A Rational Decision-Making Framework for Inhibitory Control (Poster T7)

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Inhibitory Control

the ability to inhibit a prepotent response or modify a planned course of action according to behavioral context

• Psychiatric conditions

- drug abuse (Nigg et al., 2006)
- attention-deficit hyperactivity disorder (Alderston et al., 2007)
- obsessive compulsive disorder (Menzies et al., 2007)
- schizophrenia (Enticott et al., 2008)

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• Neurological diseases

- Parkinson's (Gauggel et al., 2004)
- Alzheimer's (Amieva et al., 2004)

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- Alzheimer's (Amieva et al., 2004)

• Pharmacology

 ADHD drug (atomoxetine, NE-reuptake inhibitor) improves stopping in animals, healthy volunteers, ADHD patients (Chamberlain et al., 2008)





Stop trial: correct (canceled response)



Stop trial: correct (canceled response)





Stop trial: error (non-canceled response)



Stop trial: error (non-canceled response)





Go trial (no stop signal): error (timeout)



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• Sensory uncertainty

- * go stimulus: left or right?
- * stop signal: present or absent?



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 - if go trial, would go response be too late?
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 - stop error penalty versus go response delay
- Learning (prior information)
- frequency of stop trials, stop signal onset, penalties





Possible actionsstop

• go



Possible actions
stop
go

• Sensory uncertainty

- * is that a yellow light or a yellow street lamp?
- * how far away is the intersection?





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Action uncertainty

- * if go, would light turn red before crossing intersection?
- * if stop, would the car stop in time?





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 - cops/tickets versus temporal delay
- Learning (prior information)
 - duration of yellow light, P(cop), \$ ticket

Outline

• Model: brain implements rational (optimal) computations

- ★ Sensory processing ⇔ Bayesian inference
- Action selection ⇔ optimal stochastic control
- Model captures a range of behavioral results
 - Classical results
 - Reward/motivation
 - Contextual effects, sequential effects
- Neural implementation
 - Race (drift-diffusion) model as neurally plausible approximation

Rational Behavior in Stop Signal Task

Fundamental decision: when (whether) to **go**?

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Sensory Processing

Bayesian inference

Track beliefs over time about

- go stimulus identity (L/R)
- *stop* signal presence (Y/N)
- frequency of stop trials

based on *noisy sensory inputs*

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Choose action given belief state

- *go* (L/R), or
- wait
- *stop* = *wait*, *wait*, *wait*...

based on *expected consequences*

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 $p_d^t \propto p_d^{t-1} f_d(x^t)$

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Simulation: Belief State Trajectories




• evidence accumulates for go stimulus identity (p_d)



- evidence accumulates for go stimulus identity (p_d)
- stop trial probability (p_s) rises (prior expectation) then falls









What is optimal? Define global cost function

 $L_{\pi} = c \langle \tau \rangle + c_s r P(\tau < D | s = 1) + (1 - r) P(\tau < D, \delta \neq d | s = 0) + (1 - r) P(\tau = D | s = 0)$

 τ : response times: stop trial δ : chosen targetd: true targetr: freq(stop trials)D: deadline



τ: response time	s: stop trial
δ: chosen target	d: true target
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Policy: $x_1, ..., x_t \Rightarrow \{left, right, wait\}$

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Objective: minimize expected (average) cost

$$\mathbf{b}^t = (p_d^t, p_s^t)$$

Bellman's Dynamic Programming Principle (Bellman, 1952)

Optimal policy: repeatedly choose best (least costly) action

$$V^{t}(\mathbf{b}^{t}) = \min \left(Q_{g}^{t}(\mathbf{b}^{t}), Q_{w}^{t}(\mathbf{b}^{t}) \right) \qquad \mathbf{b}^{t} = \left(p_{d}^{t}, p_{s}^{t} \right)$$

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Cost of Go action = time cost + stop error + go error (wrong response) $Q_g^t(\mathbf{b}^t) = ct + c_s p_s^t + (1 - p_s^t) \min(p_d^t, 1 - p_d^t)$

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Cost of wait action = expected future cost or deadline penalty

$$Q_w^t(\mathbf{b}^t) = \begin{cases} \langle V^{t+1}(\mathbf{b}^{t+1}|\mathbf{b}^t), & D > t+1 \\ c(t+1) + (1-p_s^t), & D = t+1 \end{cases}$$

Optimal Policy: Belief State \Rightarrow *Go* & *Wait* **Regions**

Policy: $x_1, ..., x_t \Rightarrow \{left, right, wait\}$



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Go & wait regions



Optimal Policy: Belief State \Rightarrow *Go* & *Wait* **Regions**

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Go & wait regions







- Q(go) decreases as go stimulus becomes less ambiguous
- Q(go) increases after stop-signal onset
- Q(go) dips below $Q(wait) \Rightarrow go$ response, otherwise wait

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- non-canceled SE RT shorter than go RT
- Q(go) needs to dip below Q(wait) early enough to elicit response





- Longer stop signal delay results in more errors
- More likely Q(go) has already dipped below Q(wait)

Reward/Motivation \Rightarrow **Stopping Behavior**



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Race model as approximation to optimal decision-making



Stimulus Statistics \Rightarrow **Stopping Behavior**



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Stimulus Statistics ⇒ **Stopping Behavior**



Immediate Context \Rightarrow **Stopping Behavior**



Immediate Context ⇒ **Stopping Behavior**

- Data: dependence on trial history
 - faster RT after go trials
 - slower after stop trials


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- Data: dependence on trial history
 - faster RT after go trials
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• Model: estimating P(stop)



Immediate Context ⇒ **Stopping Behavior**



Immediate Context \Rightarrow **Stopping Behavior**

3+

3+

2

2

- Data (from Emric et al., 2007) **Data: dependence on trial history** 350 ---- EF ----- KW ----- JB ----- SN ----- EL (ms) 250 faster RT after go trials slower after stop trials * 200 3+ 2 Go Trials Stop Trials Model **Model:** estimating P(stop) 36 * tracking $P(stop) \Rightarrow$ sequential effects 34 inter-subject variability due to * memory/learning rate (α)? 26 24 3+2 Stop Trials Go Trials
 - $P(r_k|\mathbf{s}_k) \propto P(s_k|r_k)((1-\alpha)P(r_{k-1}|\mathbf{s}_{k-1}) + \alpha P_0(r-k))$ $(\alpha = volatility = learning rate)$

Prediction: Go Difficulty => Stopping Behavior

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30% coherence



Prediction: Go Difficulty \Rightarrow **Stopping Behavior**

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5% coherence



Predictions: Go Difficulty Affects Stopping





- ↓ go RT
- ↑ stop errors
- ↓ **SSRT** (stopping latency)

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Contextual Effects ⇒ **Stopping Behavior** Race model Approximation to Optimal DM



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• Optimality framework for inhibitory control

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* sensory processing \Leftrightarrow Bayesian inference

* decision policy \Leftrightarrow optimal stochastic control

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- Model explains wide range of behavioral data
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 - prediction: go difficulty affects stopping behavior









- Yu Lab
 - Pradeep Shenoy
 - Joseph Schilz
 - * Crane H Huang, Jake Olson, Katherine Naimark, Jeremy Karnowski



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• Collaborators

 Chiang-shan Li & Jaime Ide, Martin Paulus, Veit Stuphorn, Birte Forstmann (U. Amsterdam)

Experimental Paradigm: Stop Signal Task



Go trial (no stop signal): correct



Experimental Paradigm: Stop Signal Task



Go trial (no stop signal): error (misidentified)



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Inhibitory Control: An Example



Inhibitory Control: An Example














Possible actions stop





Possible actions stop go





Possible actions

- stop
- go
- speed up!

- Neural implementation/approximation of optimal DM?
 - interactive race model (Boucher et al, 2007):
 fixation/movement neurons in FEF & SC
 - * theory: other (neural) approximation of optimal DM?
 - * experiments: fMRI (Li & Ide @ Yale), EEG (Makeig @ UCSD)

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 - ★ temporal expectancies ⇒ stopping errors & SSRt

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 - ★ temporal expectancies ⇒ stopping errors & SSRt
- Population with impaired inhibitory control
 - depressives, stimulant users -- differentiate underlying cause





• *Stop* trials induce *slowing* of *Go* RT



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- Higher coherence (easier) induces faster Go response



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- Higher coherence (easier) induces faster Go response
- 100% coherence similar to standard symbol discrimination

A. Model



A. Model



A. Model



A. Model



- Later stop signal \Rightarrow more stop errors
- More difficult *go* task \Rightarrow fewer stop errors
- Consequence of slower *go* RT

A. Model



A. Model



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- **SSRT** increase \Rightarrow **go** & **stop** processes fundamentally inter-related

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Race Model



(Logan & Cowan, 1984)

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SSRT As a Measure of Inhibitory Control

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- SSRT slower in populations with inhibitory deficits
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- Behavioral SSRT linked closely to neural activity
 - Neural response in frontal eye field, superior colliculus (Hanes et al., 1996, Pare & Hanes, 2003)
 - * Suggests a *neural mechanism* underlying stopping behavior

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 - motivational factors (Leotti & Wager, 2009)
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 - * go response difficulty (Logan et al, JEP:HPP, 1984)

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- Single parameter (SSRT) cannot explain full range of data

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- Design: *random-dot motion task* -- coherence controls difficulty
Experiment: Vary Go Discrimination Difficulty



```
30% coh
```



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Race -- Diffusion Model



(Logan & Cowan, 1984)

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(Logan & Cowan, 1984)

(e.g. Verbruggen & Logan, 2007)

Rational Framework for Stop Signal Task

Fundamental decision: when (whether) to go?

Reasons to go fast

sensory

• go discrimination easy

prior knowledge

• stop signal rare

costs

- time cost high
- deadline penalty large
- stop error penalty small

Reasons to go slow

sensory

• go discrimination difficult

prior knowledge

• stop signal frequent

costs

- time cost low
- deadline penalty small
- stop error penalty large

Decision Policy: Go & Wait Regions of Belief State **Simulation Results**

20 SS SE GO 15 P(d) counts 10 5 0 0.25 0.5 0.75 P(s)

Time = 20 steps

Neural Coding (FEF) of Instantaneous Action Value?

D





Neural Coding (FEF) of Instantaneous Action Value?



• FEF: fixation neurons (A) and movement neurons (C) diverge around SSRT between go and successfully stopped trials

Neural Coding (FEF) of Instantaneous Action Value?



- FEF: fixation neurons (A) and movement neurons (C) diverge around SSRT between go and successfully stopped trials
- Model: trajectories of stop/go action values mimic neural activity (B,D)

The Race Model of Stopping

- A race between independent *go* and *stop* processes (Logan & Cowan, 1984)
- Winner determines trial outcome
- Stopping latency (SSRT) not directly observable
- SSRT estimated from go RT and stopping errors



Rational Agent: Perception

Ex 1: visual illusions & ideal observer



Rational Agent: Perception

Ex 1: visual illusions & ideal observer



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Ex 1: visual illusions & ideal observer



visual percept











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Stop trial? $p_{s}^{t} = p_{z}^{t} + P\{\text{stop signal in future}\}$

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R present P(stop)P(go)Time (ms) Time (ms)

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Ex: 2AFC motion discrimination

(from Roitman & Shadlen, 2002)



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30% coh



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5% coh



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Speed

VS.



• Slow response \Rightarrow fewer errors, higher opportunity cost



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- What is optimal tradeoff? What computations involved?



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- Neural implementation?
Reward/Motivation \Rightarrow **Stopping Behavior**



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Race Model Approximation to Rational Decision-Making







Monitoring Process

Incorporate evidence iteratively (Bayes' Rule):

$$q_t \triangleq P(s=1|x_1,\ldots,x_t) = \frac{p(x_t|s=1)q_{t-1}}{p(x_t|x_1,\ldots,x_{t-1})}$$



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Decision Process

$$\pi(x_1,\ldots,x_t)\to\{0,1,\mathrm{cont}\}$$

- at time t, *wait* if $b < q_t < a$
- **go** & choose $\hat{s} = 1$ if $q_t > b$, choose $\hat{s} = 0$ if $q_t < a$



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- **go** & choose $\hat{s} = 1$ if $q_t > b$, choose $\hat{s} = 0$ if $q_t < a$
- model of both accuracy and RT



Rational DM Explains Behavioral Data



Rational DM Explains Neural Data

Saccade generation



(from Smith & Ratcliff, 2004)

Rational DM Explains Neural Data

LIP = neural SPRT integrator?

(Roitman & Shalden, 2002; Gold & Shadlen, 2004)

Saccade generation



(from Smith & Ratcliff, 2004)

LIP Response & Coherence

















