exp(\mathbf{W} \mathbf{I} + \mathbf{U} \mathbf{y}))$$



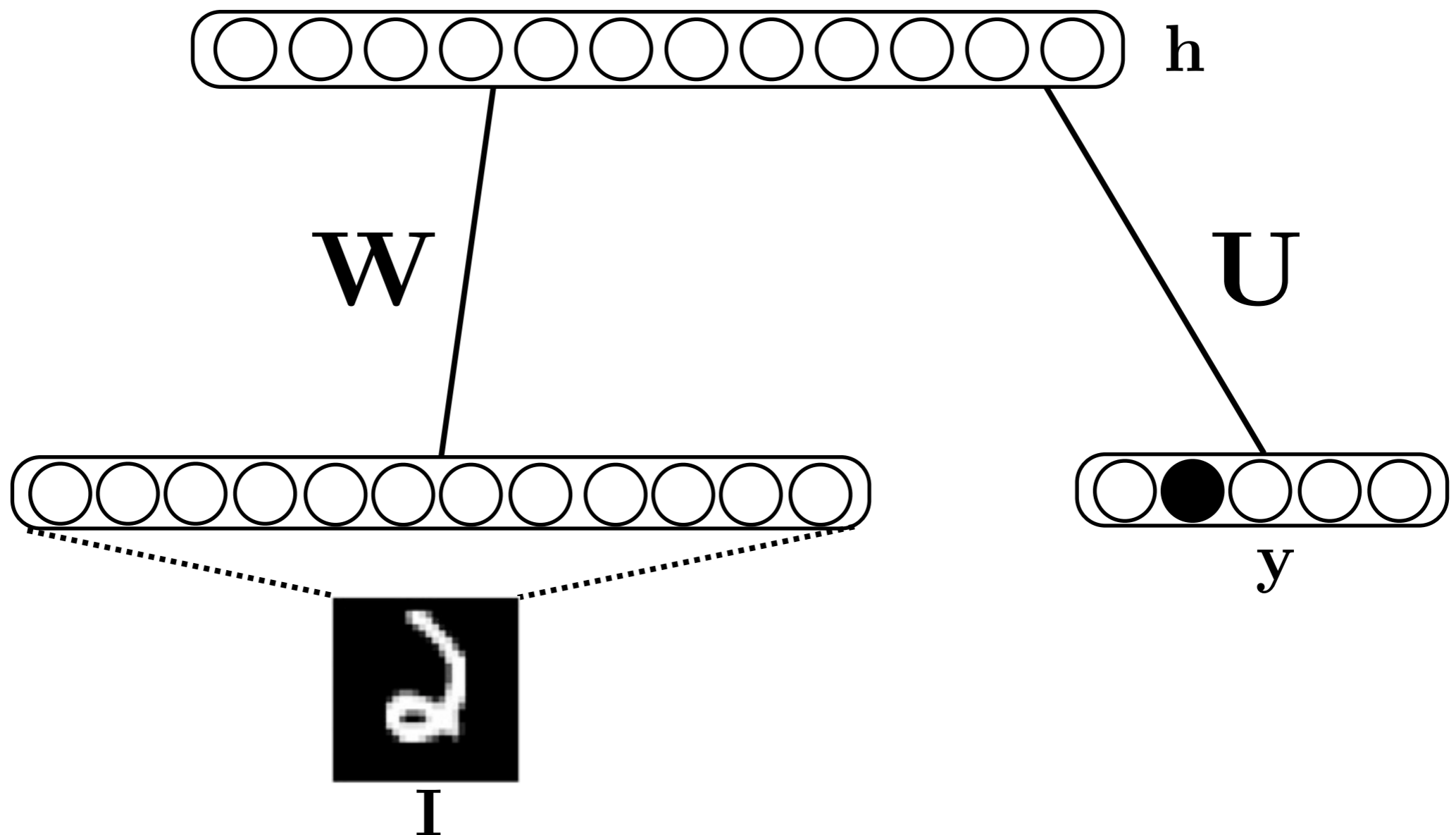
# Restricted Boltzmann Machine (RBM)

- Classification from the whole image  $\mathbf{I}$



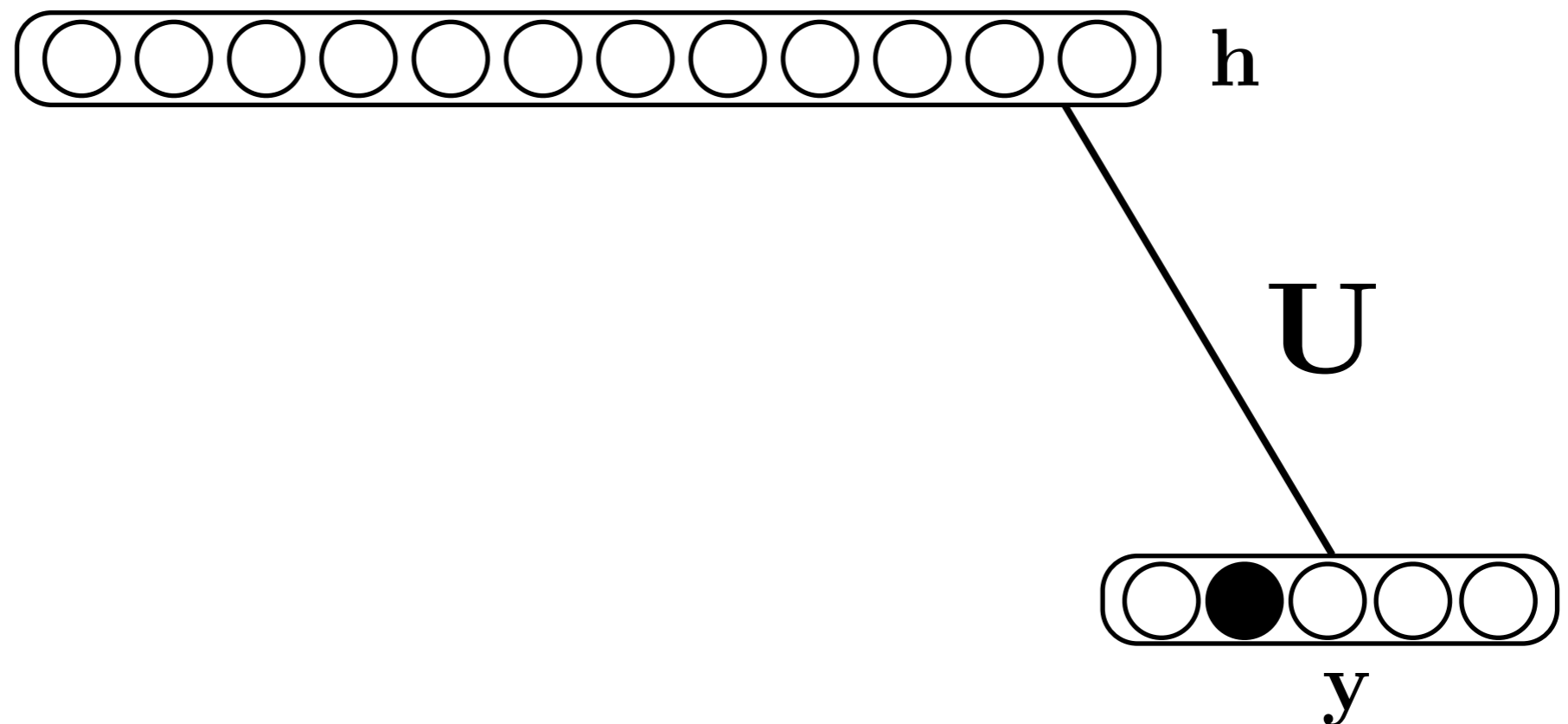
# Restricted Boltzmann Machine (RBM)

- Classification from the whole image  $\mathbf{I}$



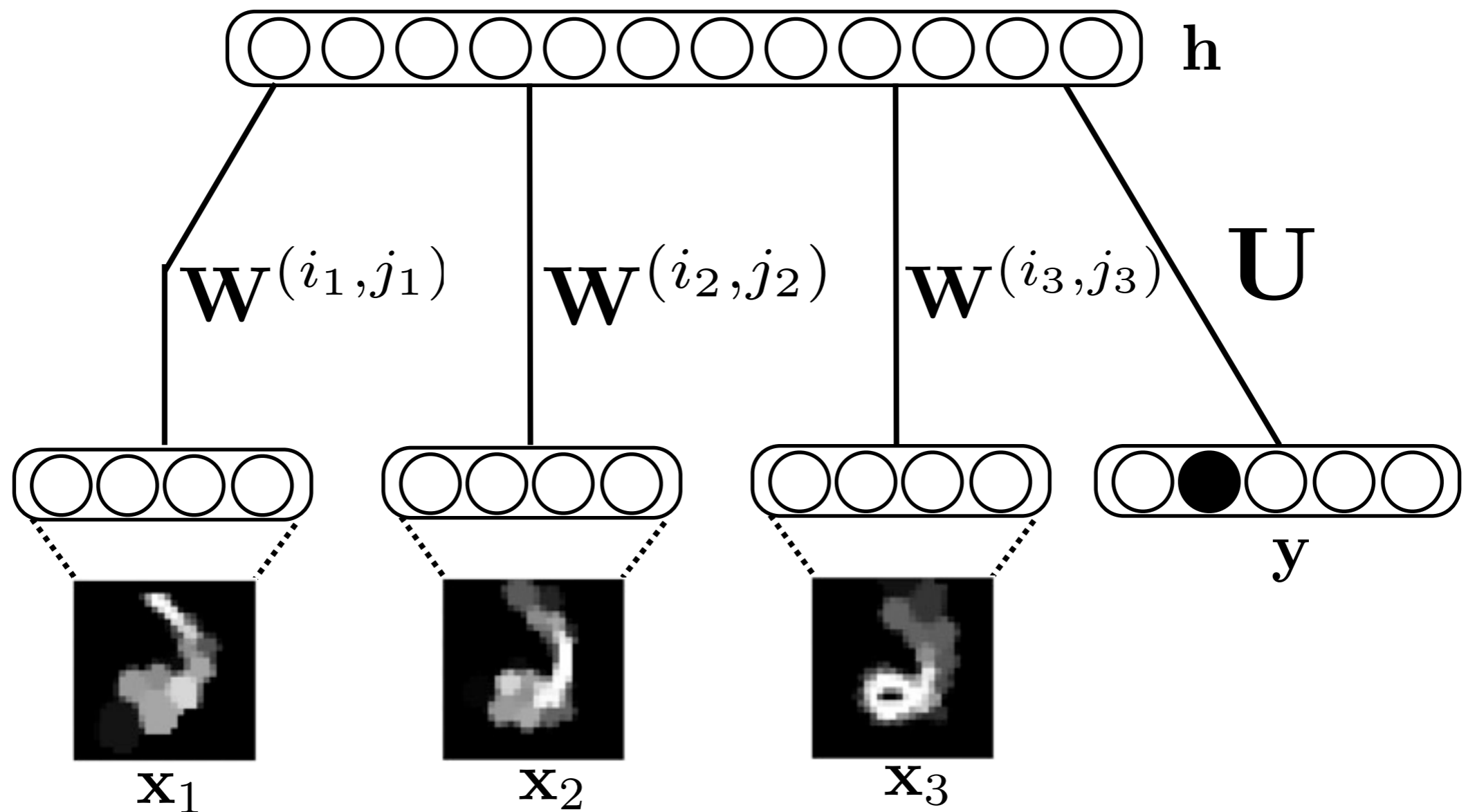
# Restricted Boltzmann Machine (RBM)

- Classification from the whole image  $\mathbf{I}$



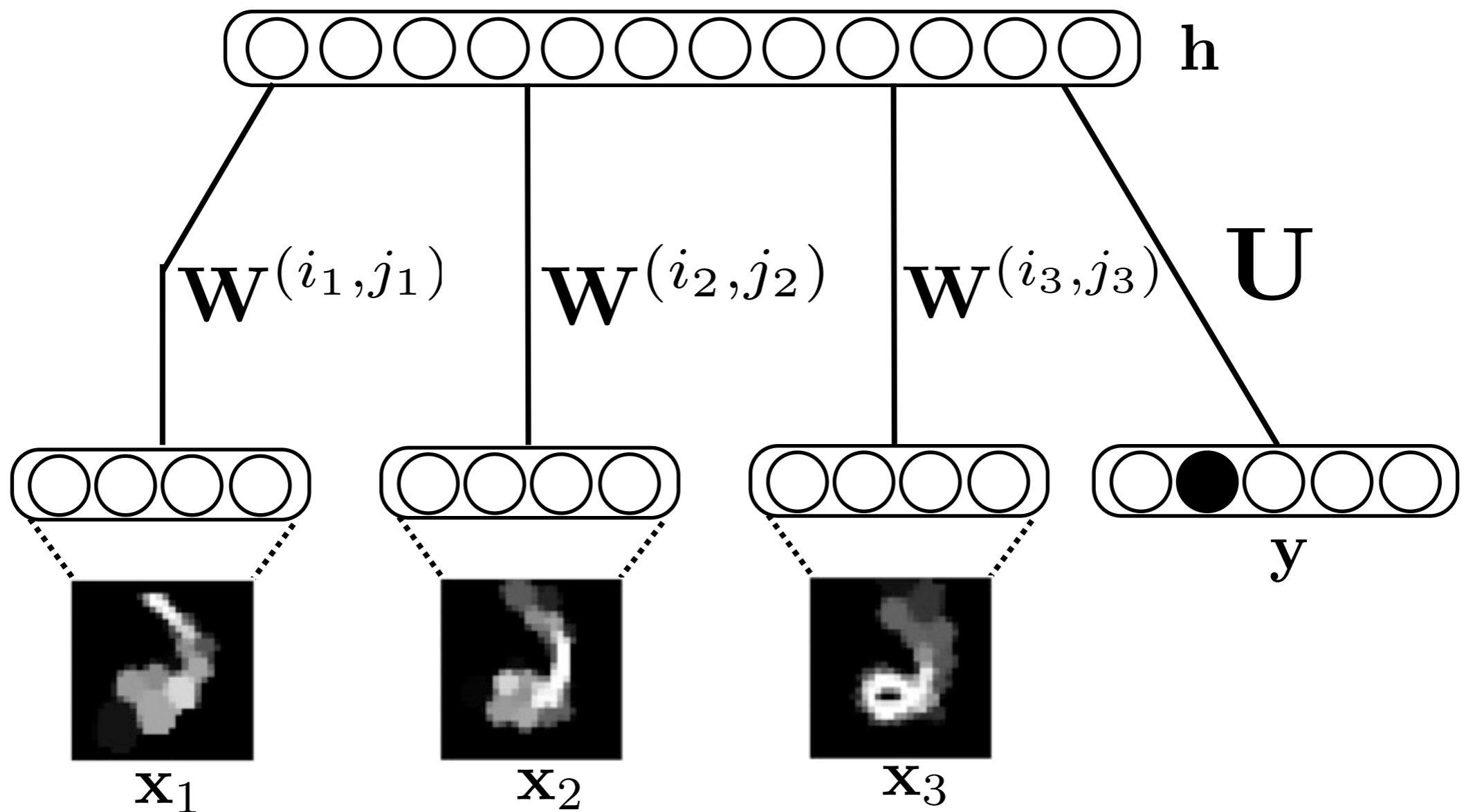
# Restricted Boltzmann Machine (RBM)

- Classification from the  $K=3$  fixations on  $\mathbf{I}$



# Multi-fixation RBM

- Classification from the  $K=3$  fixations on  $\mathbf{I}$

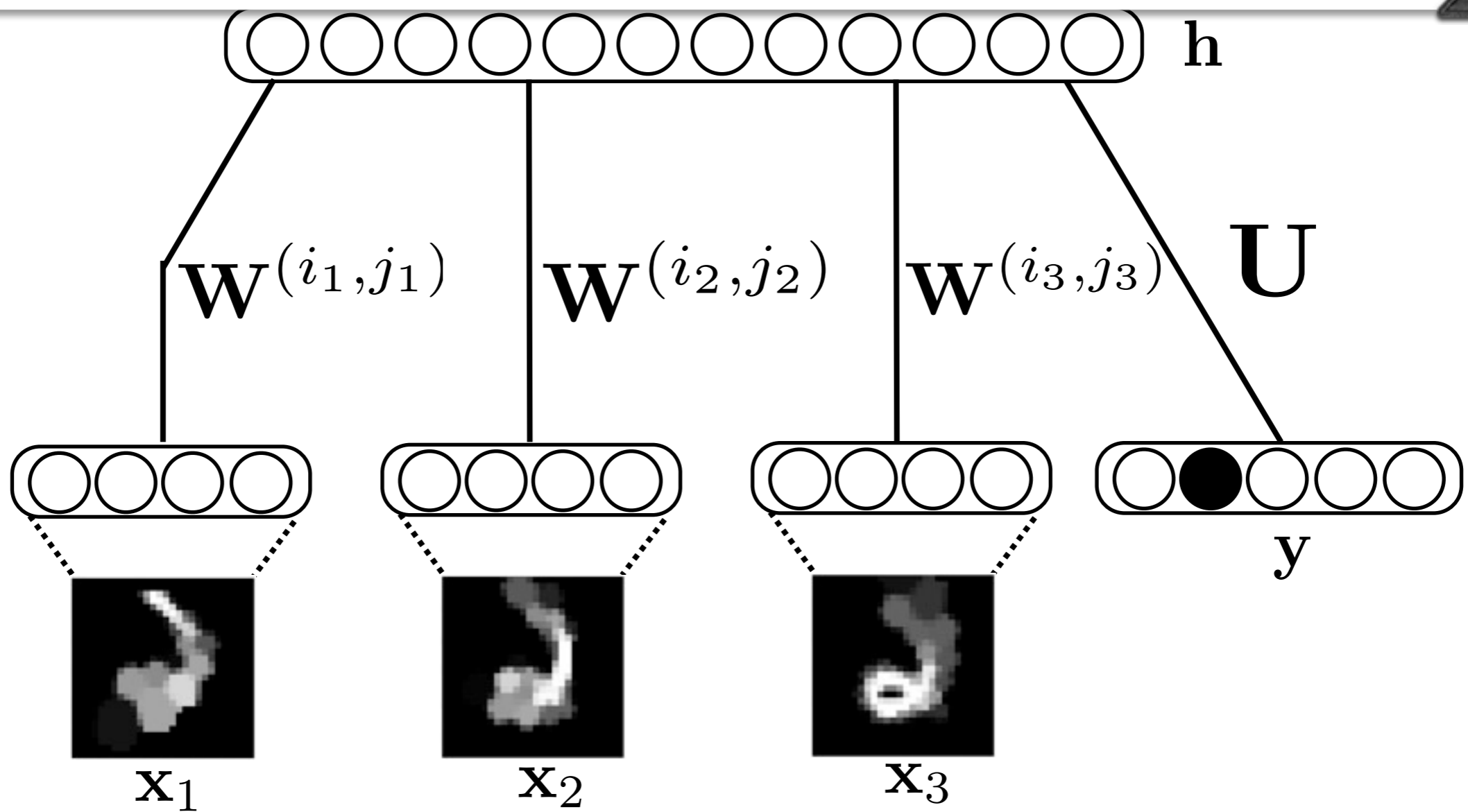




# Weight Factorization

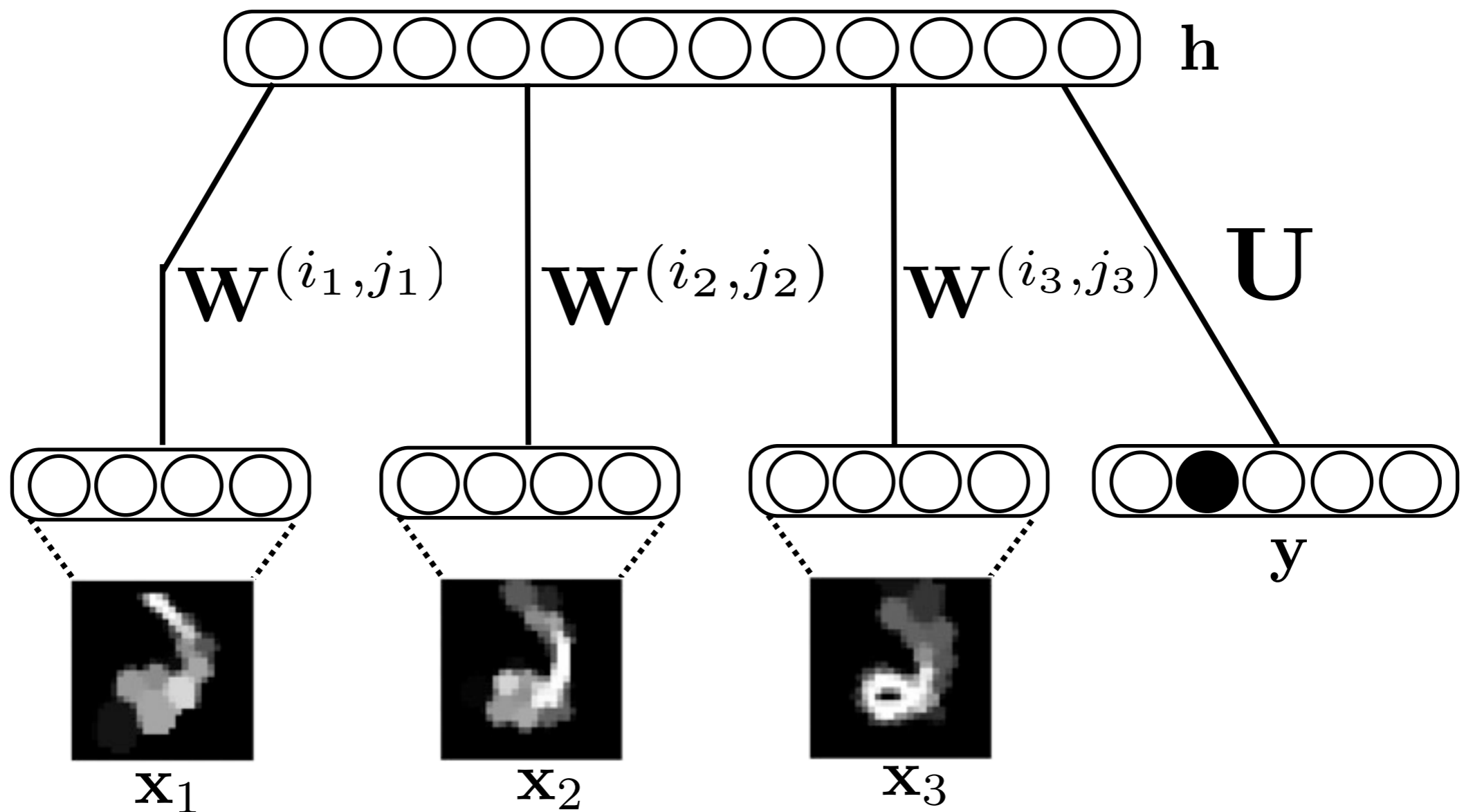
$$\mathbf{W}^{(i_k, j_k)} = \mathbf{P} \text{diag}(\mathbf{z}^{(i_k, j_k)}) \mathbf{F}$$

pooling                      gating                      filters



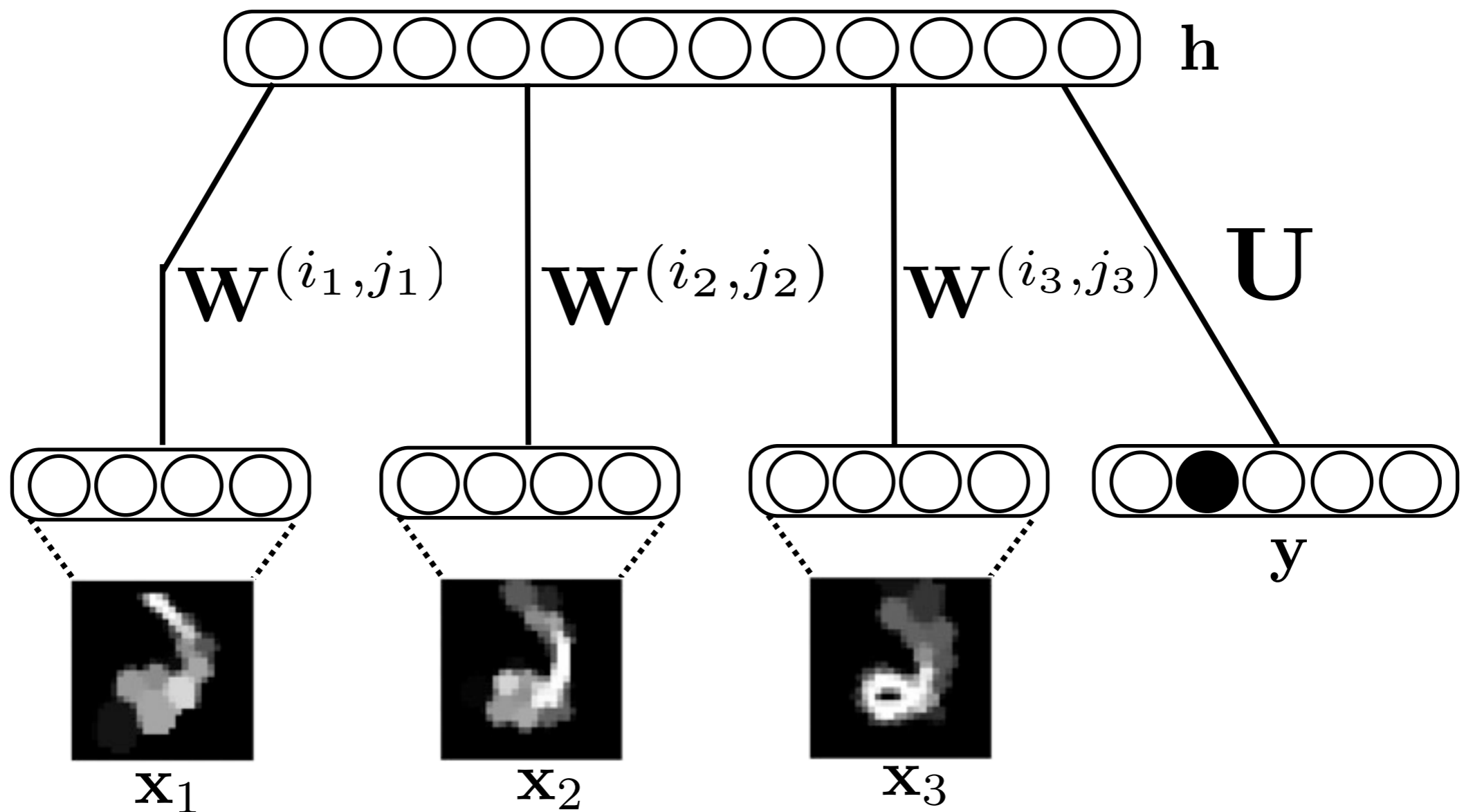
# Multi-fixation RBM

- Classification from the  $K=3$  fixations on  $\mathbf{I}$



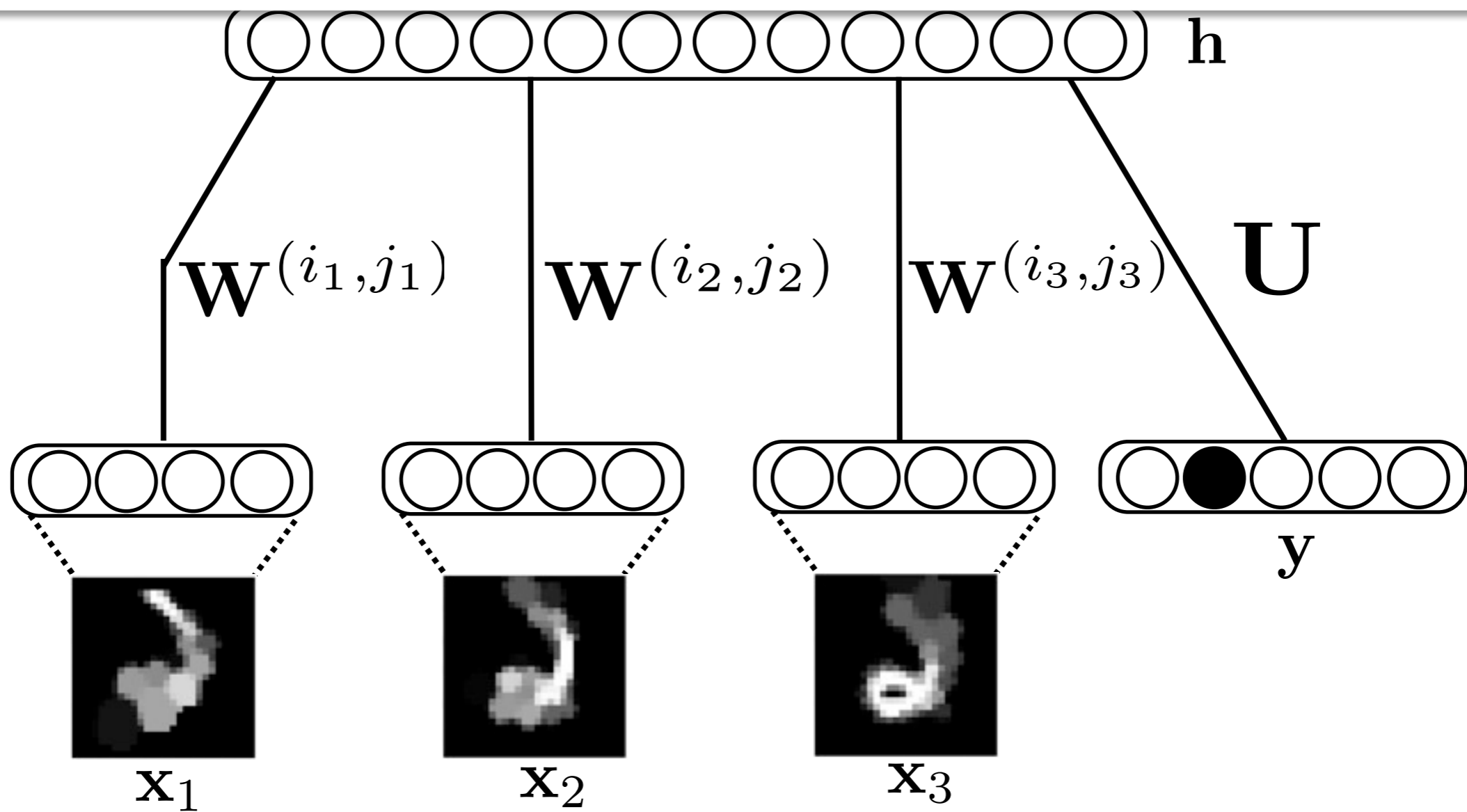
# Multi-fixation RBM

- Classification from the  $K=3$  fixations on  $\mathbf{I}$



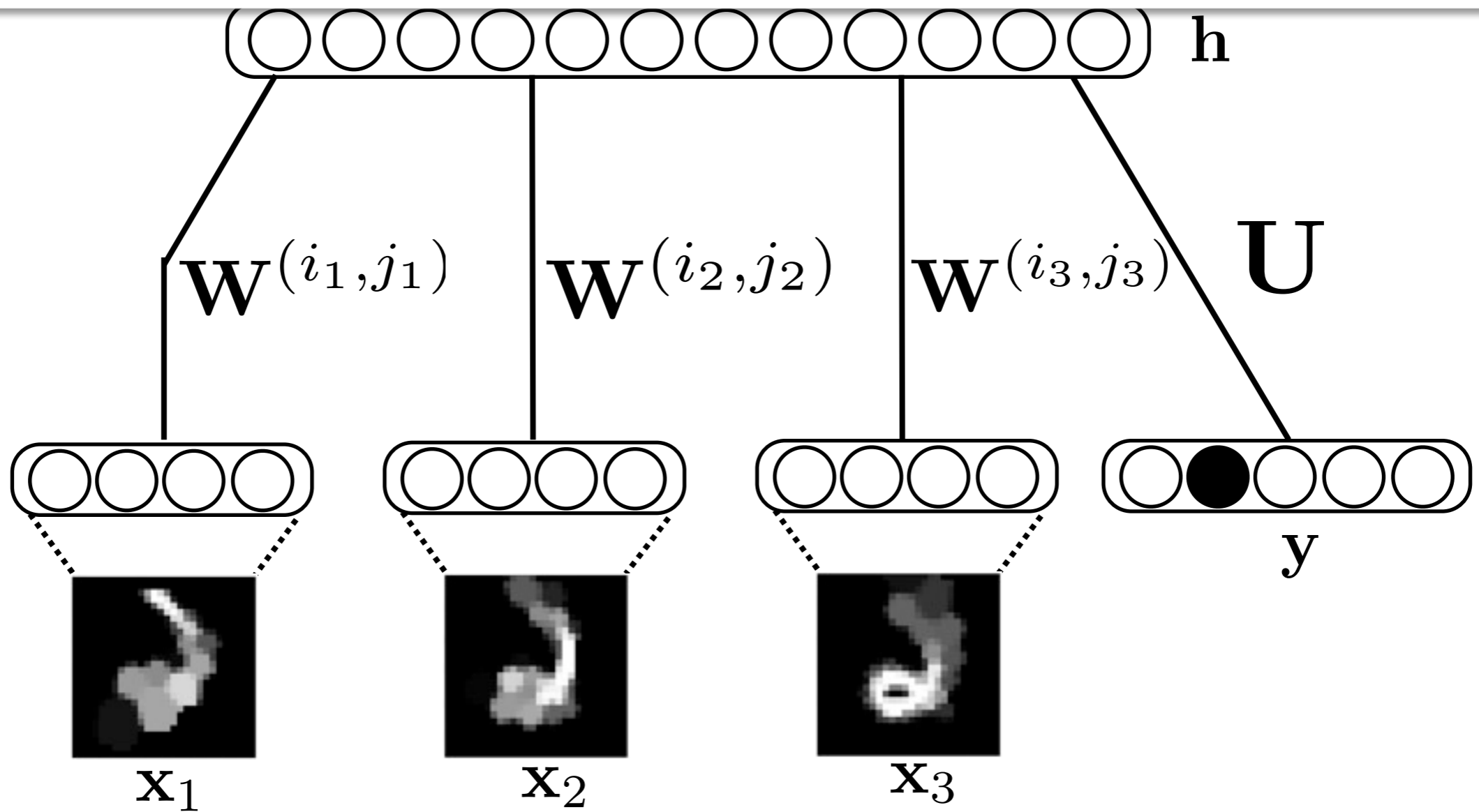
# Weight Factorization

$$\mathbf{W}^{(i_1, j_1)} \mathbf{x}_1 = \mathbf{x}_1$$



# Weight Factorization

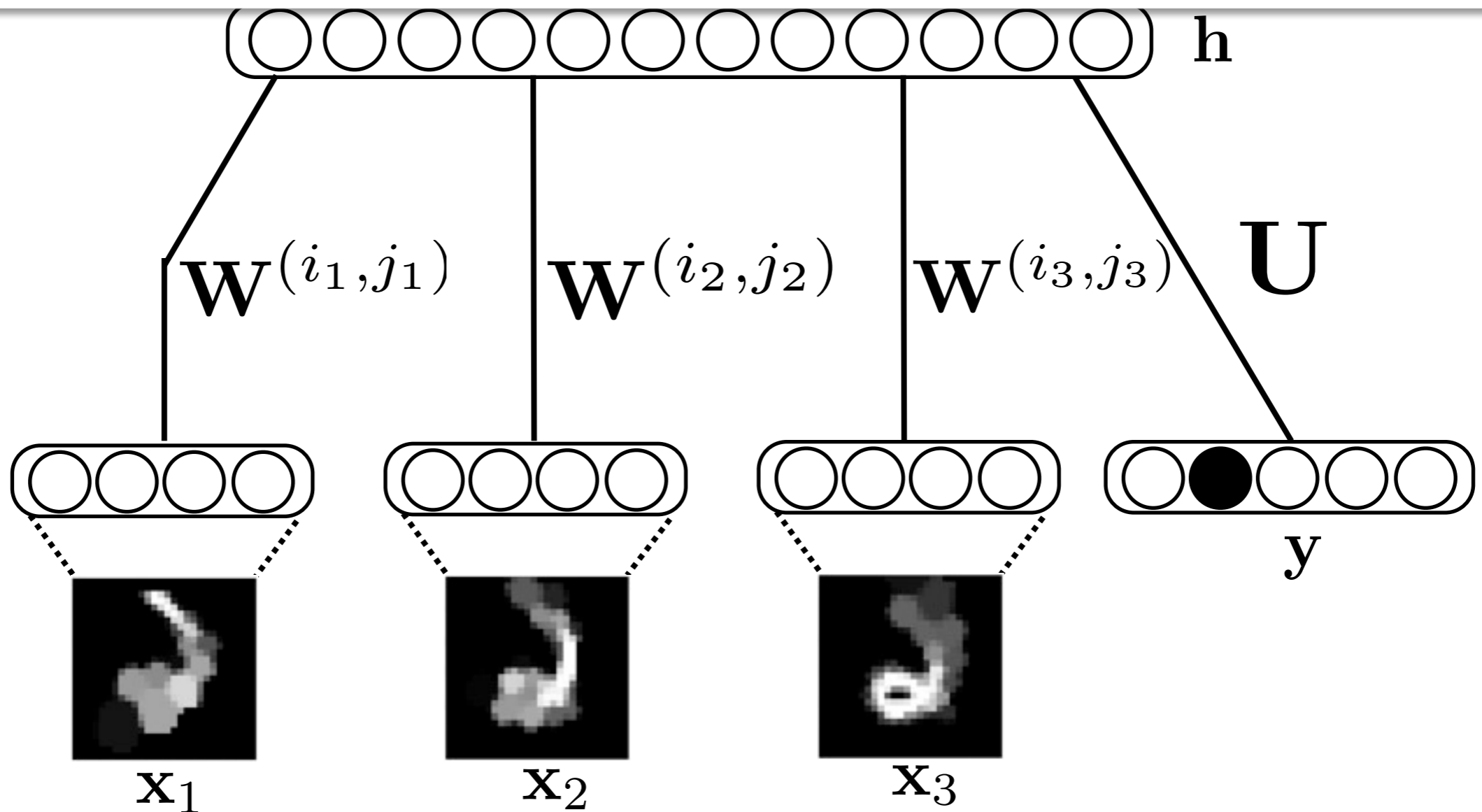
$$\mathbf{W}^{(i_1, j_1)} \mathbf{x}_1 = \text{filters} \rightarrow (\mathbf{F} \mathbf{x}_1)$$



# Weight Factorization

$$\mathbf{W}^{(i_1, j_1)} \mathbf{x}_1 = \left( \mathbf{z}^{(i_1, j_1)} \odot (\mathbf{F} \mathbf{x}_1) \right)$$

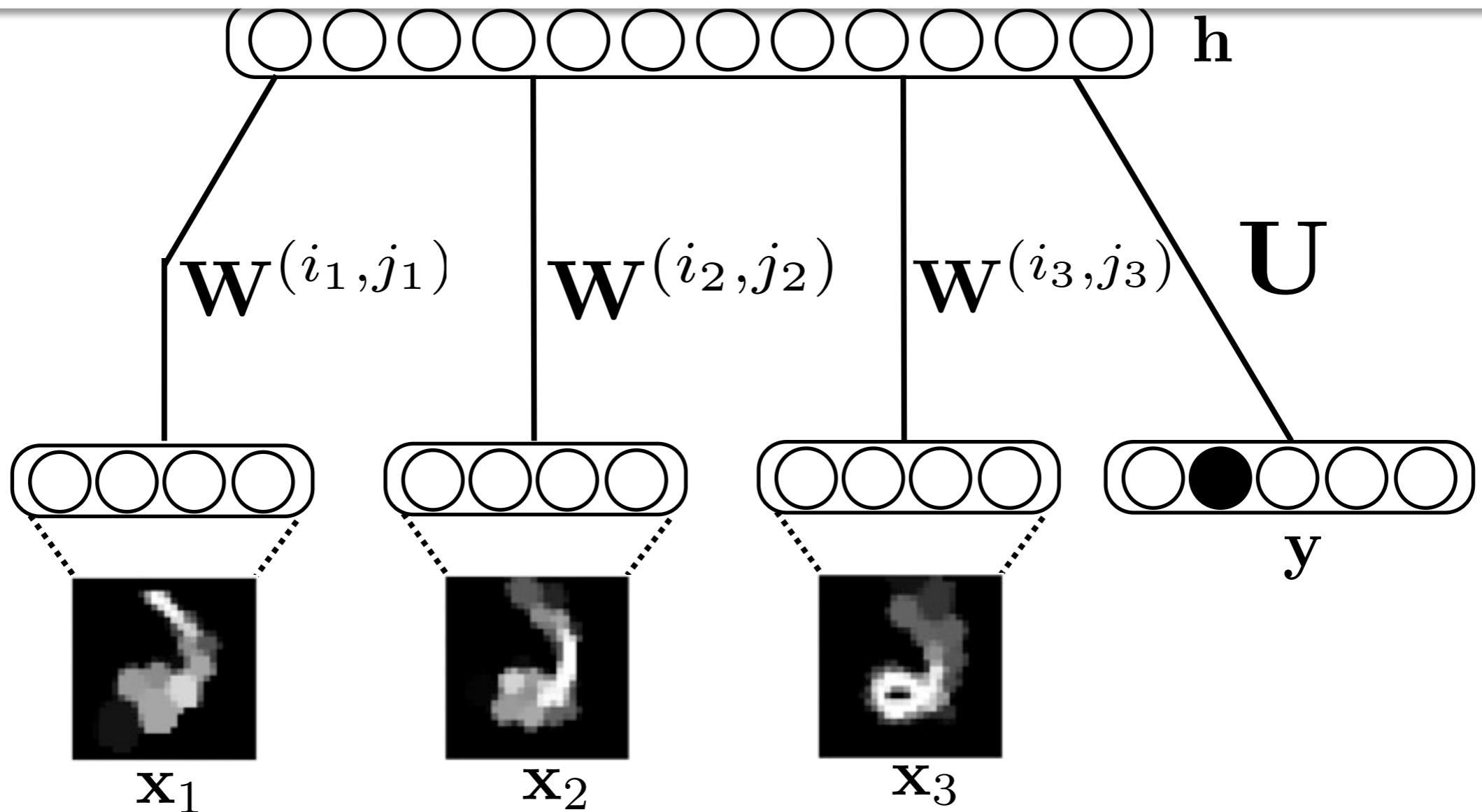
gating      filters



# Weight Factorization

$$\mathbf{W}^{(i_1, j_1)} \mathbf{x}_1 = \mathbf{P} \left( \mathbf{z}^{(i_1, j_1)} \odot (\mathbf{F} \mathbf{x}_1) \right)$$

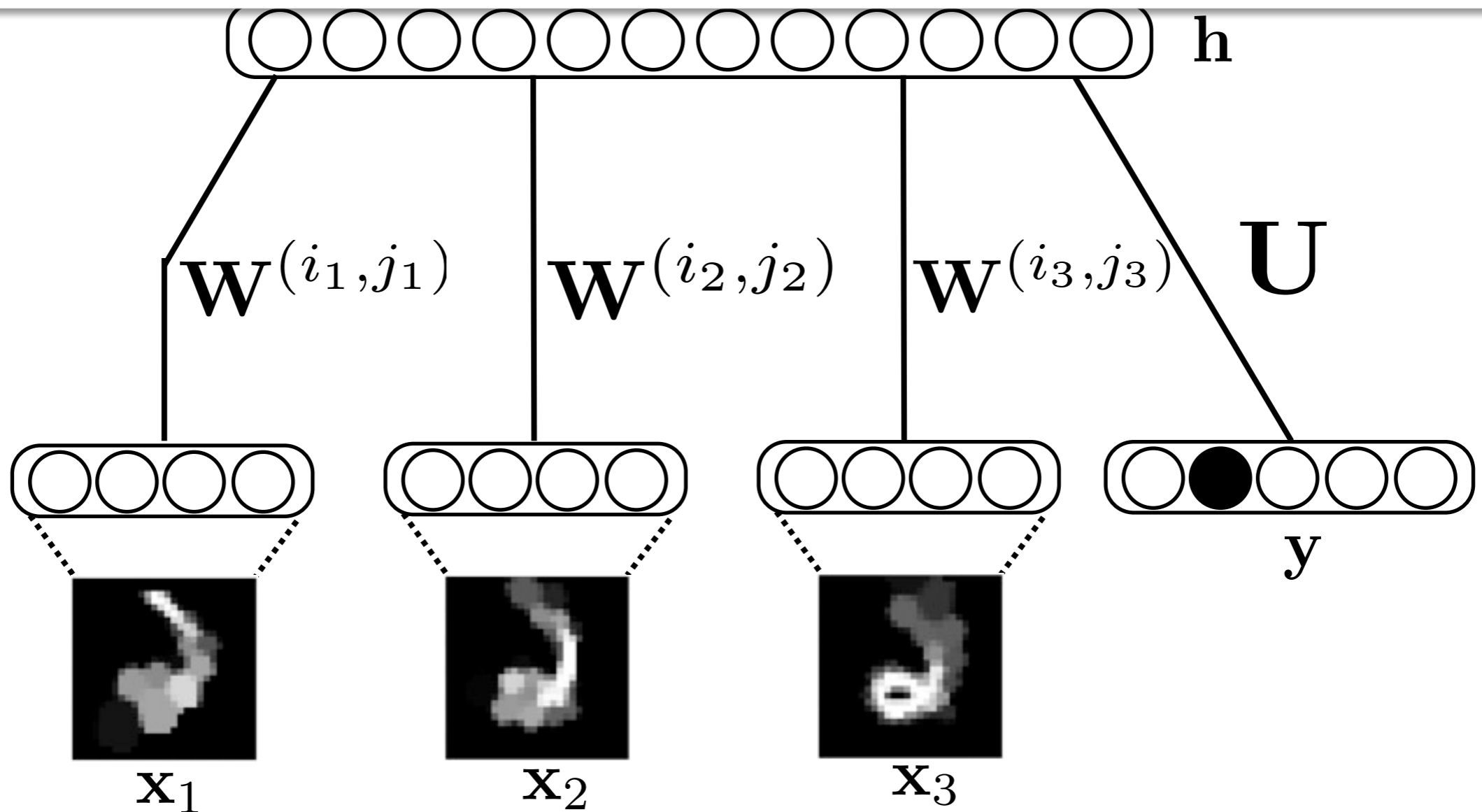
pooling      gating      filters



# Weight Factorization

$$\mathbf{W}^{(i_2, j_2)} \mathbf{x}_2 = \mathbf{P} \left( \mathbf{z}^{(i_1, j_1)} \odot (\mathbf{F} \mathbf{x}_2) \right)$$

pooling      gating      filters

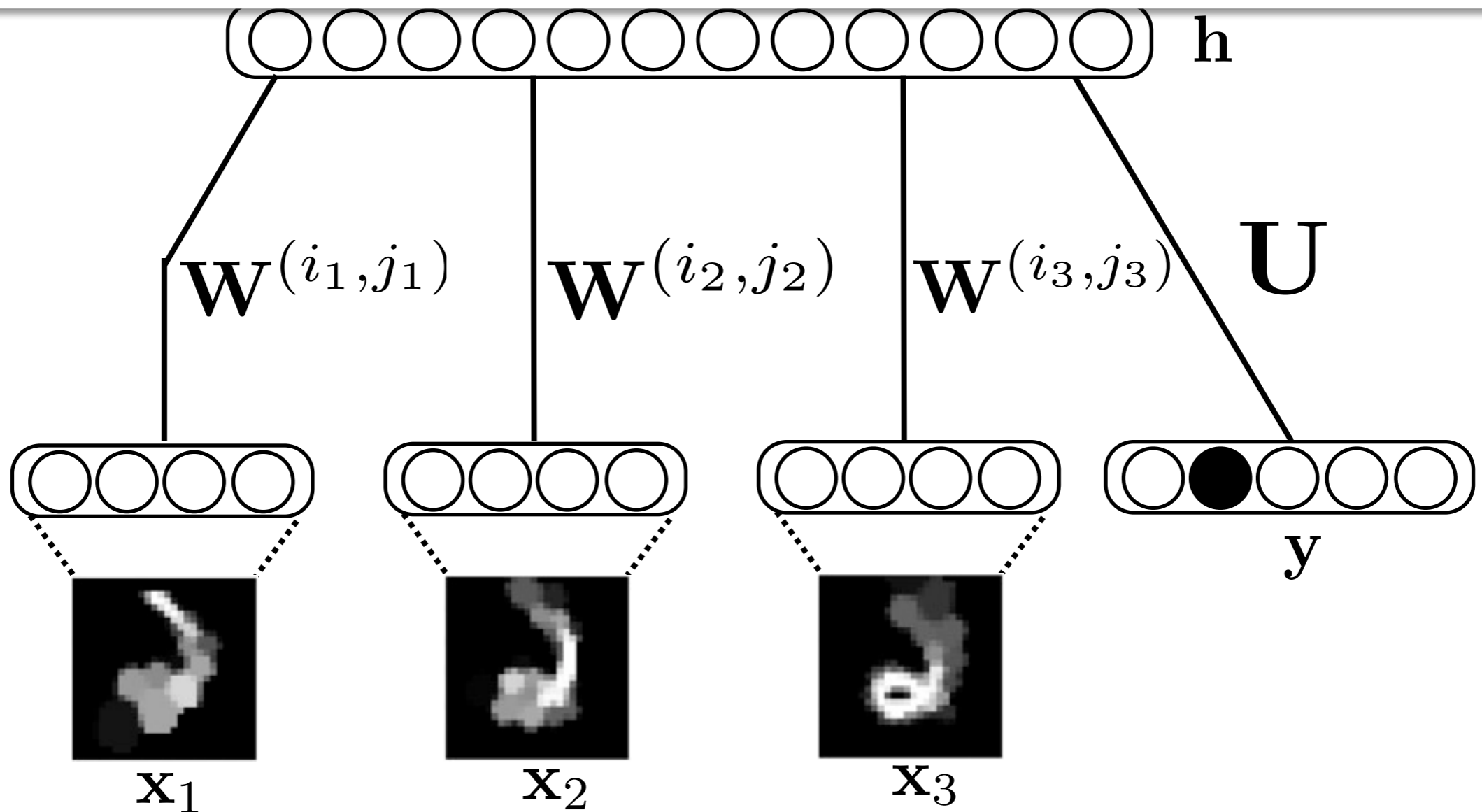




# Weight Factorization

$$\mathbf{W}^{(i_2, j_2)} \mathbf{x}_2 = \mathbf{P} \left( \mathbf{z}^{(i_2, j_2)} \odot (\mathbf{F} \mathbf{x}_2) \right)$$

pooling      gating      filters



# Training objectives

Discriminative:

$$\mathcal{C}_{\text{disc}} = -\log p(\mathbf{y}^t | \mathbf{x}_{1:K}^t)$$

Generative:

$$\mathcal{C}_{\text{gen}} = -\log p(\mathbf{y}^t, \mathbf{x}_{1:K}^t)$$

Hybrid:

$$\mathcal{C}_{\text{hybrid}} = \mathcal{C}_{\text{disc}} + \alpha \mathcal{C}_{\text{gen}}$$

Bouchard &  
Triggs, 2004

Hybrid-  
sequential:

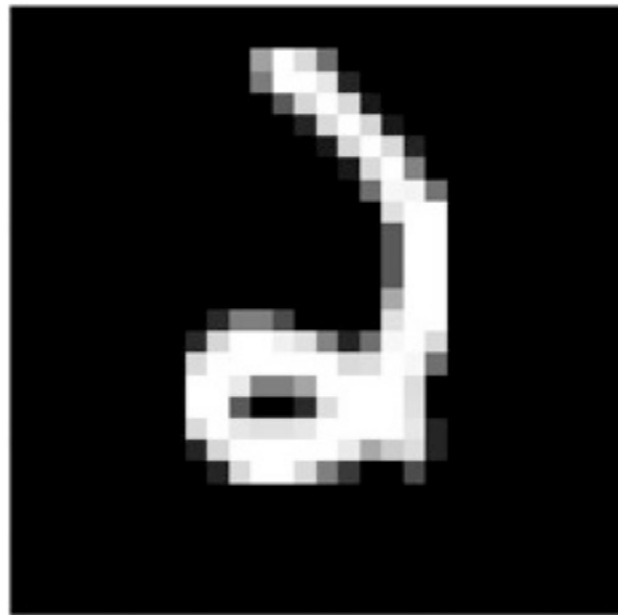
$$\sum_{k=1}^K -\log p(\mathbf{y}^t | \mathbf{x}_{1:k}^t) - \alpha \log p(\mathbf{y}^t, \mathbf{x}_k^t | \mathbf{x}_{1:k-1}^t)$$

# Components of the system

- Recognition component (RBM)
- **Attentional component (controller)**

# Where to look: learning the controller

- Given  $k - 1$  fixations, where should the  $k^{\text{th}}$  one be



# Where to look: learning the controller

- Given  $k - 1$  fixations, where should the  $k^{\text{th}}$  one be

## Summary vector $\mathbf{S}_k$

- ★ previous fixation positions
- ★  $p(h_j = 1 | \mathbf{x}_{1:k-1})$



# Where to look: learning the controller

- Given  $k - 1$  fixations, where should the  $k^{\text{th}}$  one be

Summary vector  $\mathbf{S}_k$

- ★ previous fixation positions
- ★  $p(h_j = 1 | \mathbf{x}_{1:k-1})$

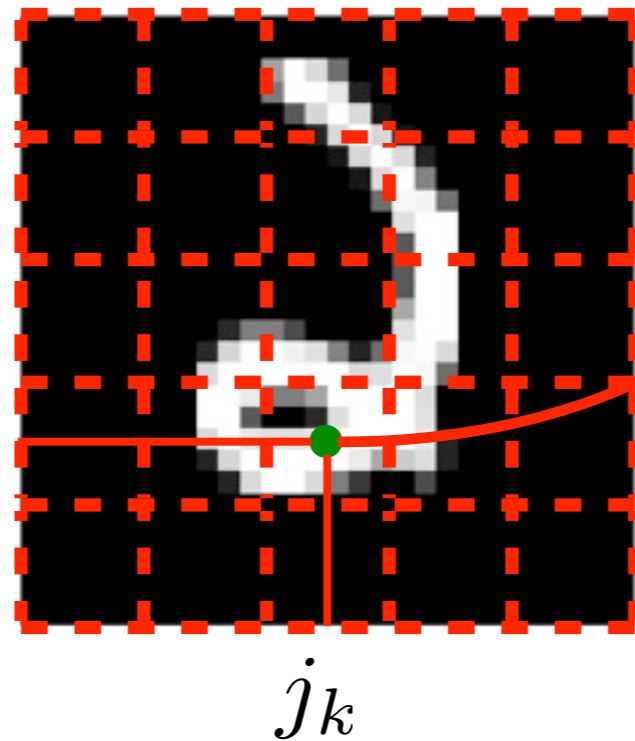


# Where to look: learning the controller

- Given  $k - 1$  fixations, where should the  $k^{\text{th}}$  one be

Summary vector  $\mathbf{S}_k$

- ★ previous fixation positions
- ★  $p(h_j = 1 | \mathbf{x}_{1:k-1})$   $i_k$



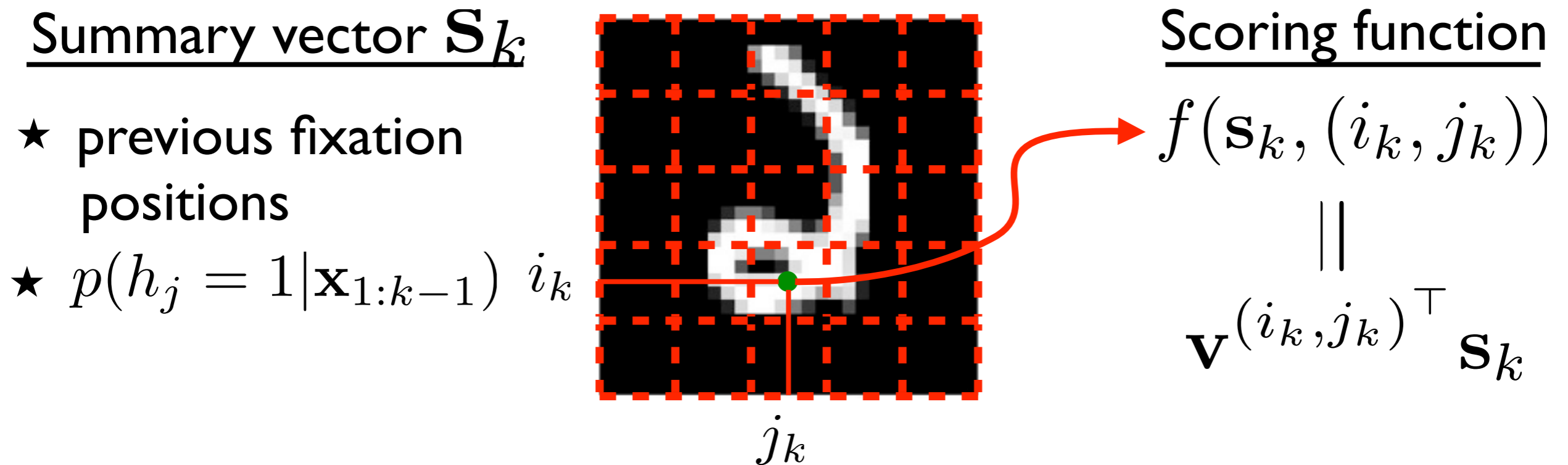
Scoring function

$$f(\mathbf{S}_k, (i_k, j_k))$$

$$\begin{aligned} & \parallel \\ & \mathbf{v}^{(i_k, j_k)\top} \mathbf{S}_k \end{aligned}$$

# Where to look: learning the controller

- Given  $k - 1$  fixations, where should the  $k^{\text{th}}$  one be



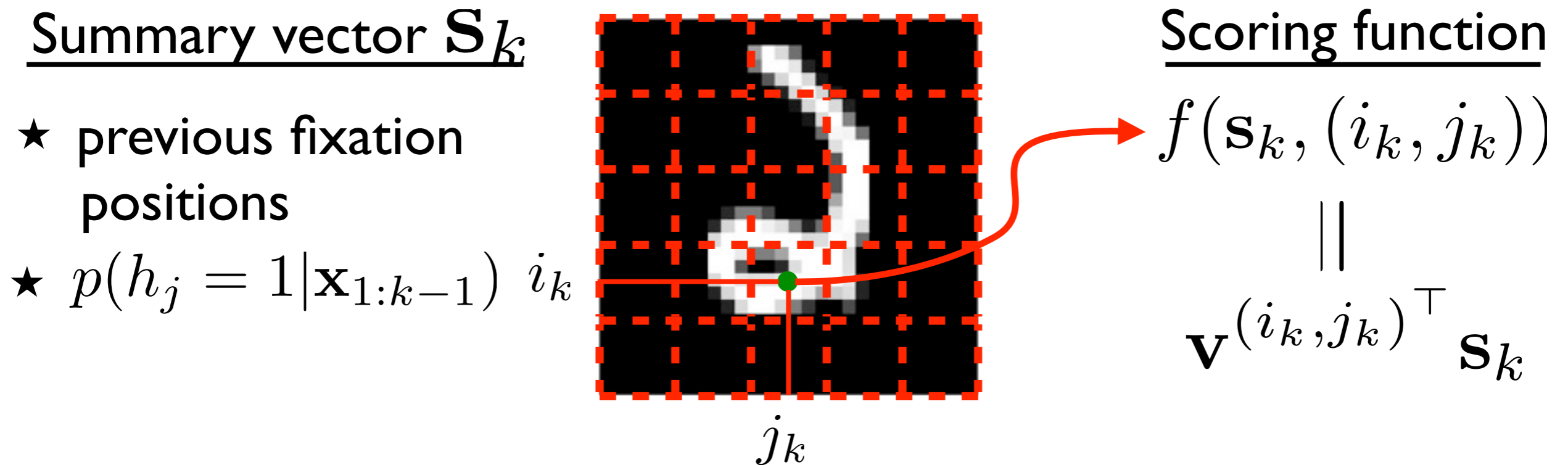
- Training objective of scoring function:

$$|f(\mathbf{S}_k, (i_k, j_k)) - \log p(\mathbf{y} | \mathbf{x}_{1:k-1}, \mathbf{x}_k)|$$



# Where to look: learning the controller

- Given  $k - 1$  fixations, where should the  $k^{\text{th}}$  one be

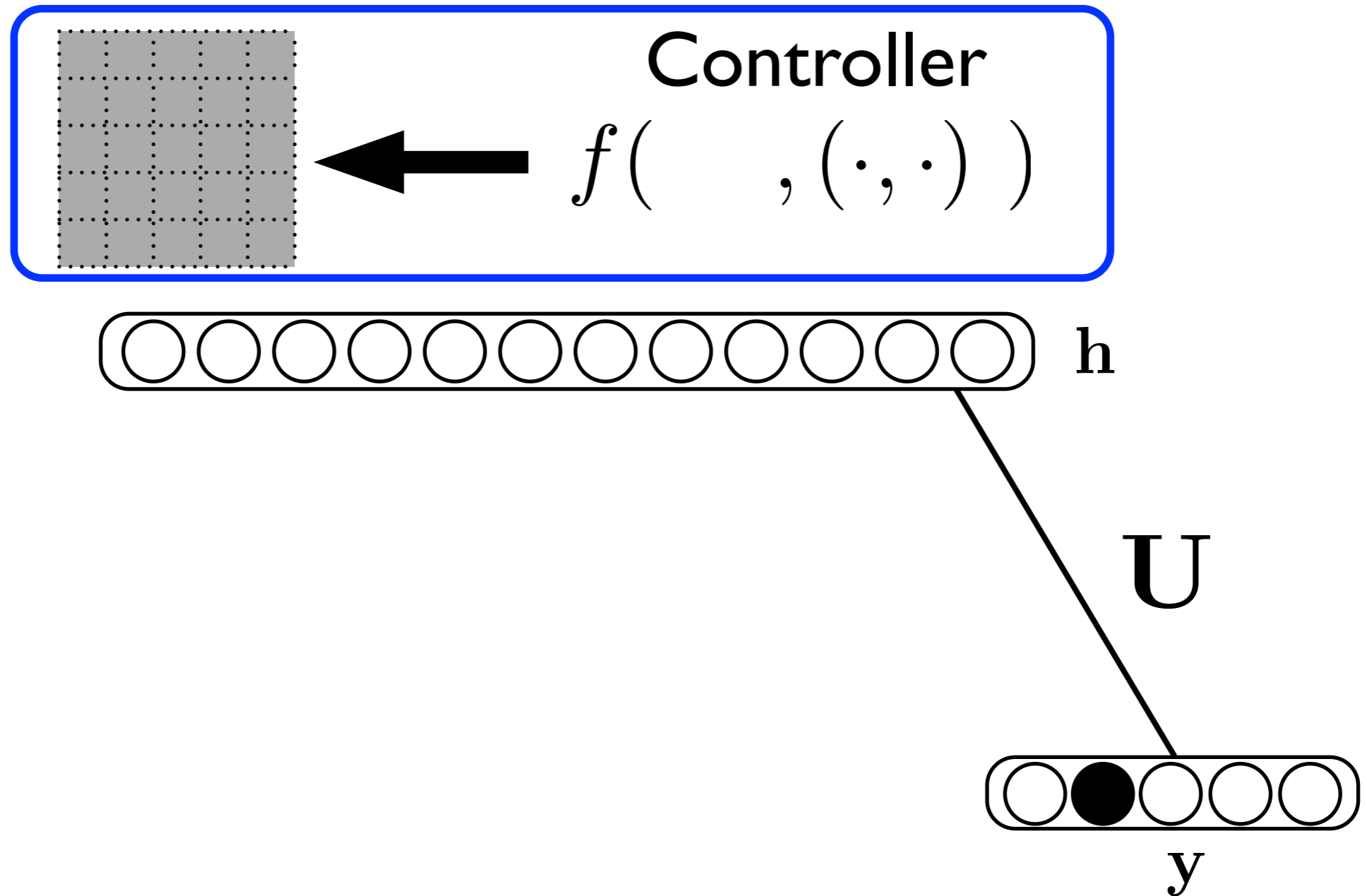


- Training objective of scoring function:

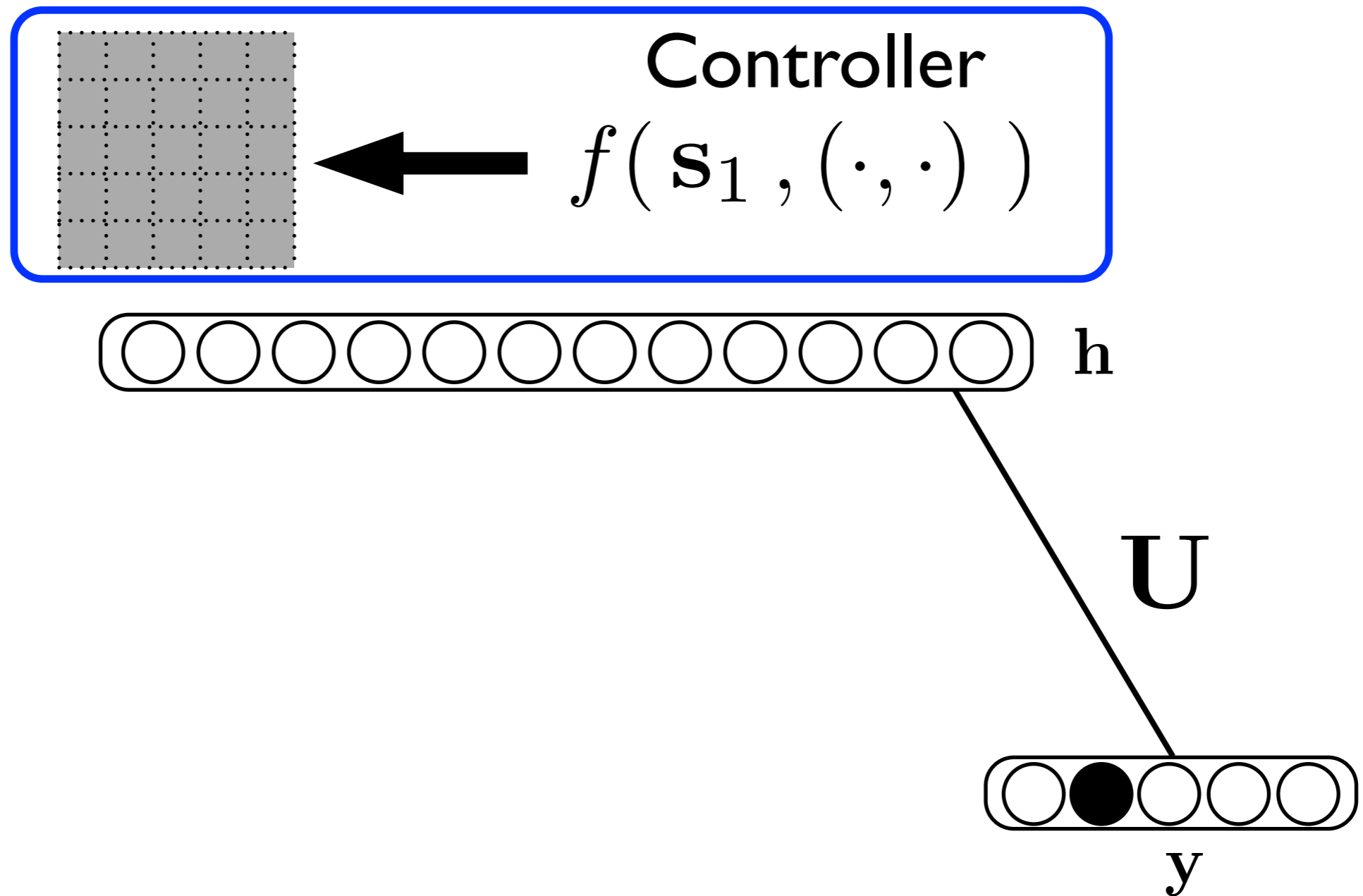
$$|f(\mathbf{S}_k, (i_k, j_k)) - \log p(\mathbf{y} | \mathbf{x}_{1:k-1}, \mathbf{x}_k)|$$

- Controller distribution:  $\exp(f(\mathbf{S}_k, (i_k, j_k))) / Z(\mathbf{S}_k)$

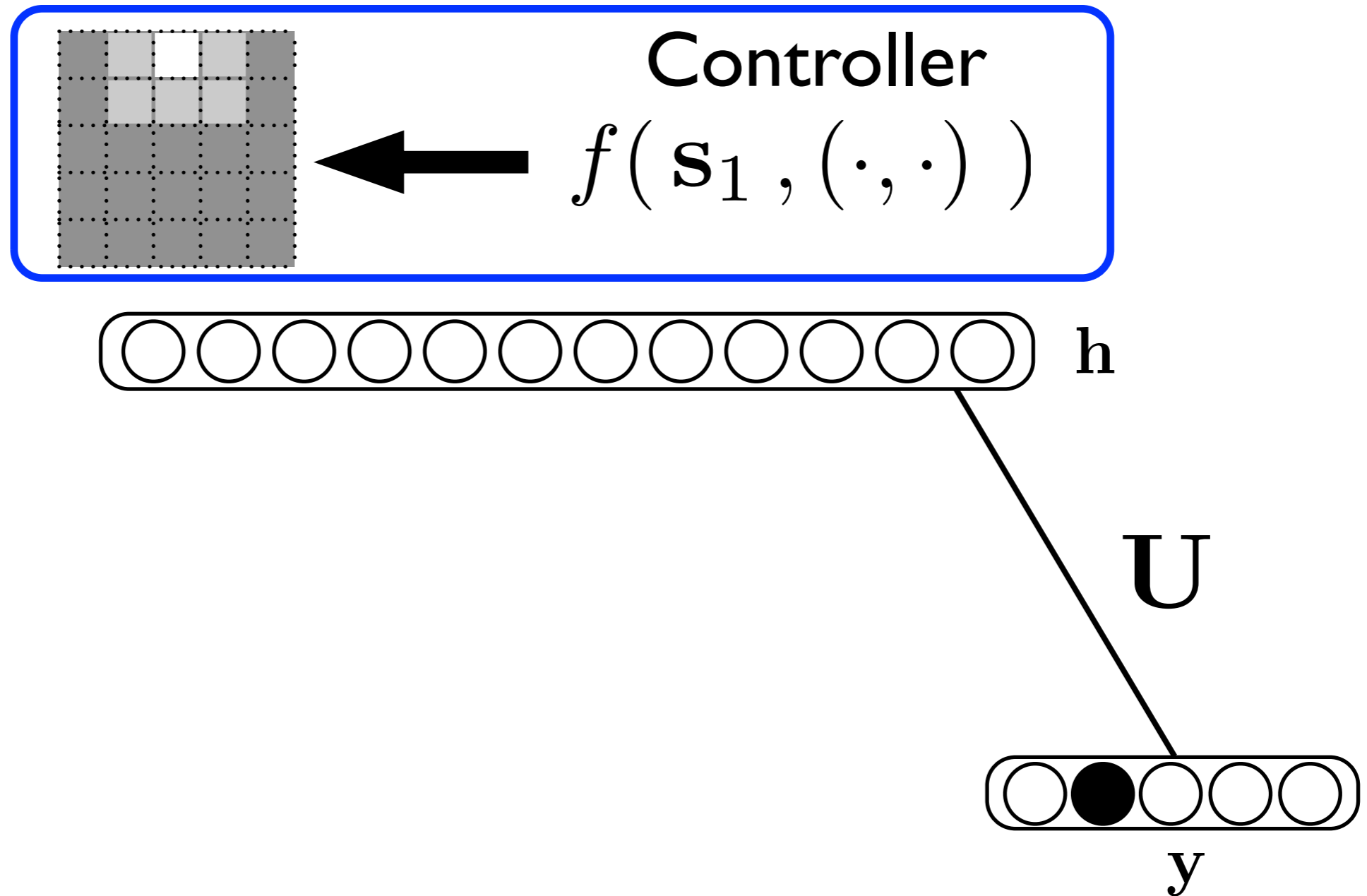
# Putting it all together



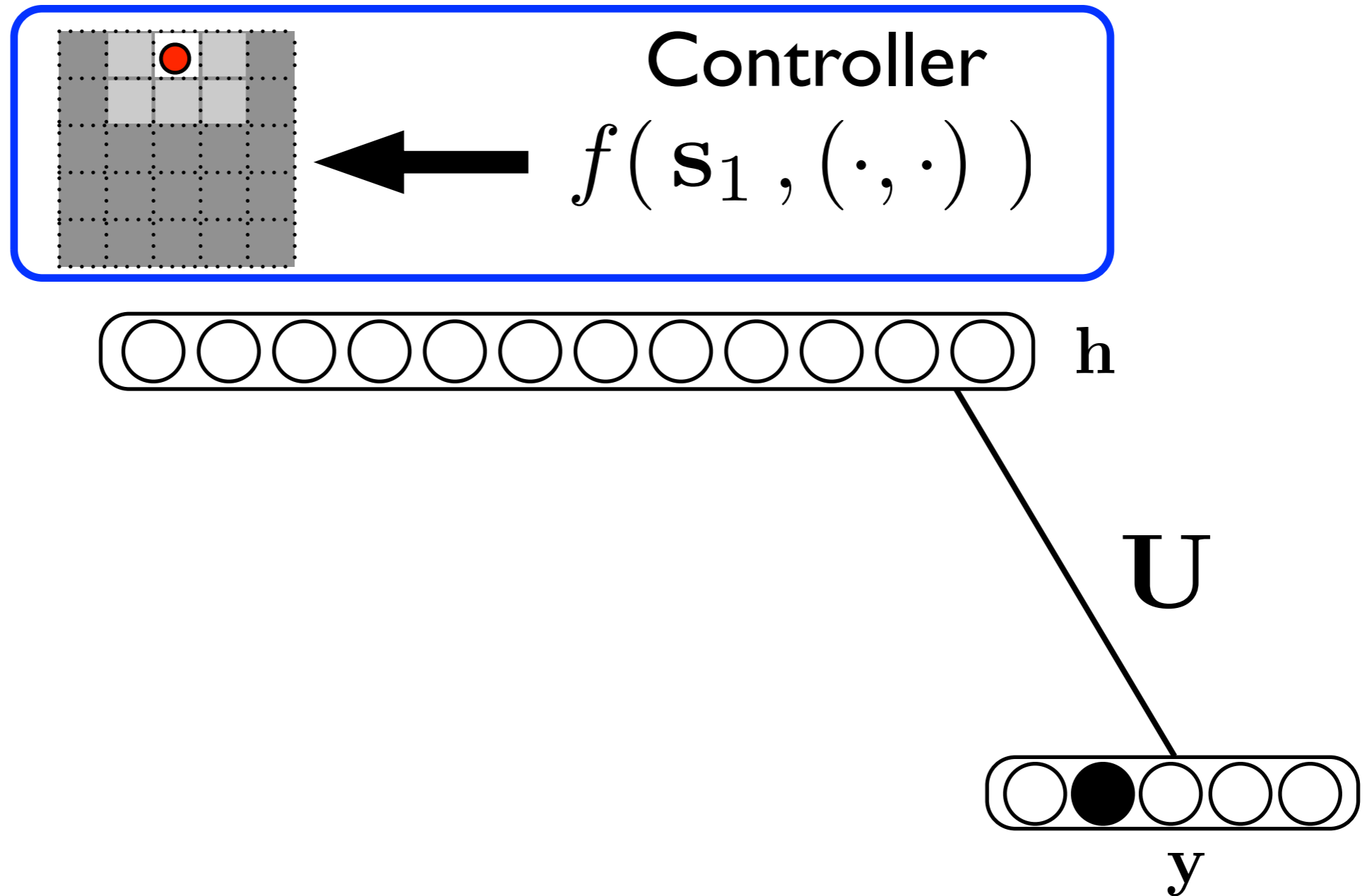
# Putting it all together



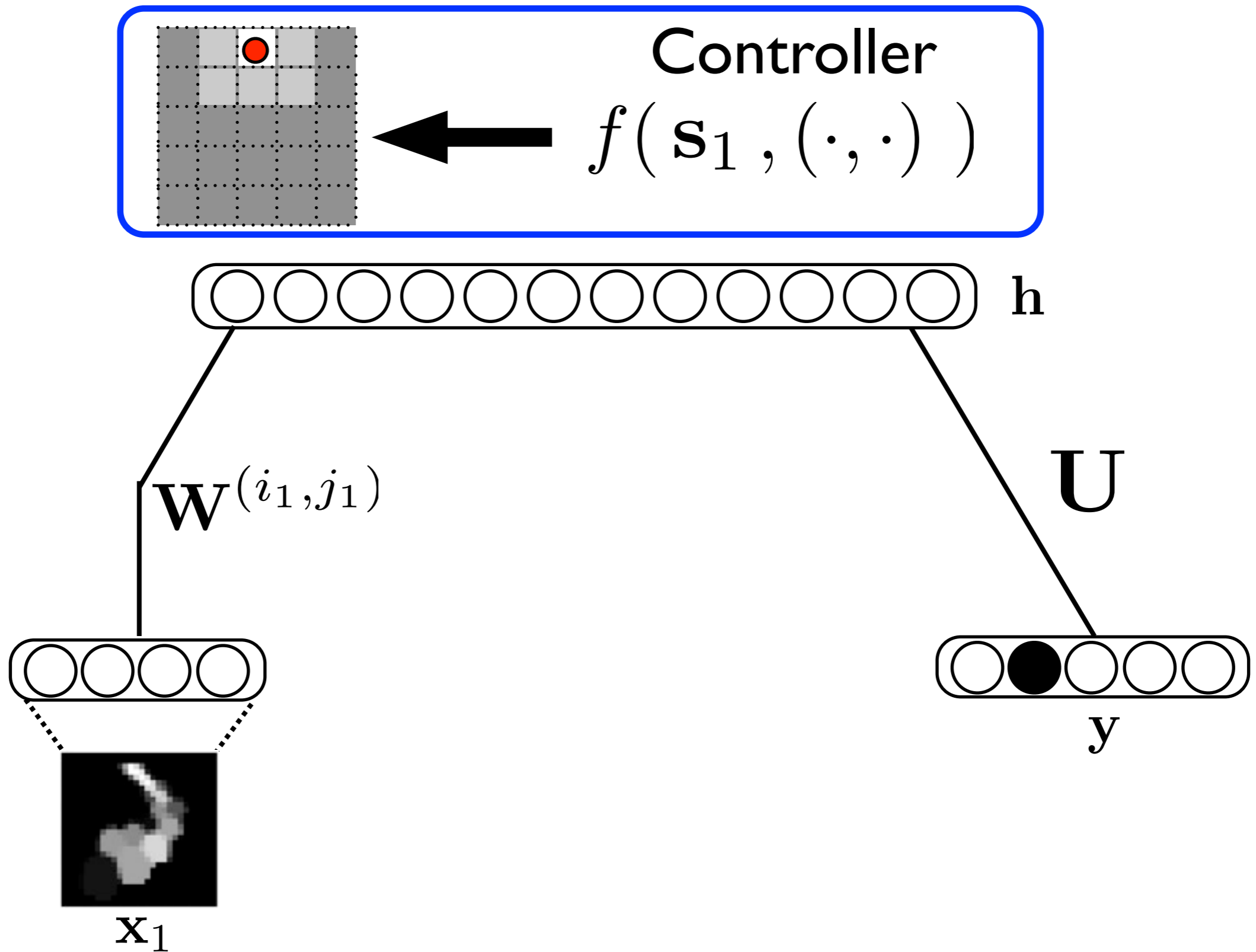
# Putting it all together



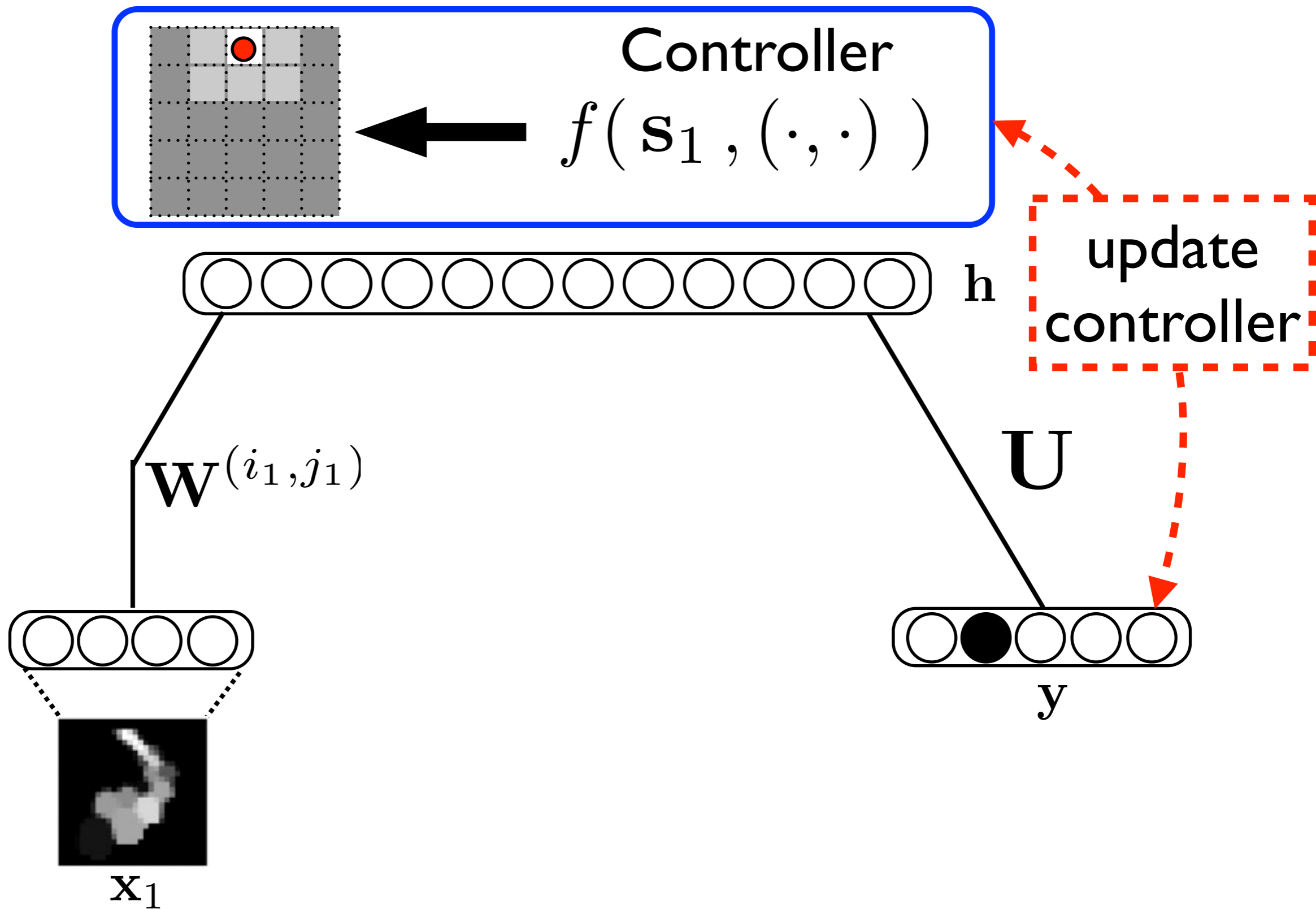
# Putting it all together



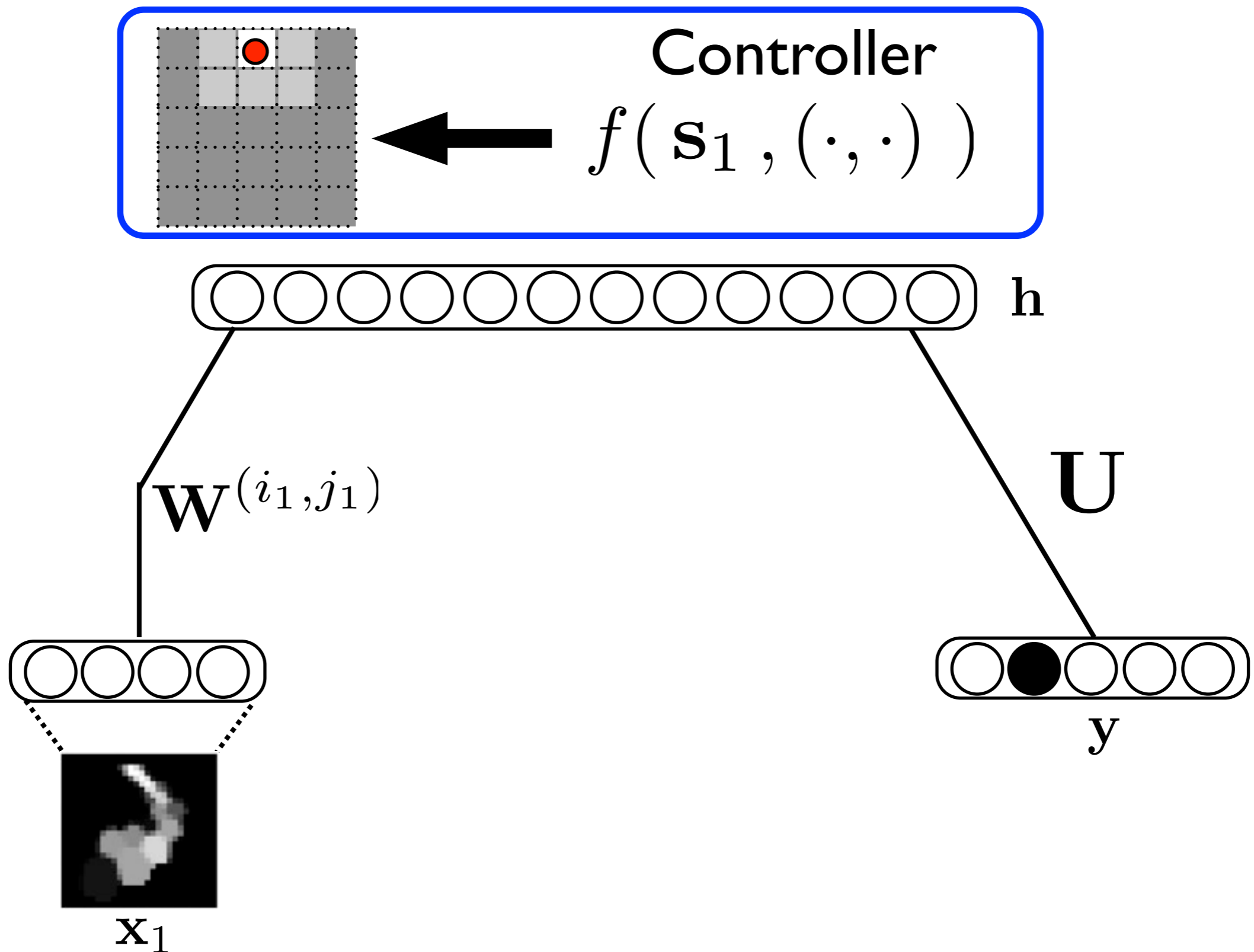
# Putting it all together



# Putting it all together

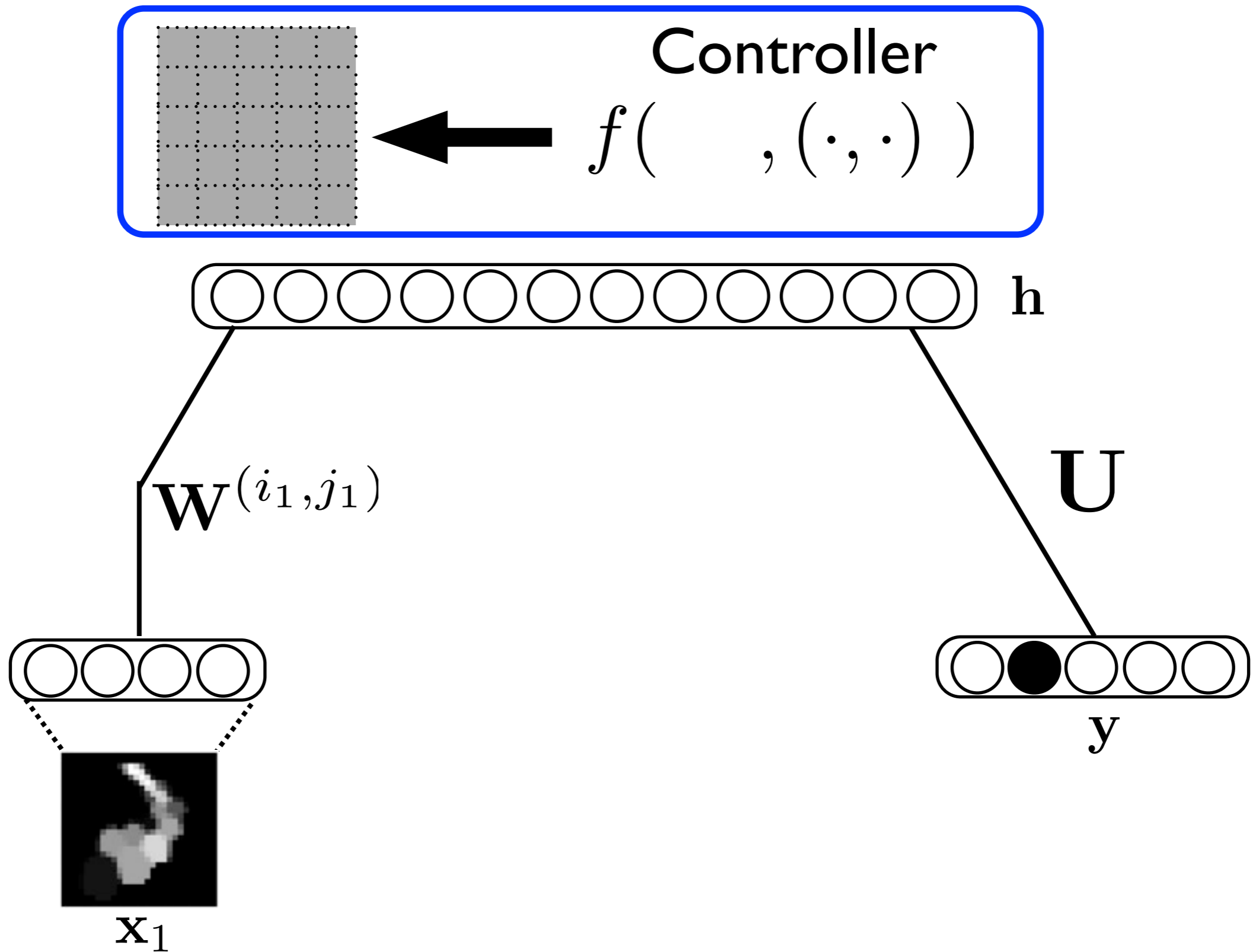


# Putting it all together

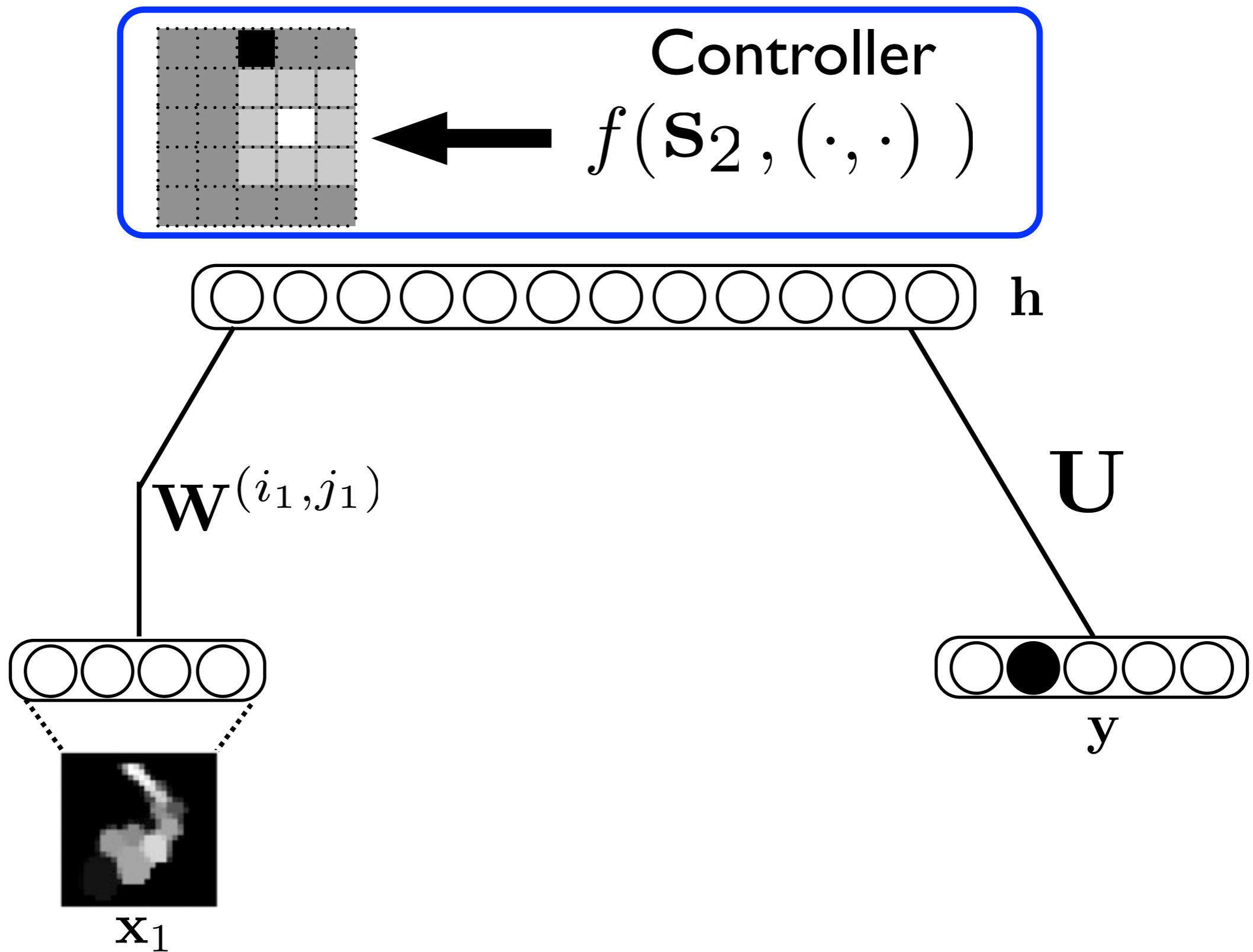




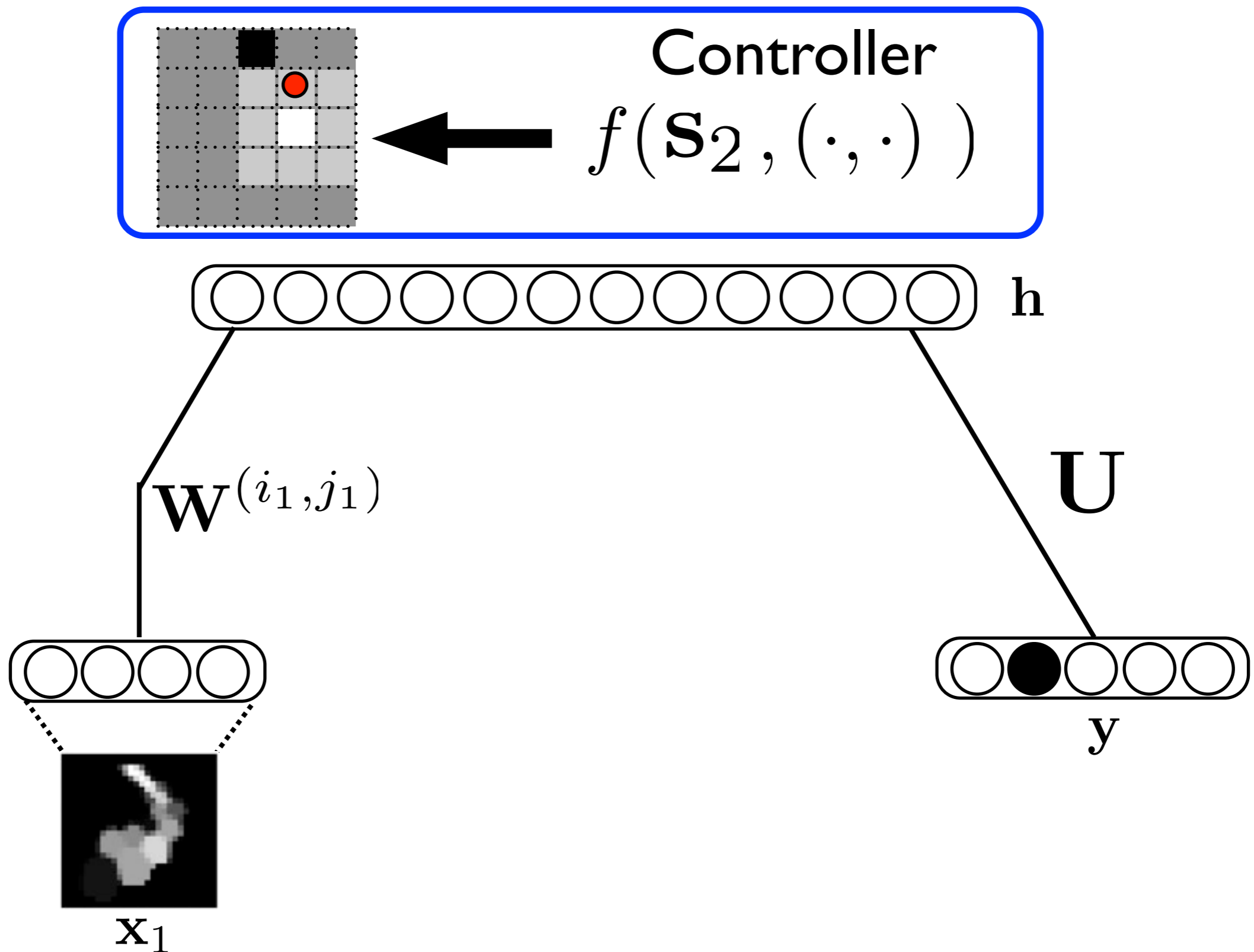
# Putting it all together



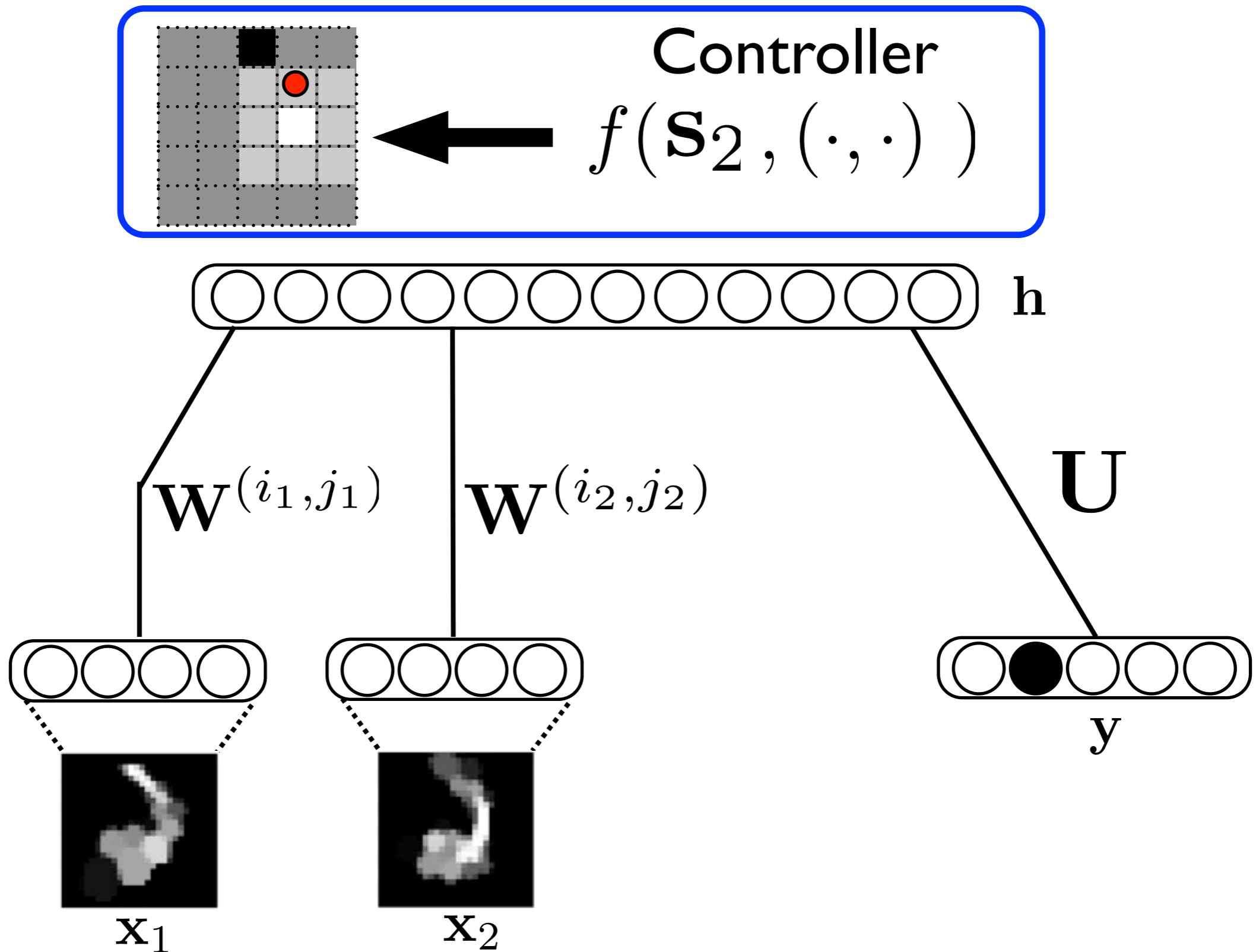
# Putting it all together



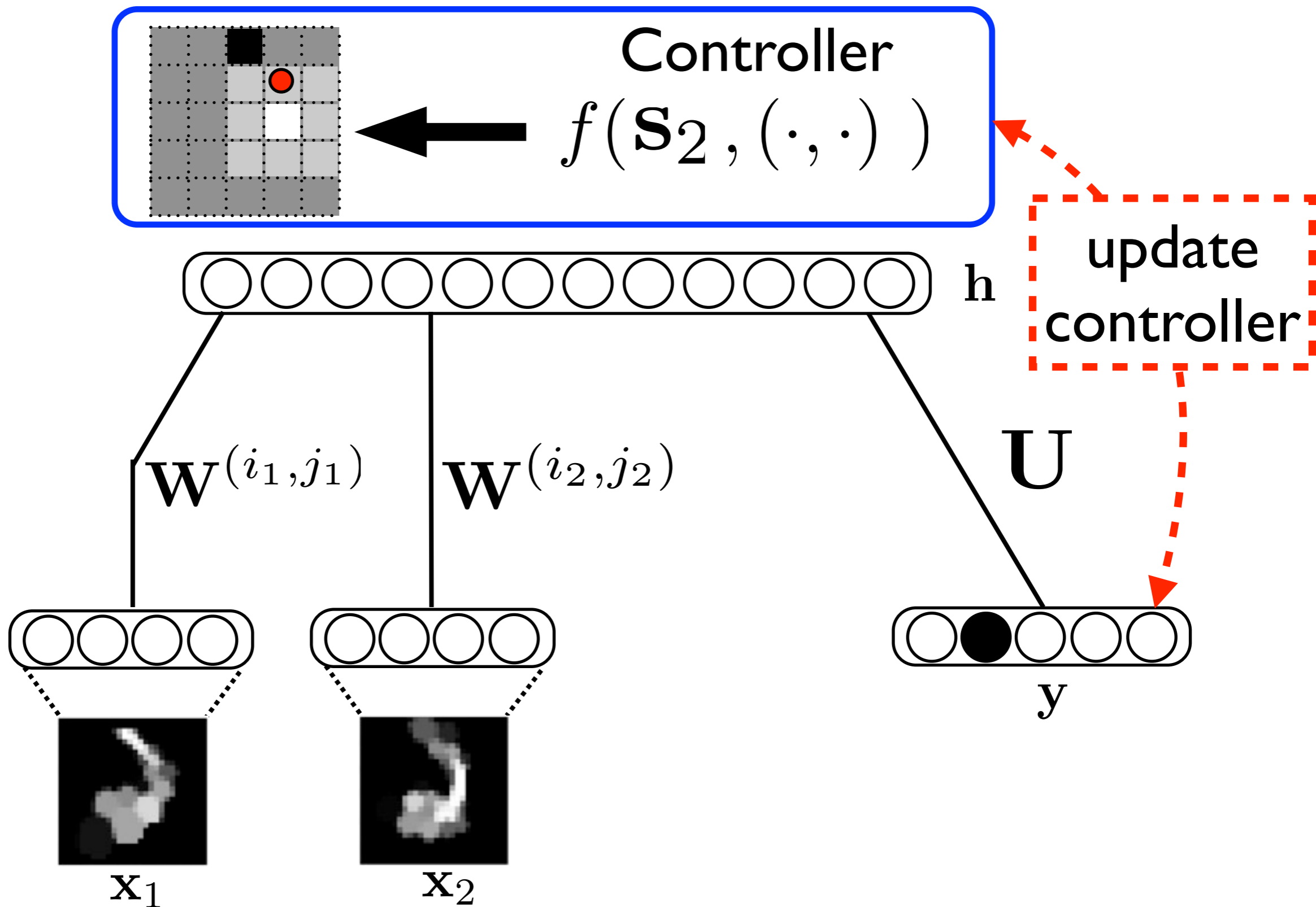
# Putting it all together



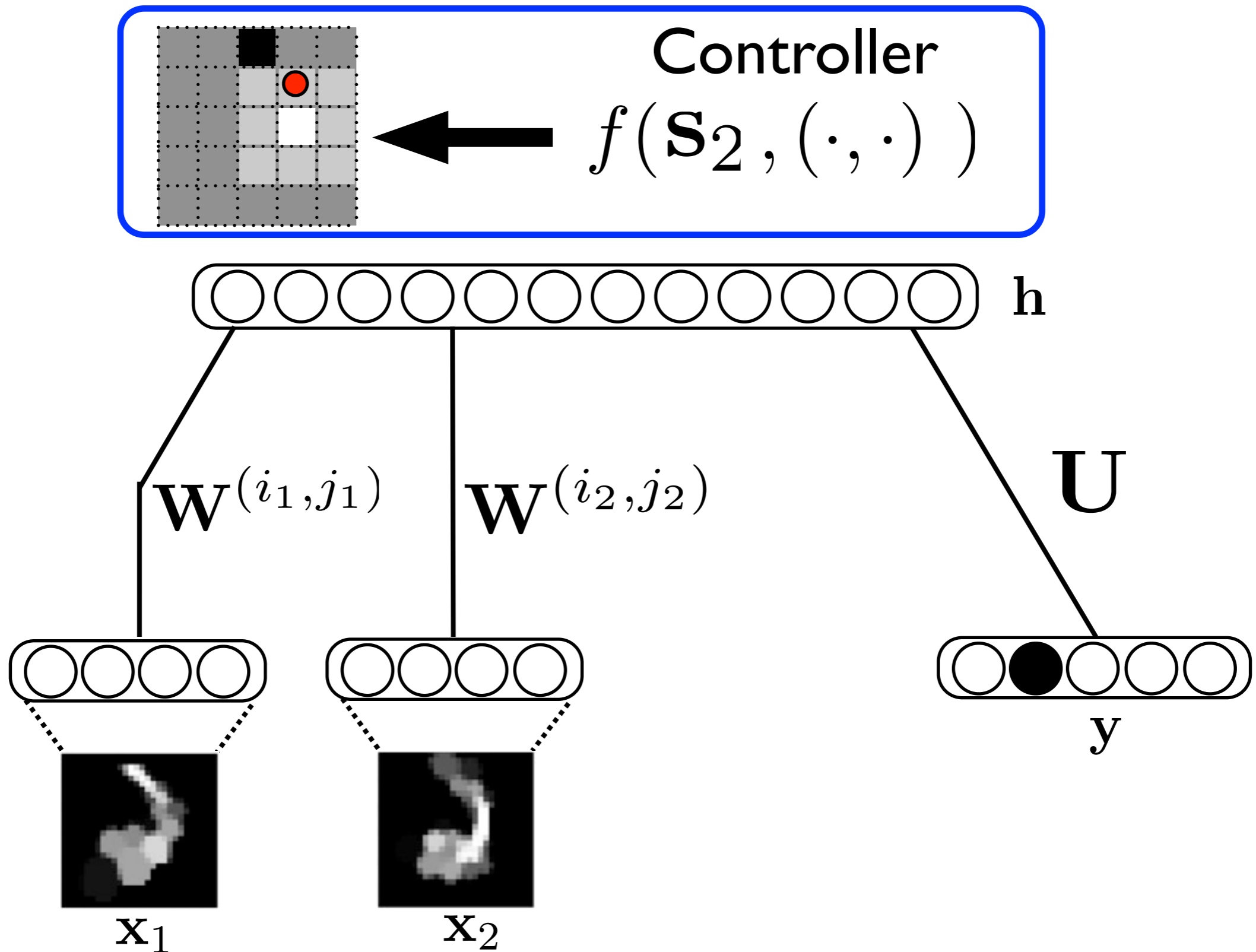
# Putting it all together



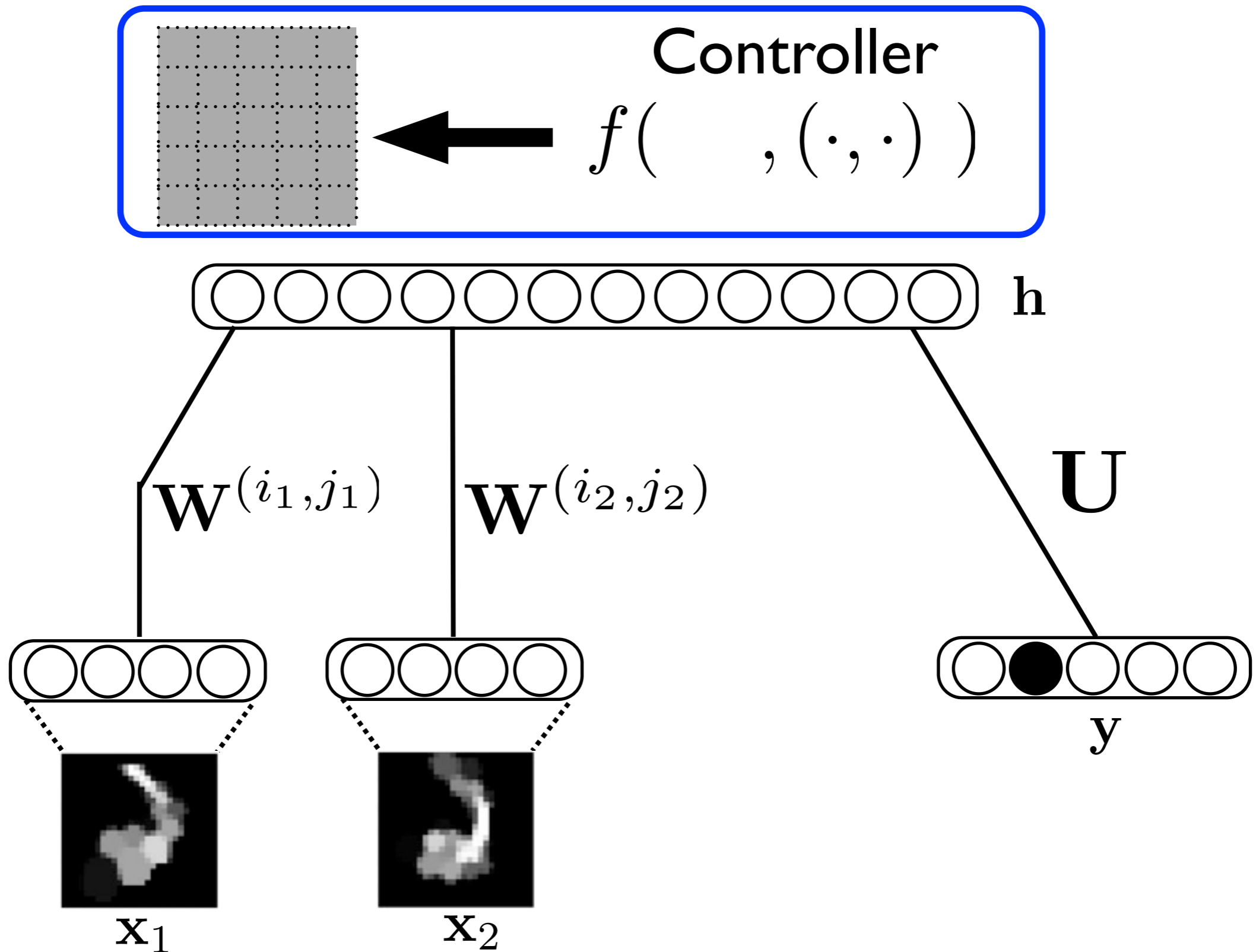
# Putting it all together



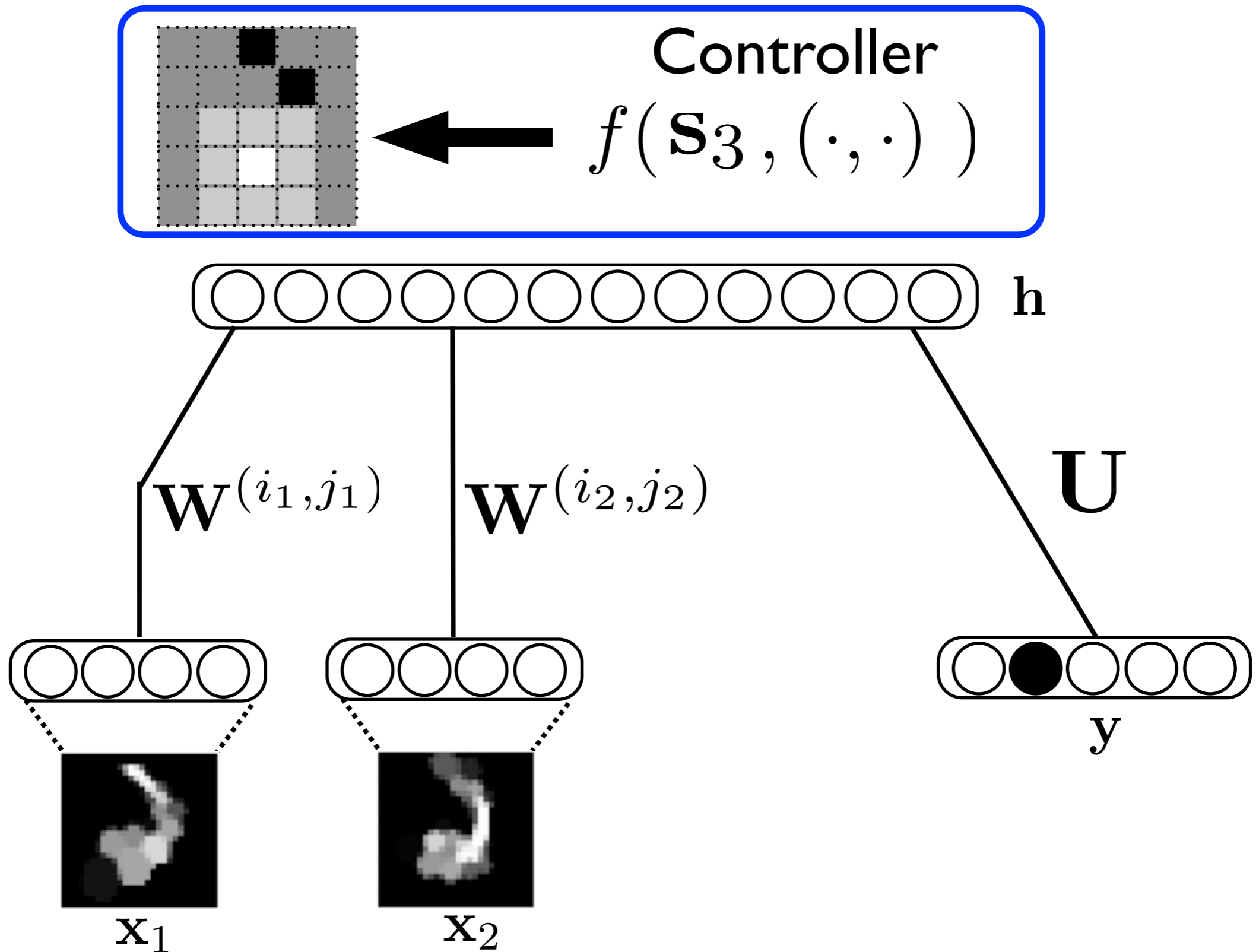
# Putting it all together



# Putting it all together

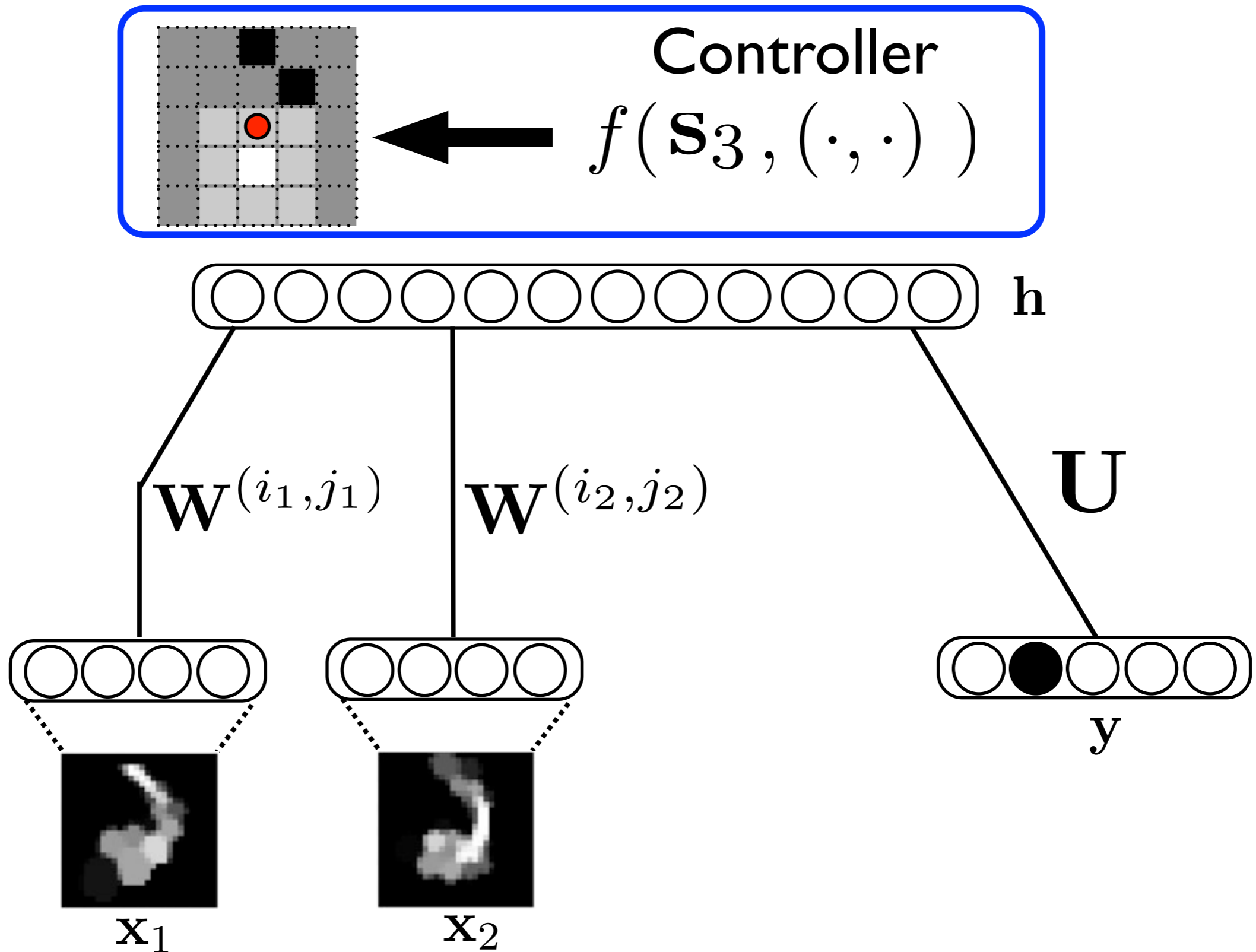


# Putting it all together

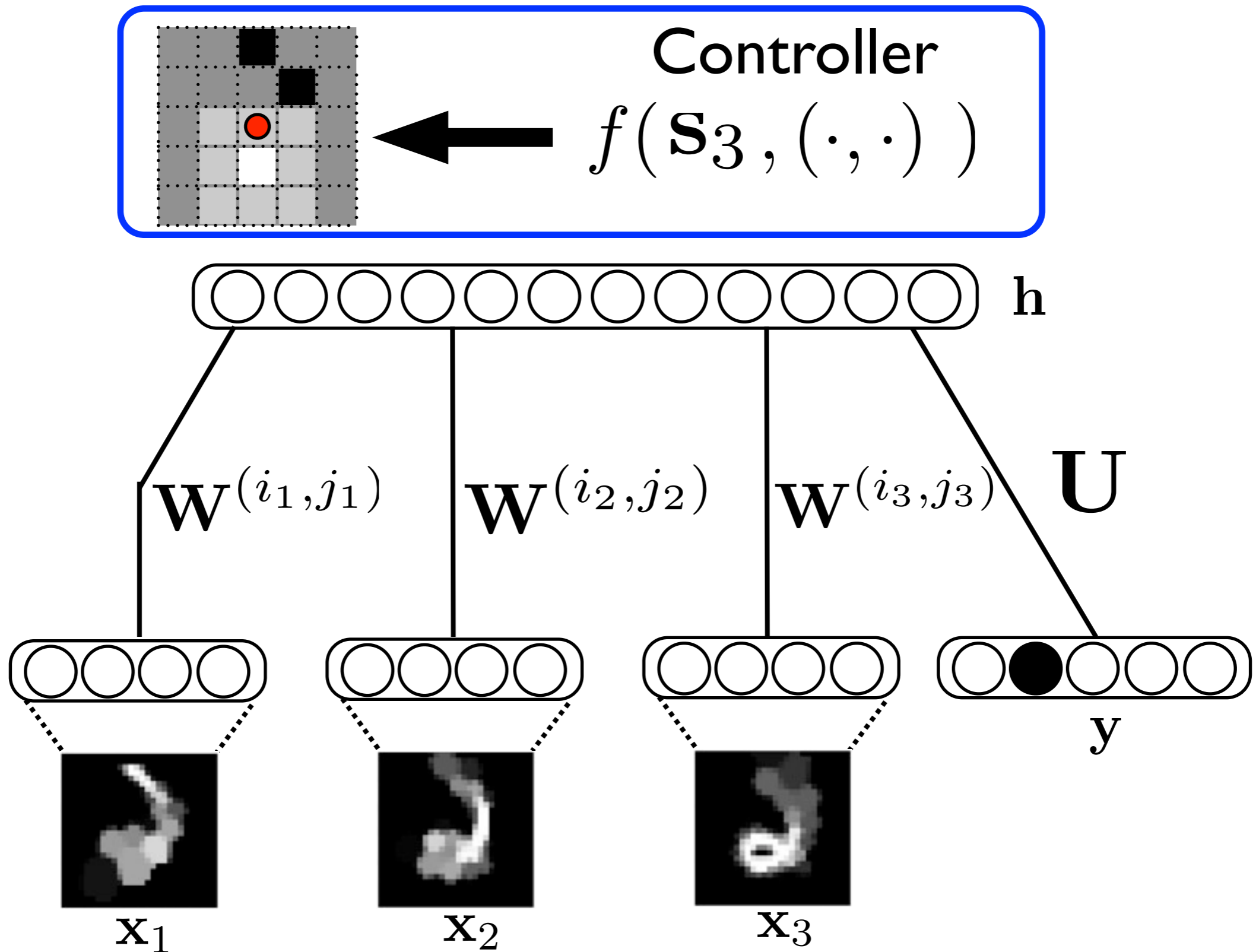




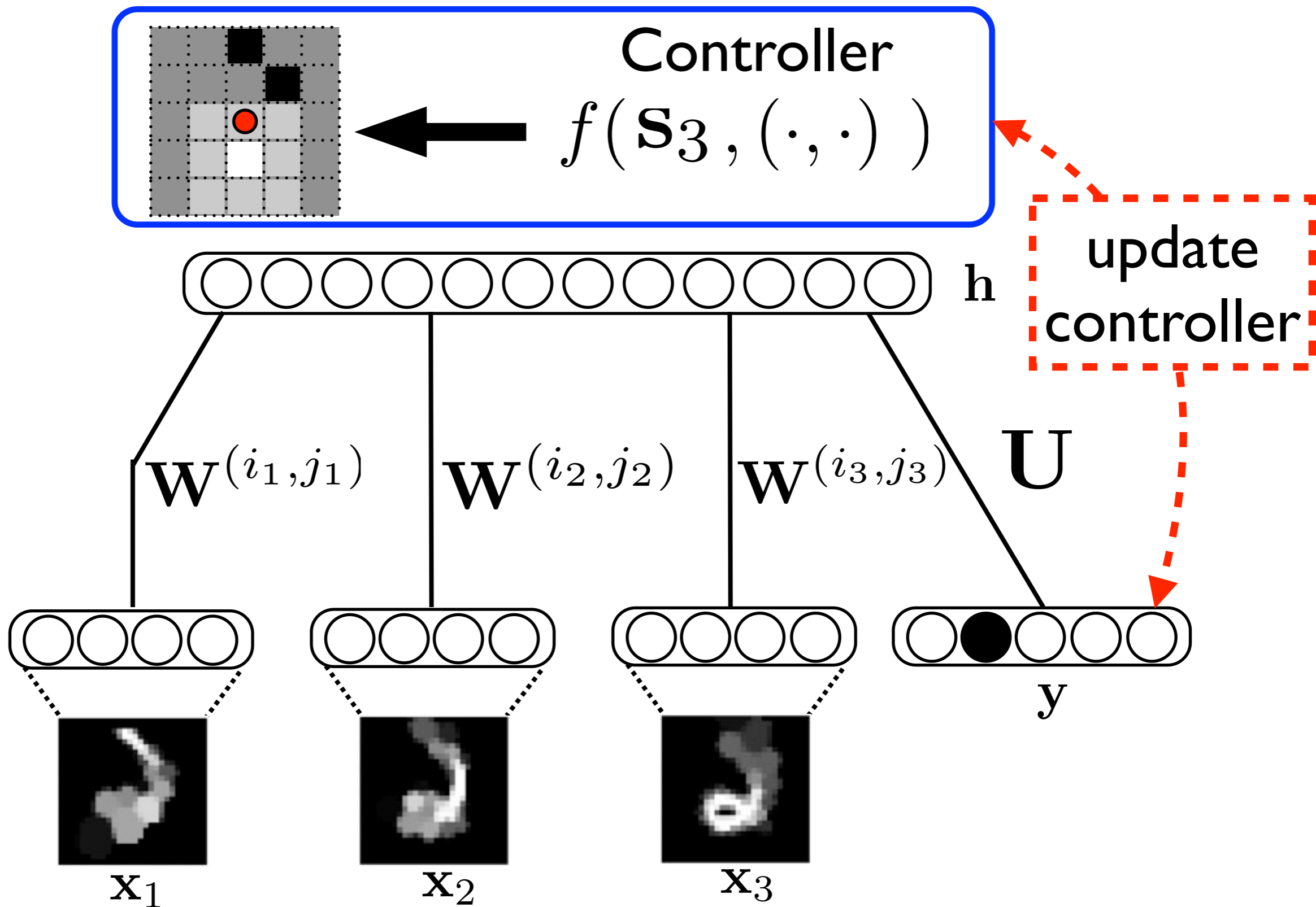
# Putting it all together



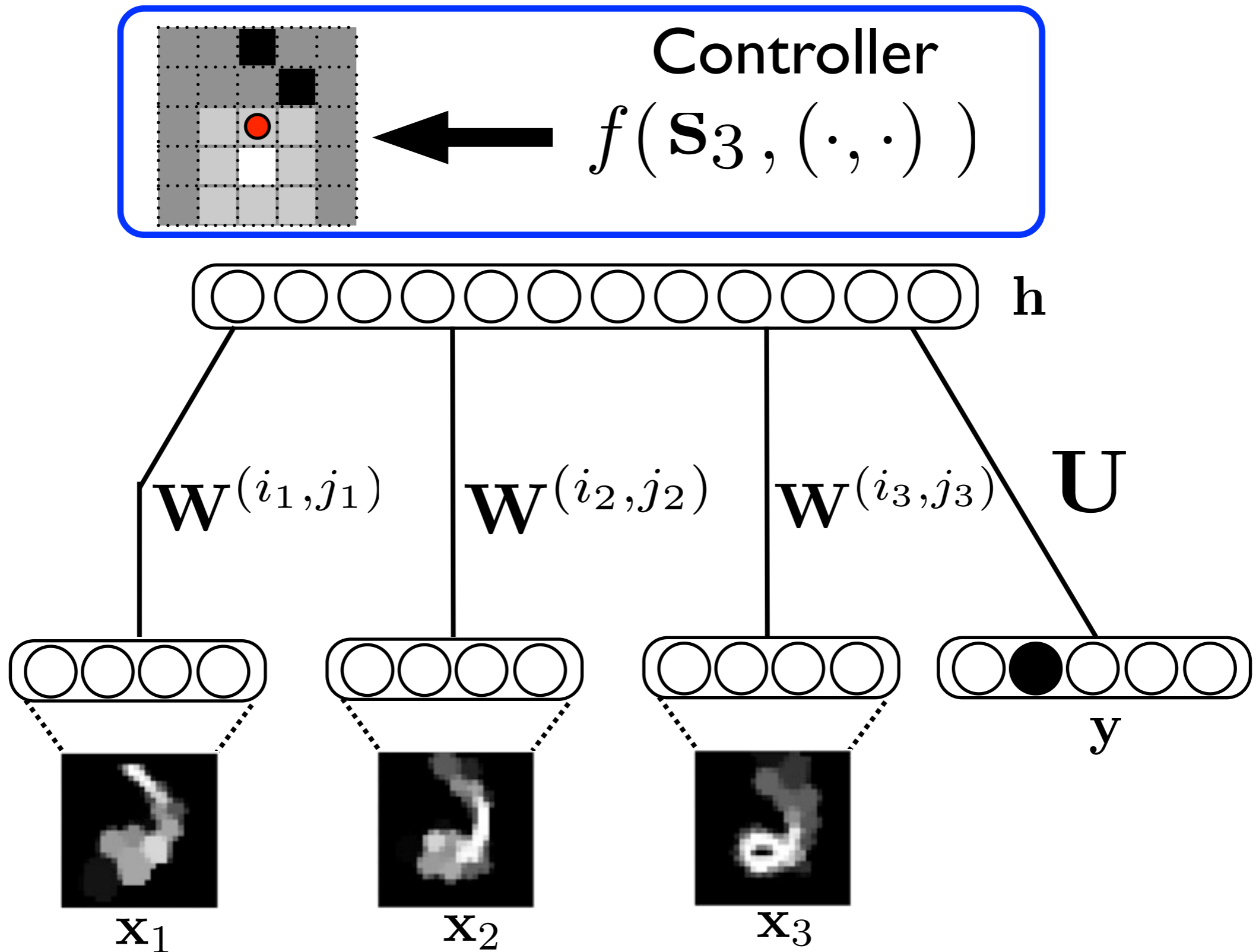
# Putting it all together



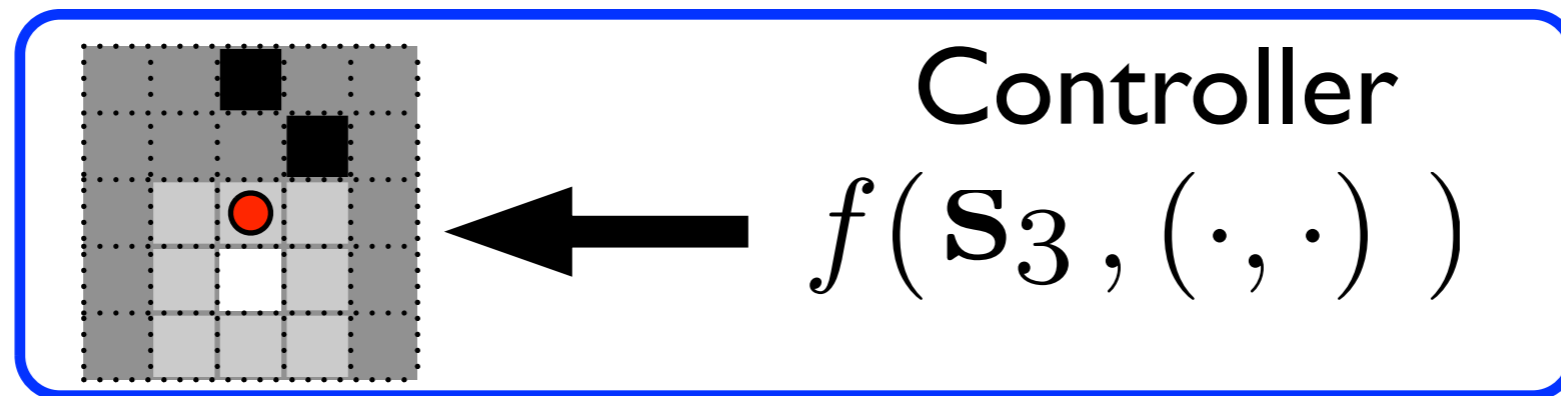
# Putting it all together



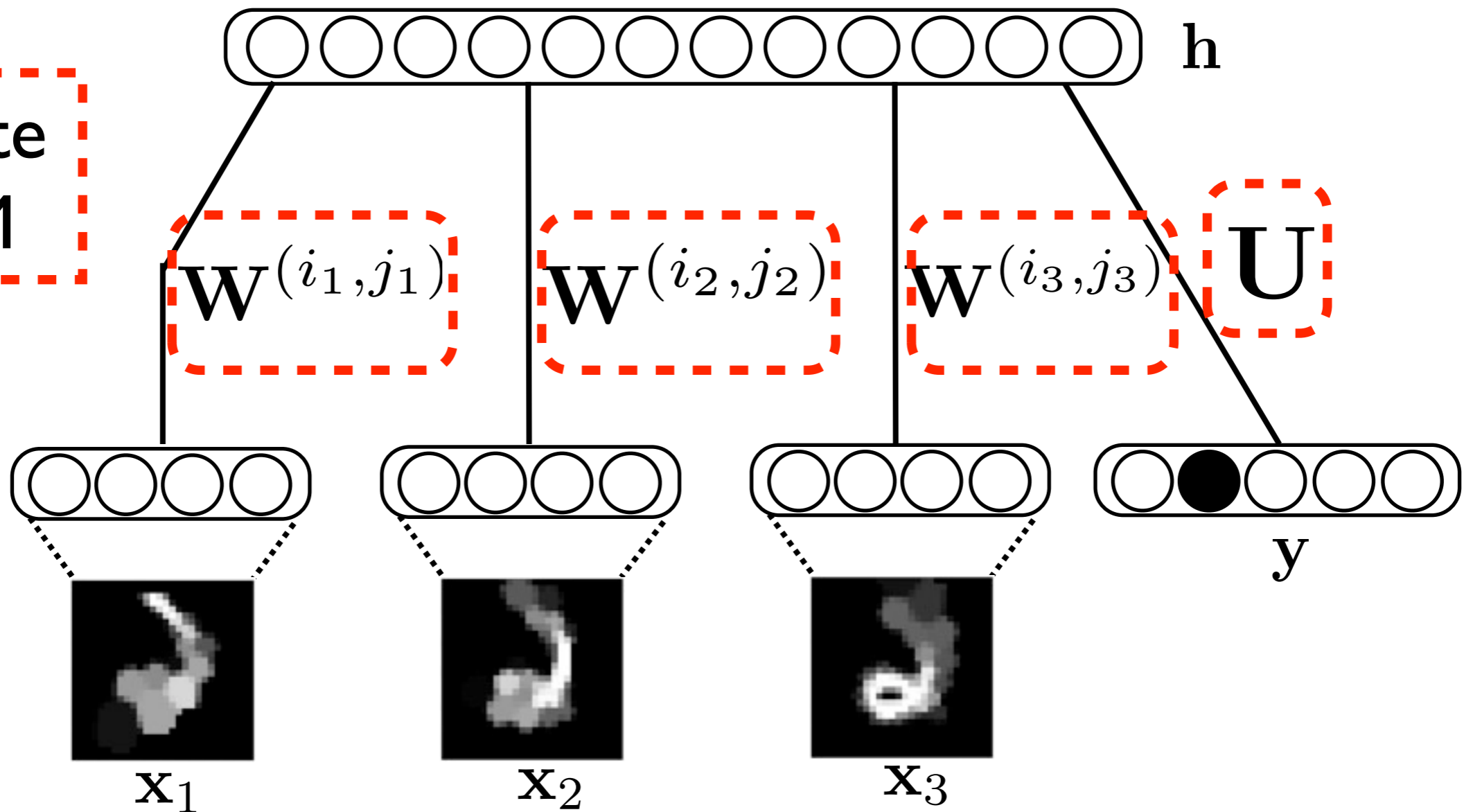
# Putting it all together



# Putting it all together



update  
RBM



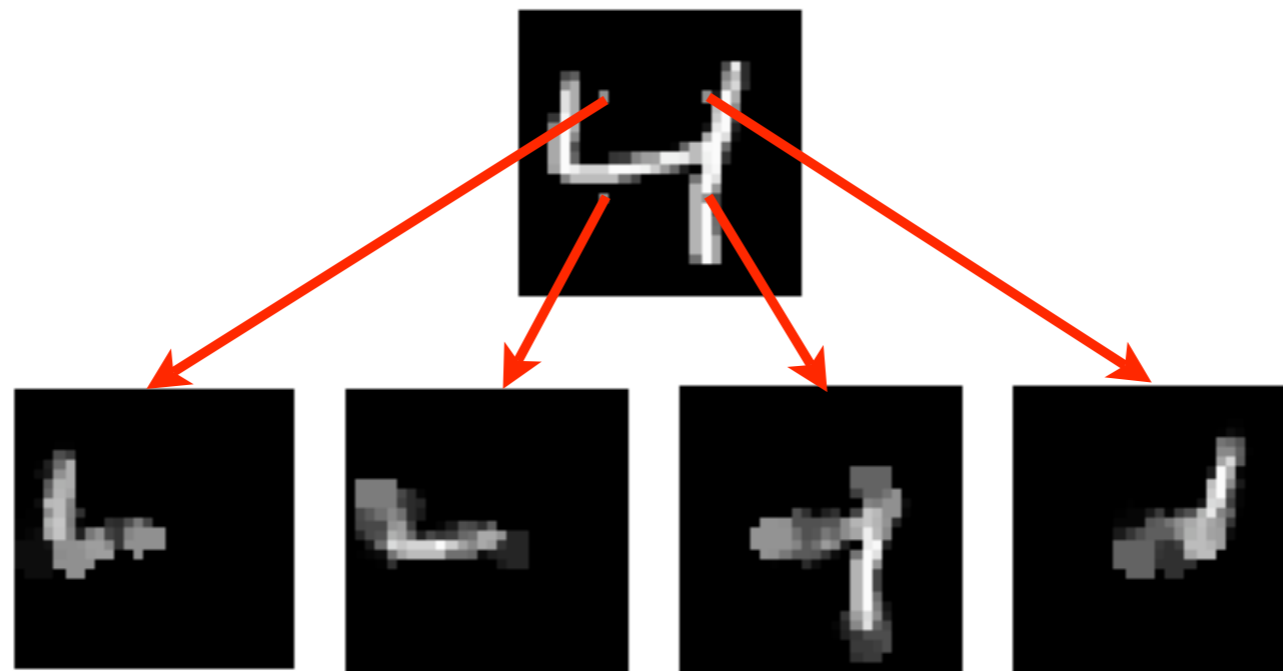
# Related work

- Alpaydin (NIPS 1996):
  - ★ neural net accumulating fixations
  - ★ based on a fixed saliency map
- Kanan and Cottrell (CVPR 2010):
  - ★ learned saliency map
  - ★ non-parametric nearest neighbor recognition
- Our work:
  - ★ joint training of a recognition component (RBM) and an attentional component (controller)
  - ★ explicitly avoids looking everywhere (unlike saliency maps on high resolution image)

# Experiments

- Evaluating the Multi-fixation RBM
- Evaluating the controller
- Evaluating the whole system

# Experiment I: MNIST (subset) with 4 fixations

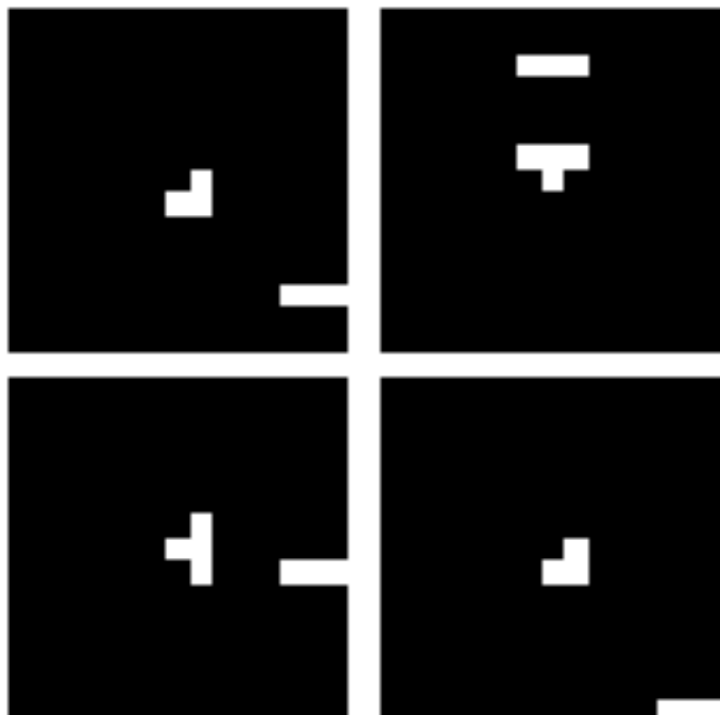


Model	Error
NNet+RBM [22]	3.17% ( $\pm 0.15$ )
SVM [21]	3.03% ( $\pm 0.15$ )
Multi-fixation RBM (hybrid)	3.20% ( $\pm 0.15$ )
Multi-fixation RBM (hybrid-sequential)	2.76% ( $\pm 0.14$ )

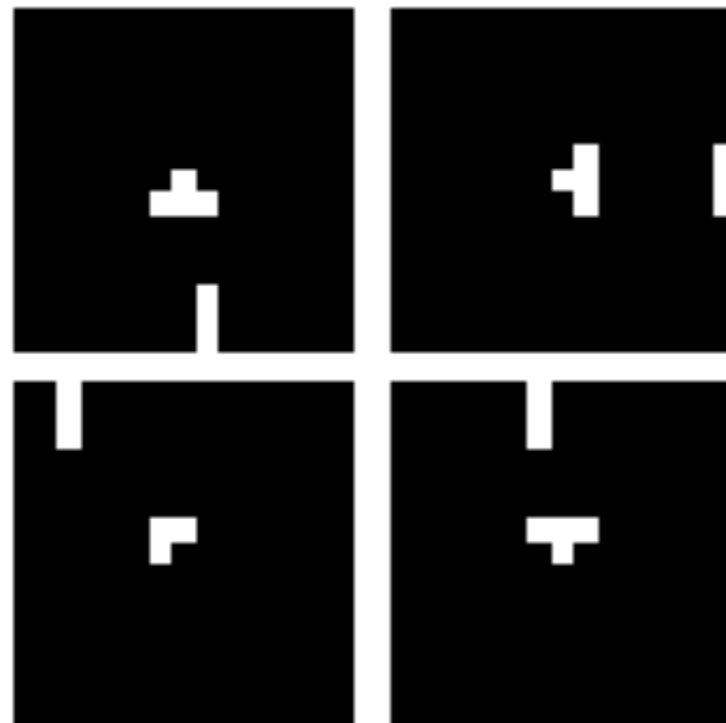


# Experiment 2: Synthetic dataset



Positive examples




Negative examples



Task

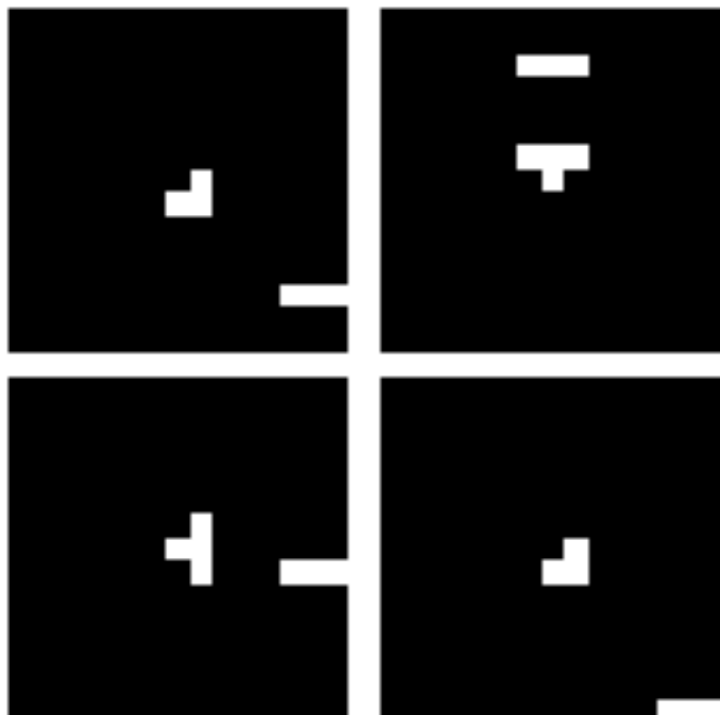
- Identify presence of horizontal (  ) or vertical (  ) bars
- Symbol at center says where the bar is

 = top left

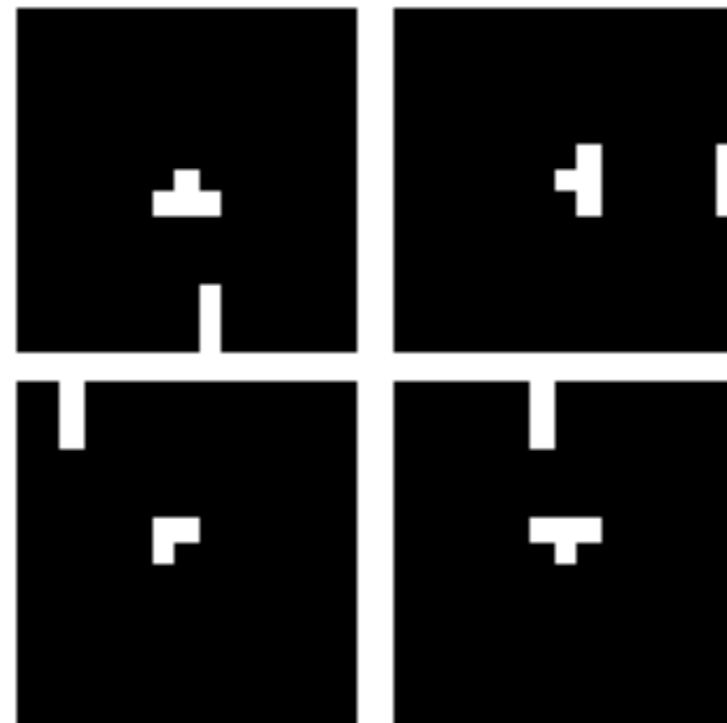
 = right

# Experiment 2: Synthetic dataset



Positive examples



Negative examples

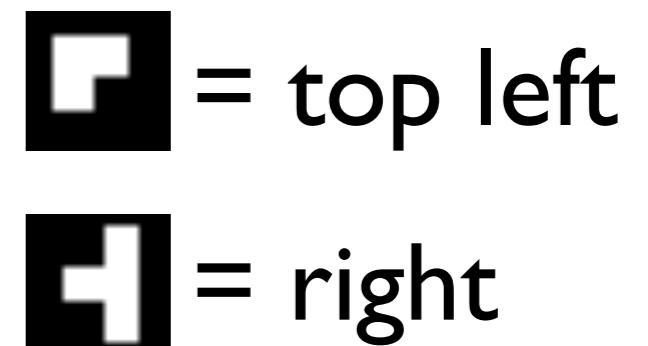


Task

- Identify presence of horizontal (  ) or vertical (  ) bars
- Symbol at center says where the bar is

## Results

1. Hybrid training solves this problem perfectly
2. Discriminative training fails (50%)

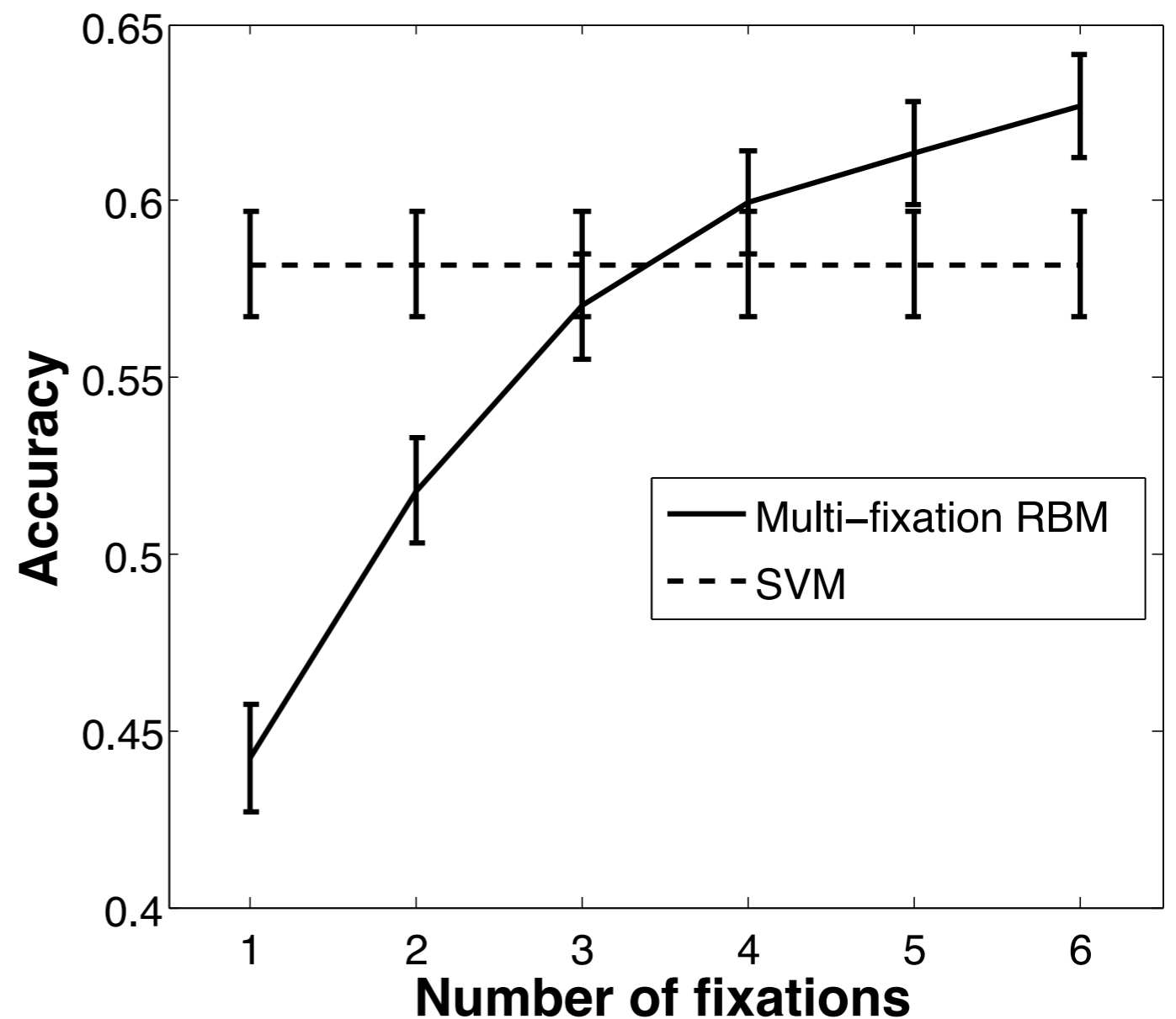


# Experiment 3: Facial expression recognition

## Examples

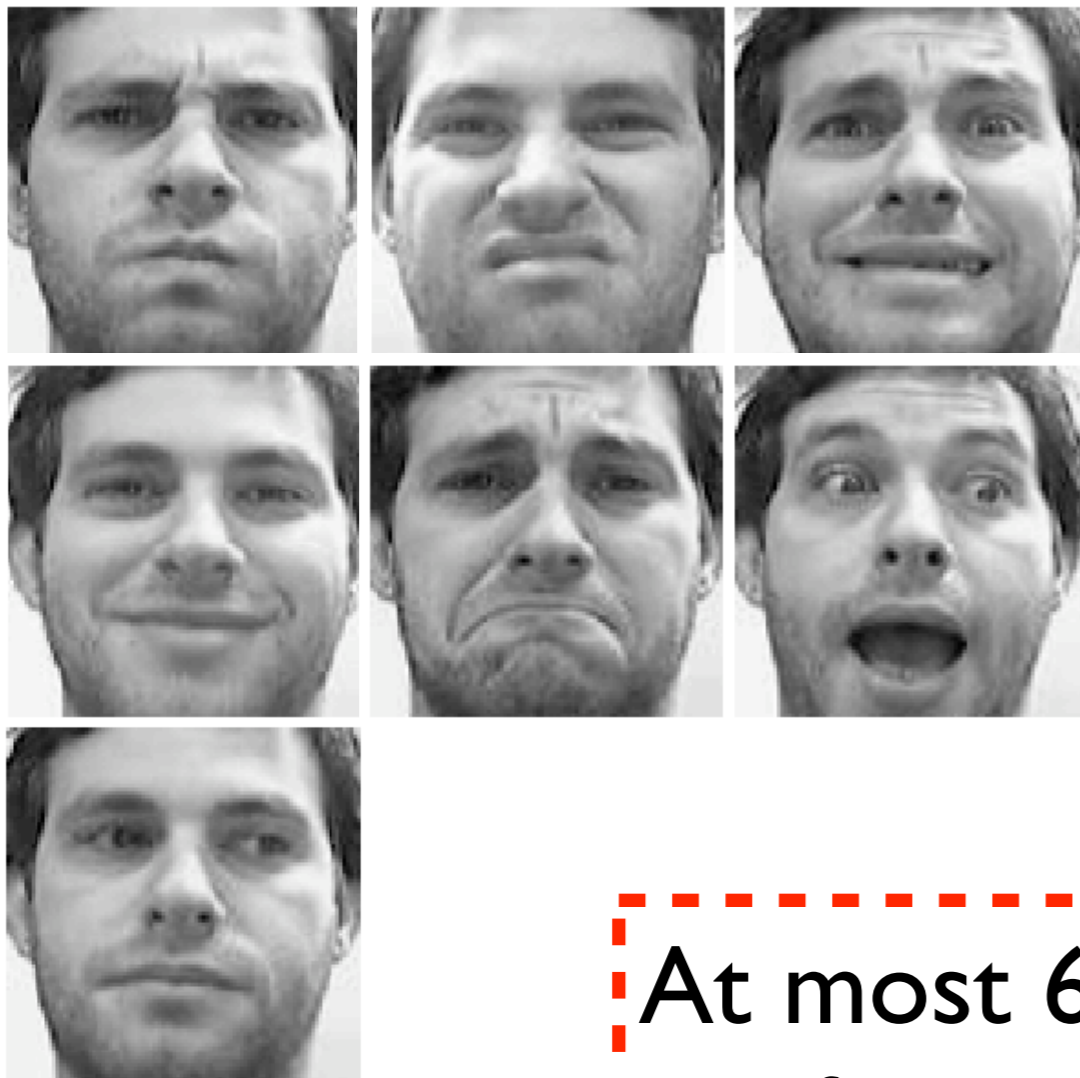


## Results

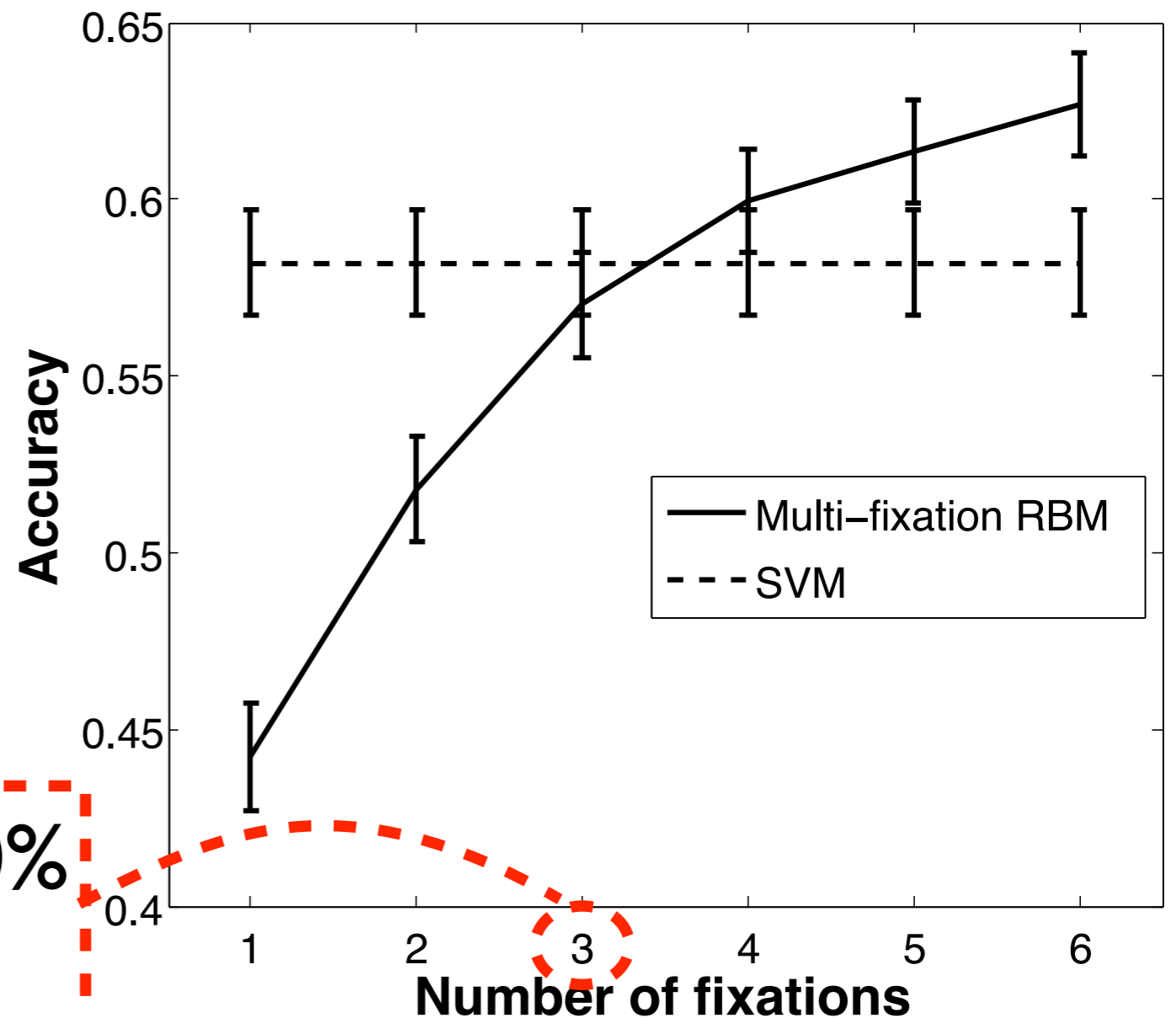


# Experiment 3: Facial expression recognition

Examples



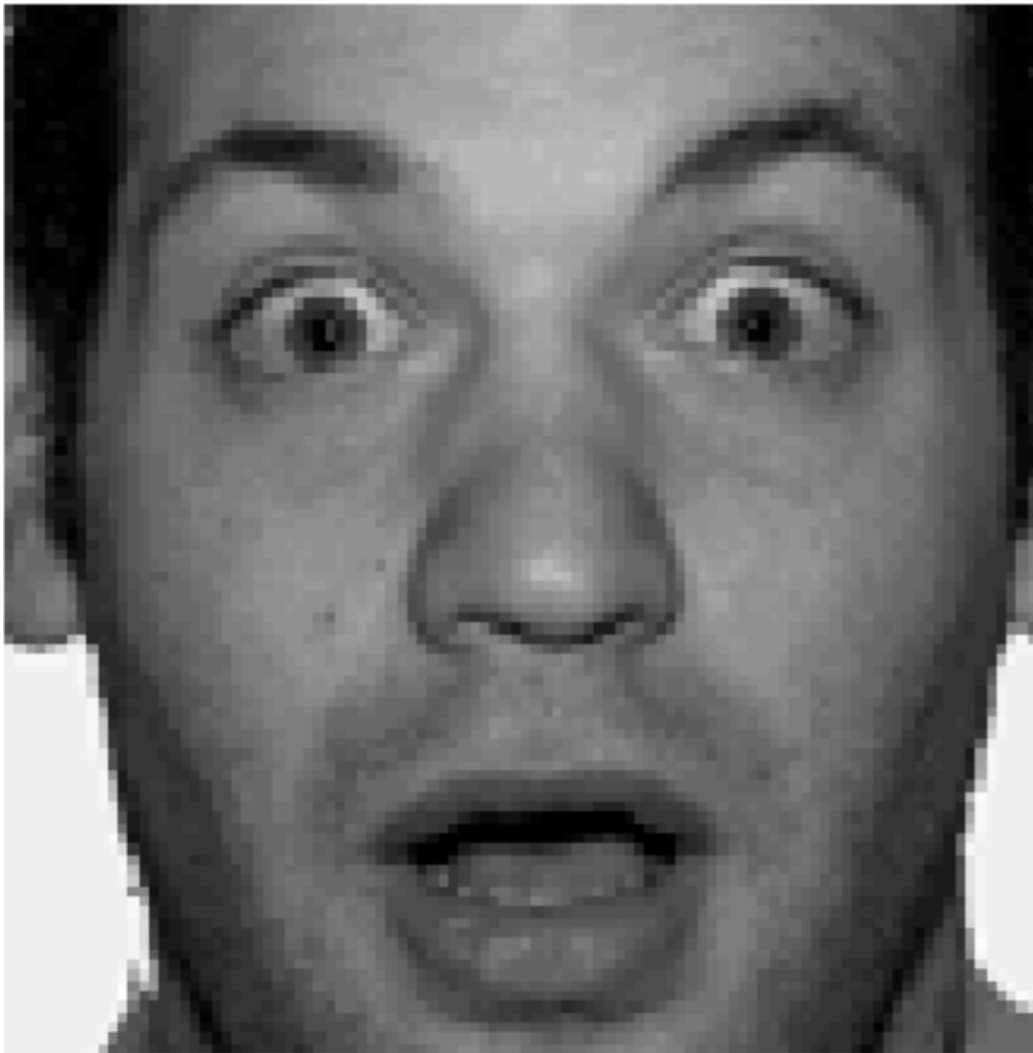
Results



At most 60%  
of image

# Experiment 3: Facial expression recognition

Full image + sequence of fixations



Individual glimpses



# Conclusion

- Investigated a model for jointly learning a recognition and attentional component using a Boltzmann machine
- Future work:
  - ★ impact of retinal rep. on performance
  - ★ improvement to controller algorithm
  - ★ multitask learning

**Thank you!**