

Community detection in networks

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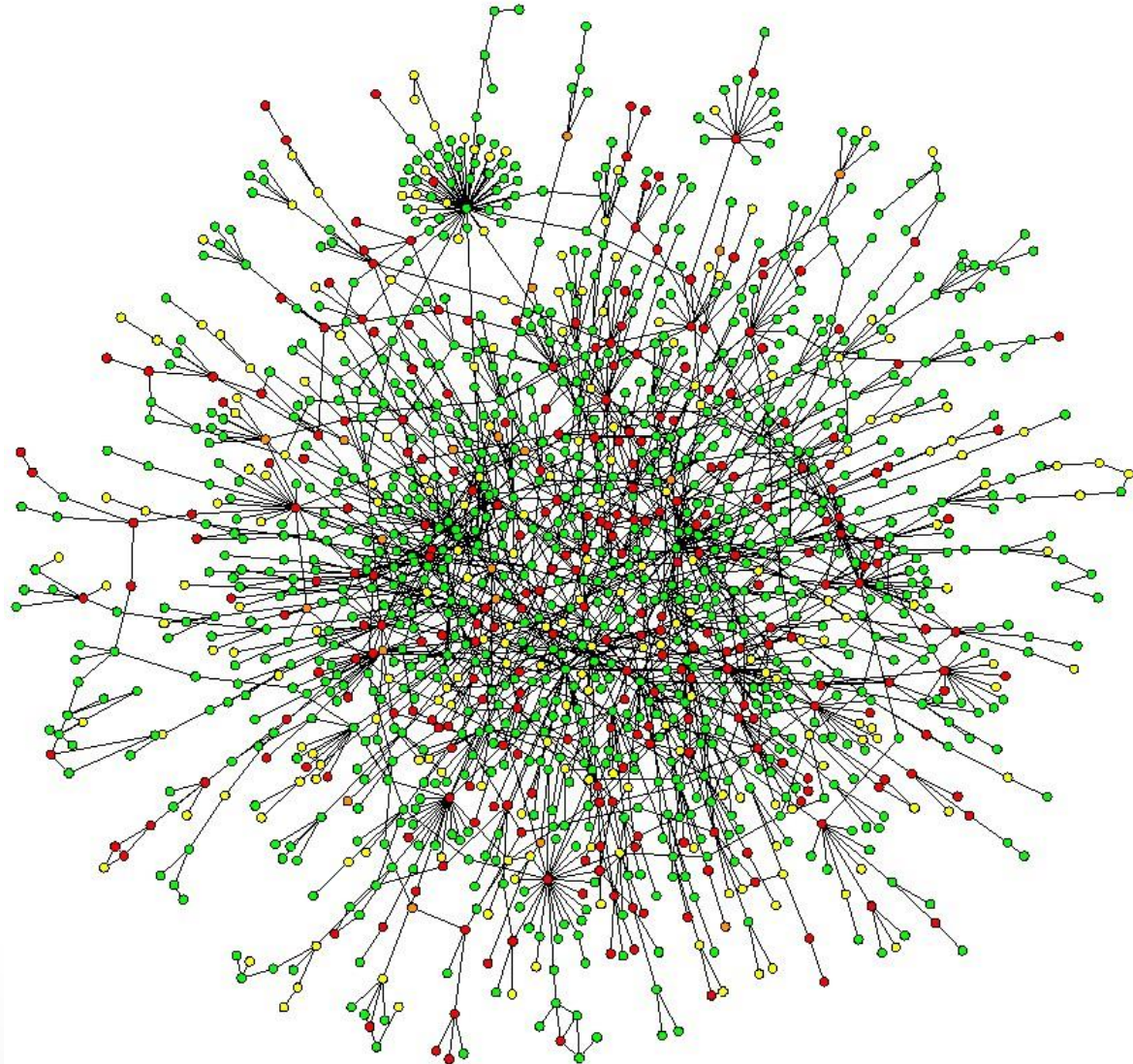
Outline

- 1) Introduction
- 2) Global optimization techniques: limits
- 3) Local techniques: OSLOM
- 4) Summary

Networks

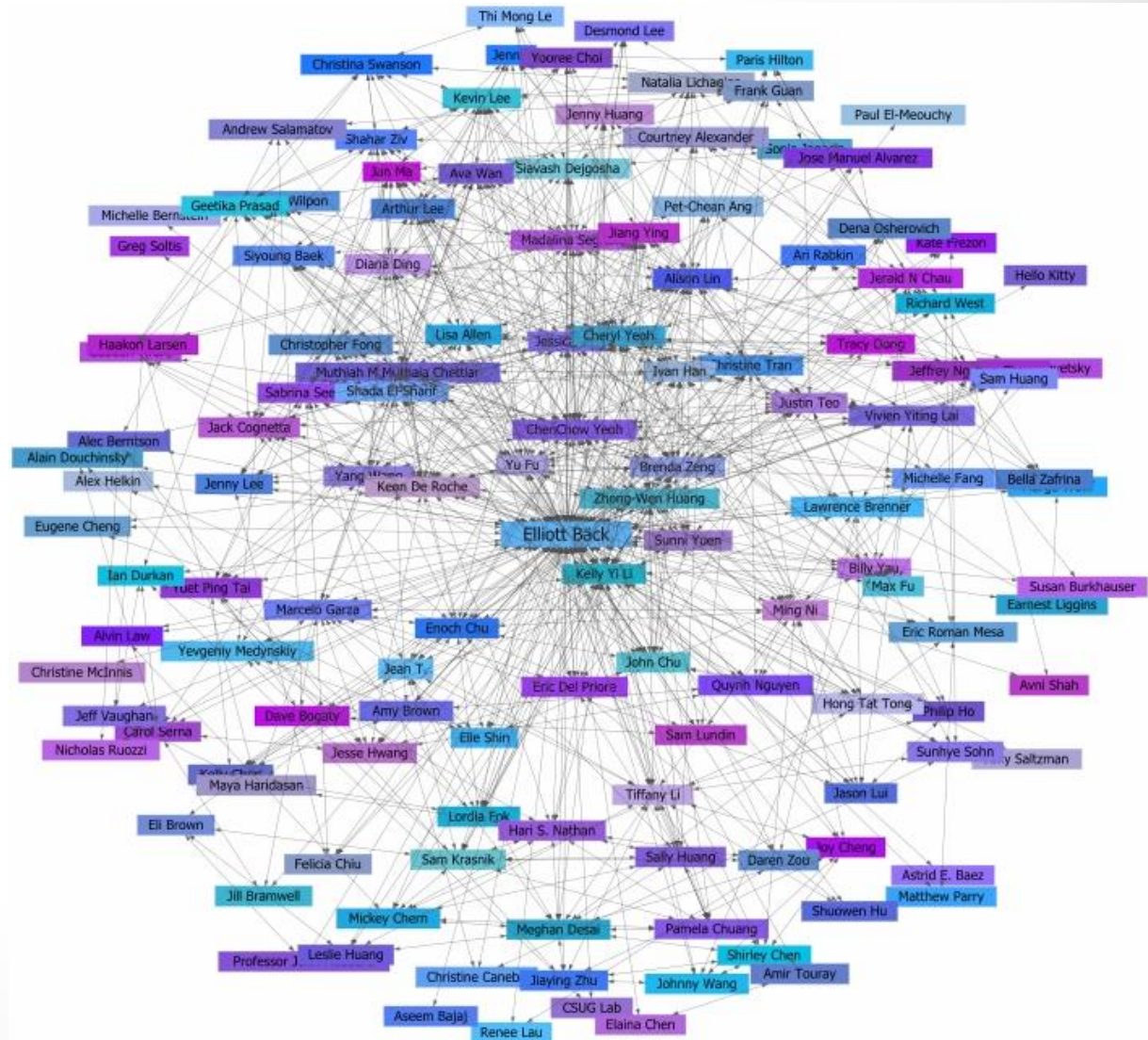
**Protein-protein
interaction networks**

**Network: simplest
representation of a
complex system**



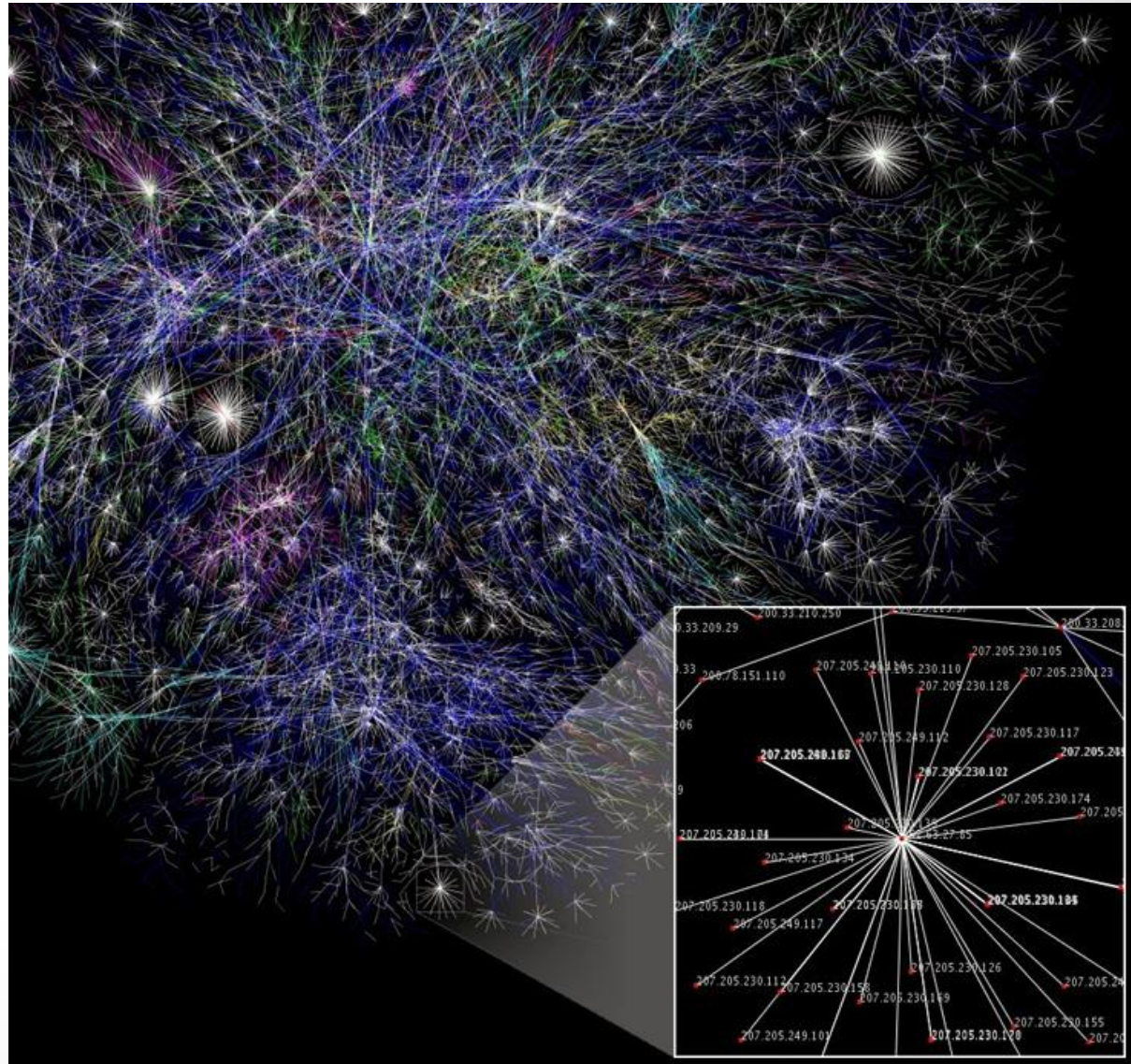
Networks

Social networks



Networks

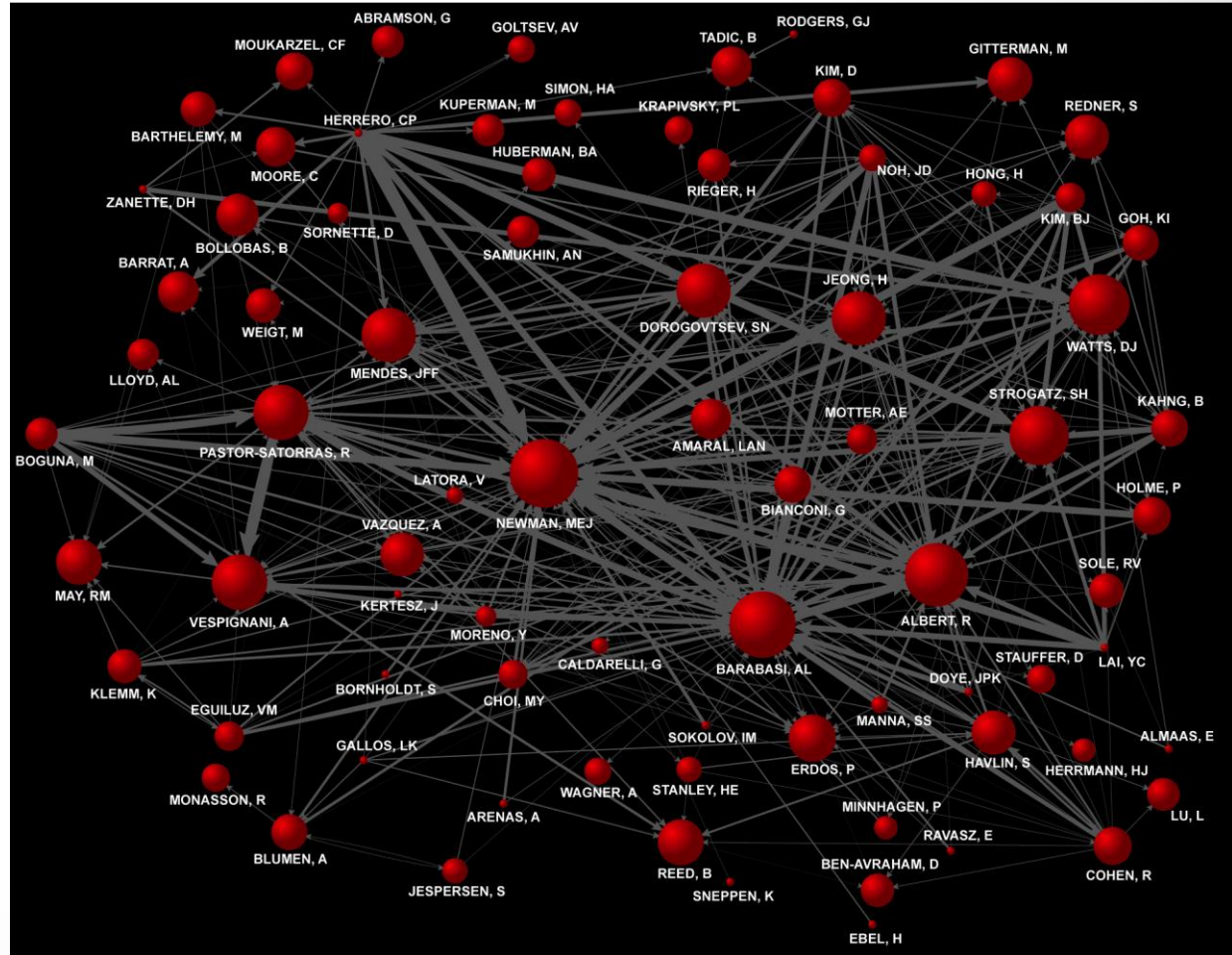
Internet



Networks

Citation networks

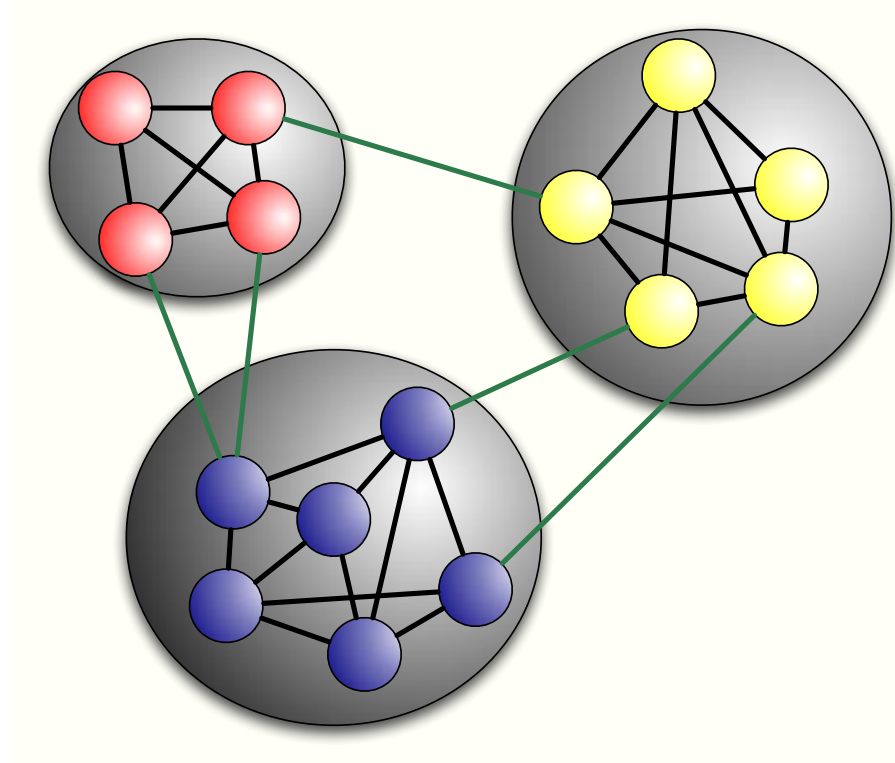
Important features
of a system and its
dynamics from
purely structural
information



Community structure

Communities: sets of tightly connected nodes

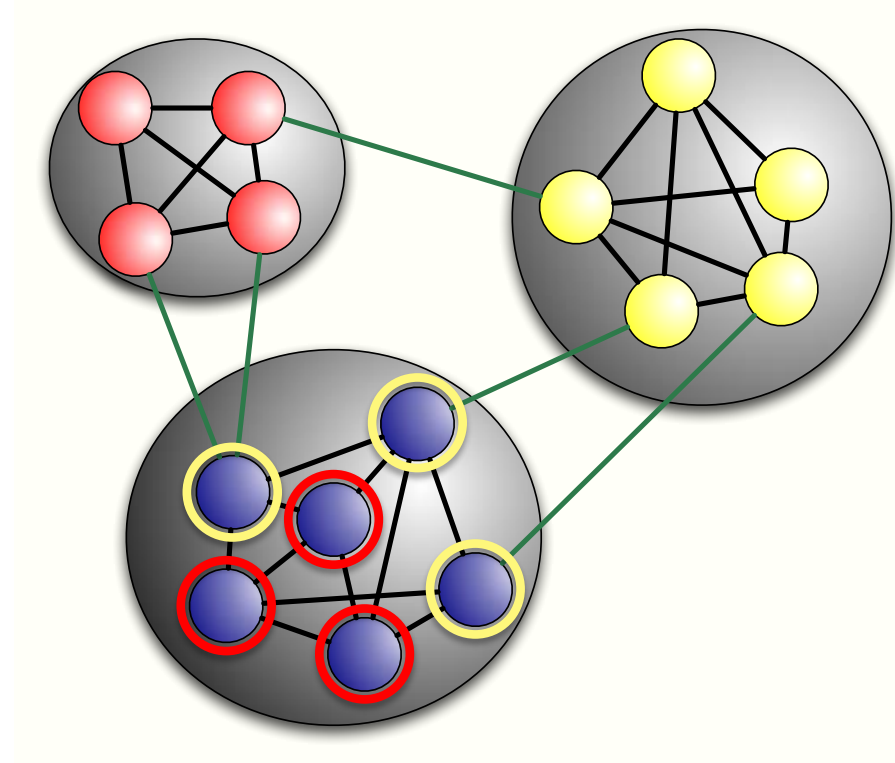
- People with common interests
- Scholars working on the same field
- Proteins with equal/similar functions
- Papers on the same/related topics
- ...



Community detection

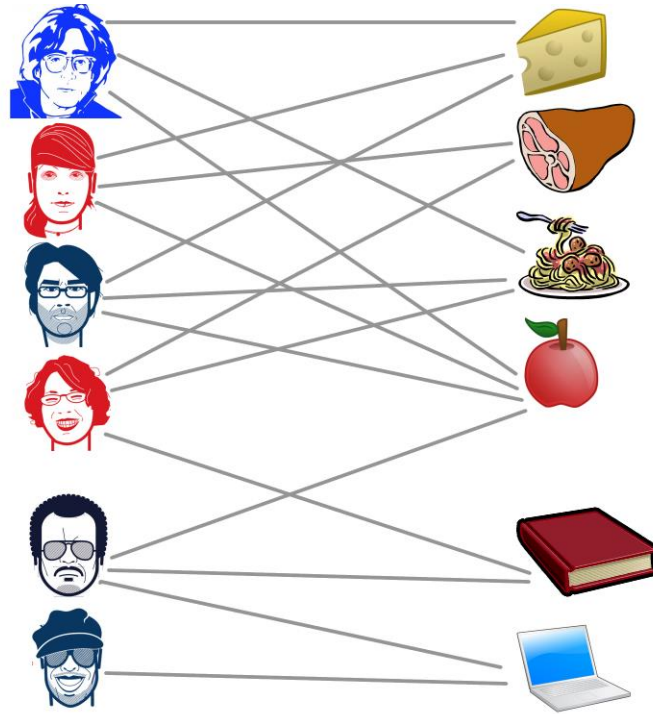
Theoretical reasons

- Organization
- Node features
- Node classification
- Missing links



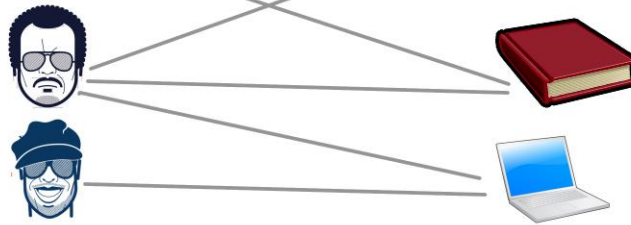
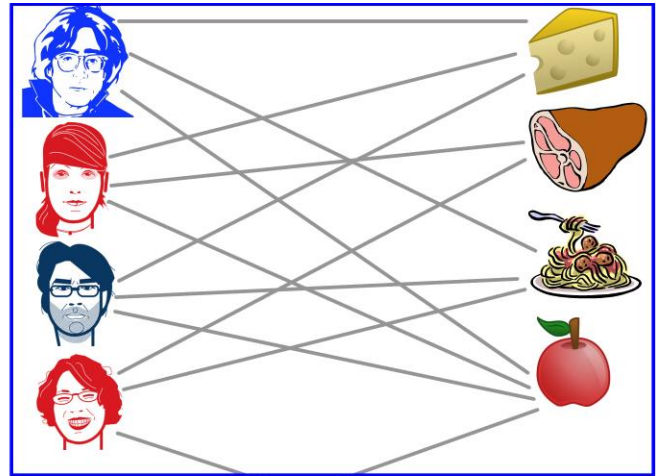
Community detection

Practical reasons: recommendation systems



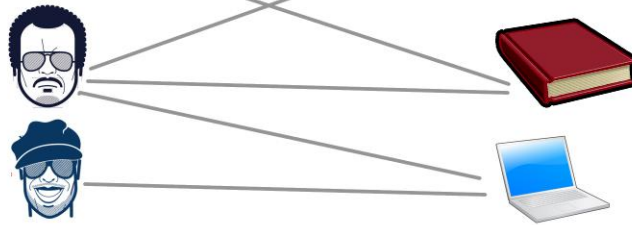
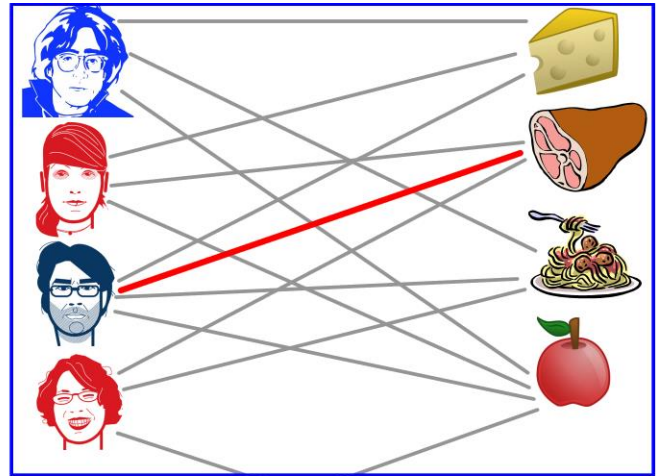
Community detection

Practical reasons: recommendation systems



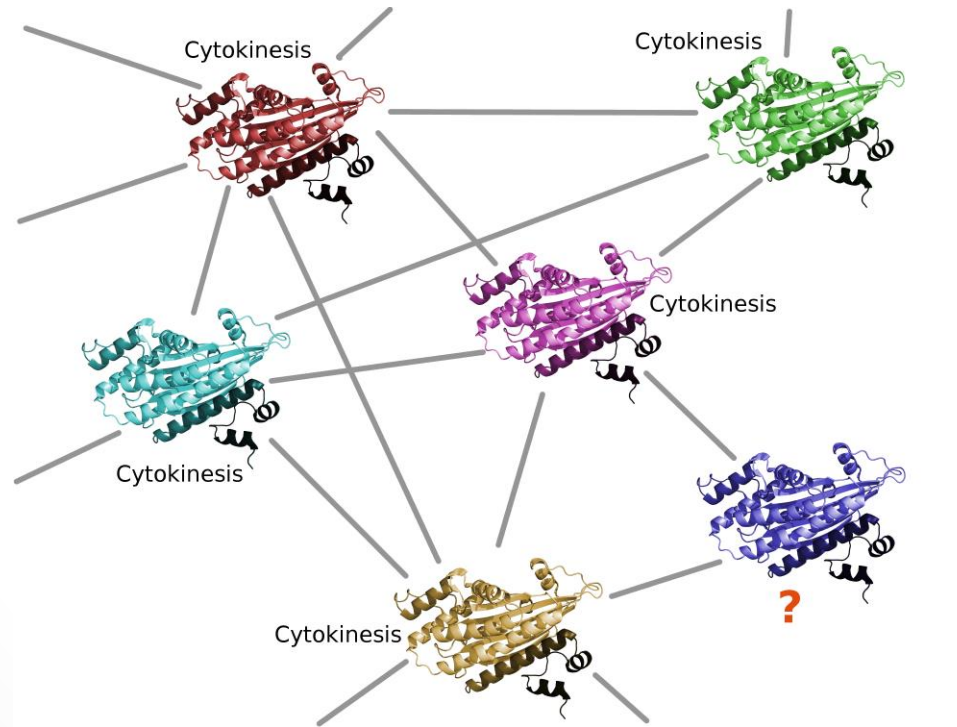
Community detection

Practical reasons: recommendation systems



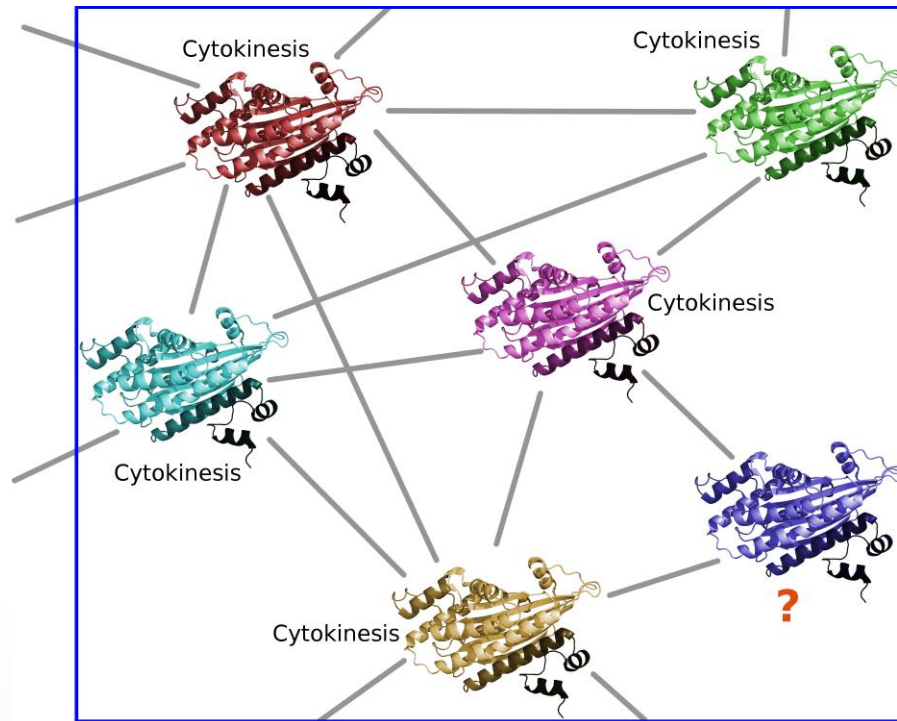
Community detection

Practical reasons: unknown protein functions



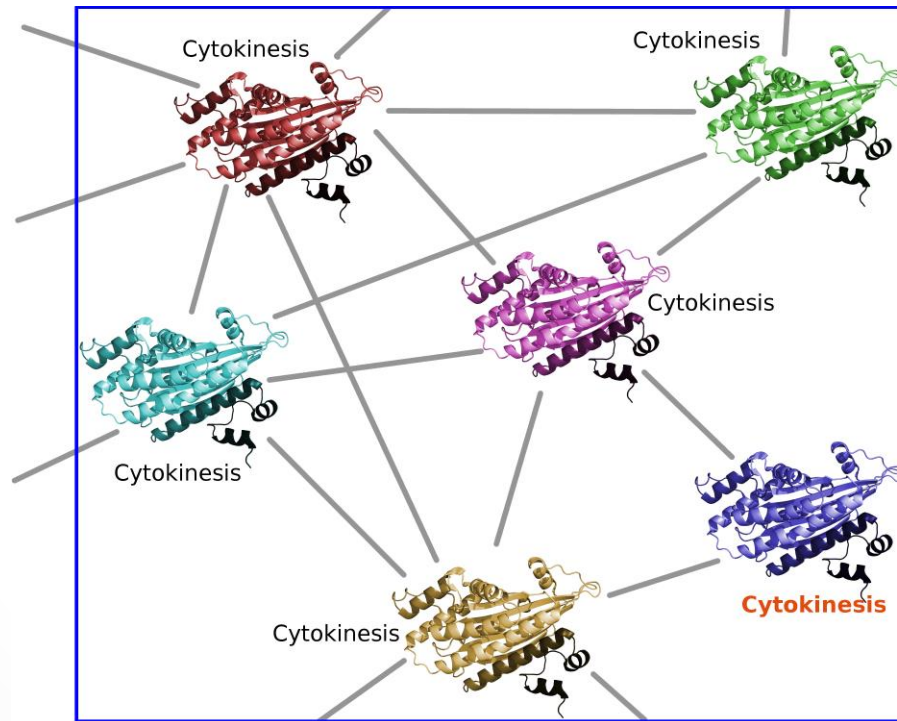
Community detection

Practical reasons: unknown protein functions

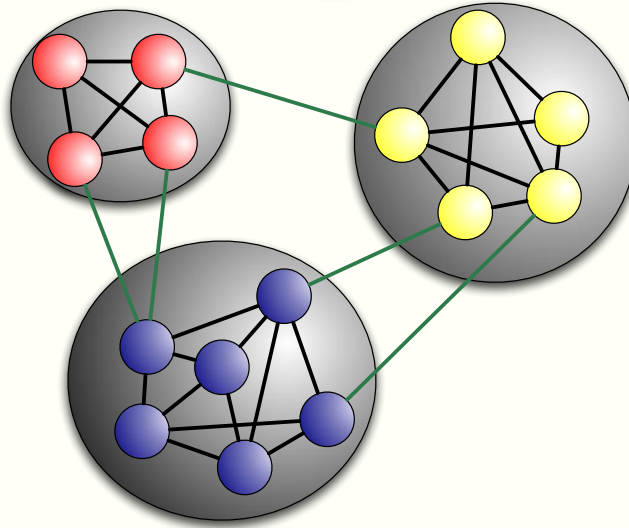


Community detection

Practical reasons: unknown protein functions



Difficult problem!



	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1								1		1	1			1	1
2						1	1							1	
3	1											1			1
4				1						1		1			1
5						1	1						1	1	
6		1						1							1
7			1						1			1	1		
8		1				1	1							1	
9			1				1					1	1		
10	1							1						1	1
11							1			1		1	1		
12			1					1		1					1
13				1			1		1				1		
14		1				1	1	1							
15	1			1		1						1			



	6	2	8	14	5	7	13	11	9	12	10	4	1	3	15
6		1	1	1											
2	1		1	1							1				
8	1	1		1	1										
14	1	1	1		1										
5			1	1		1	1			1					
7					1		1	1	1						
13					1	1		1		1					
11						1	1		1	1					
9						1		1		1			1		
12					1		1	1	1		1				
10	1											1	1	1	1
4									1	1			1		1
1								1		1	1			1	1
3										1		1			1
15											1	1	1	1	

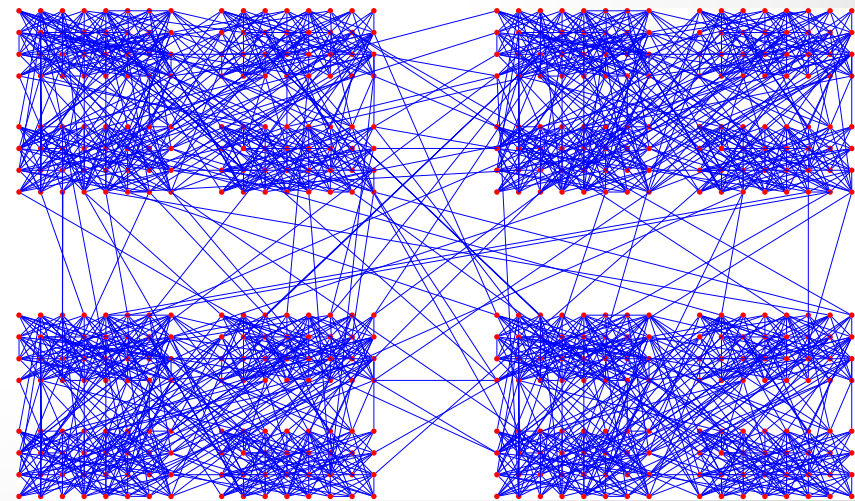
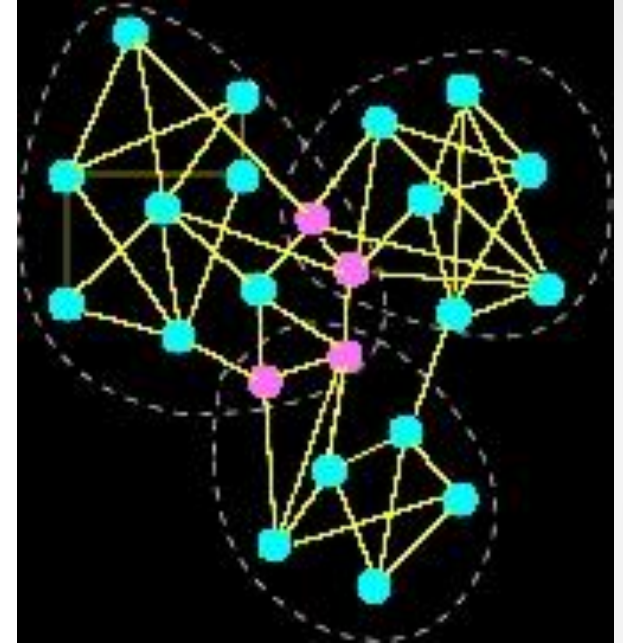
Difficult problem

Ill-defined problem:

- What is a community/partition?
- What is a *good* community/partition?

Complications:

- Link directions
- Link weights
- Overlapping communities
- Hierarchical structure



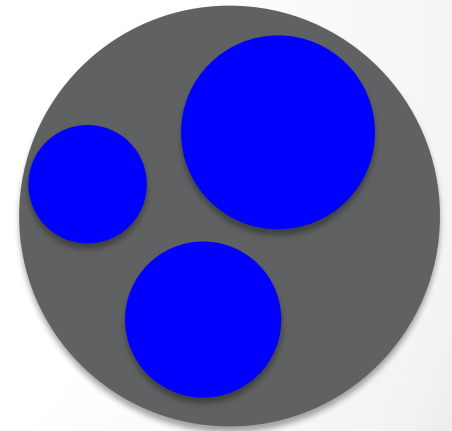
Global optimization

Principle:

- Function $Q(\mathcal{P})$ that assigns a score to each partition
- Best partition of the network \rightarrow partition corresponding to the maximum/minimum of $Q(\mathcal{P})$

Problems:

- Good partition does not imply good clusters
- Answer depends on the whole graph \rightarrow it changes if one considers portions of it or if it is incomplete



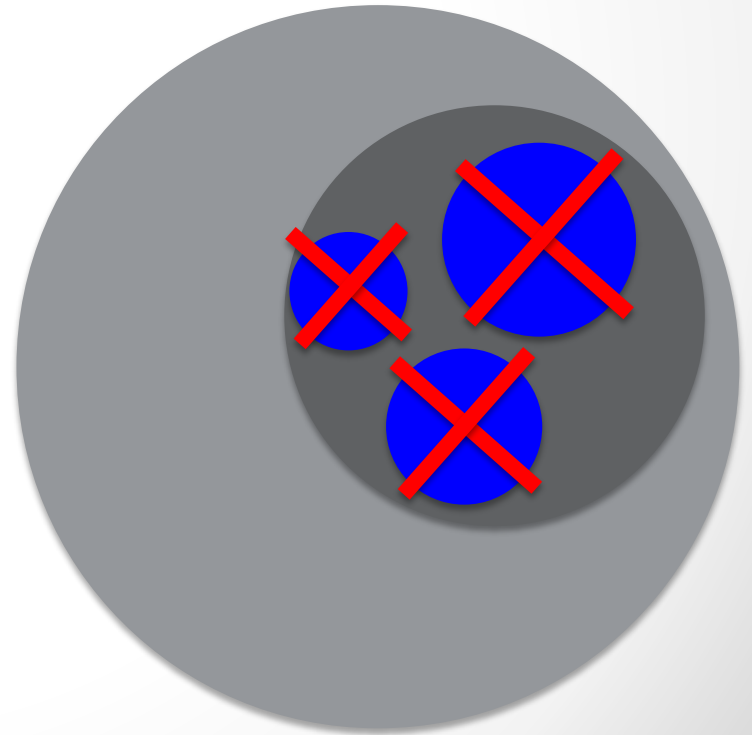
Global optimization

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Modularity optimization

$$Q = \frac{1}{m} \sum_{c=1}^{n_c} \left(l_c - \frac{d_c^2}{4m} \right)$$

M. E. J. Newman, M. Girvan, Phys. Rev. E 69, 026113 (2004)

M. E. J. Newman, Phys. Rev. E 69, 066133 (2004)

Goal: find the maximum of Q over all possible network partitions

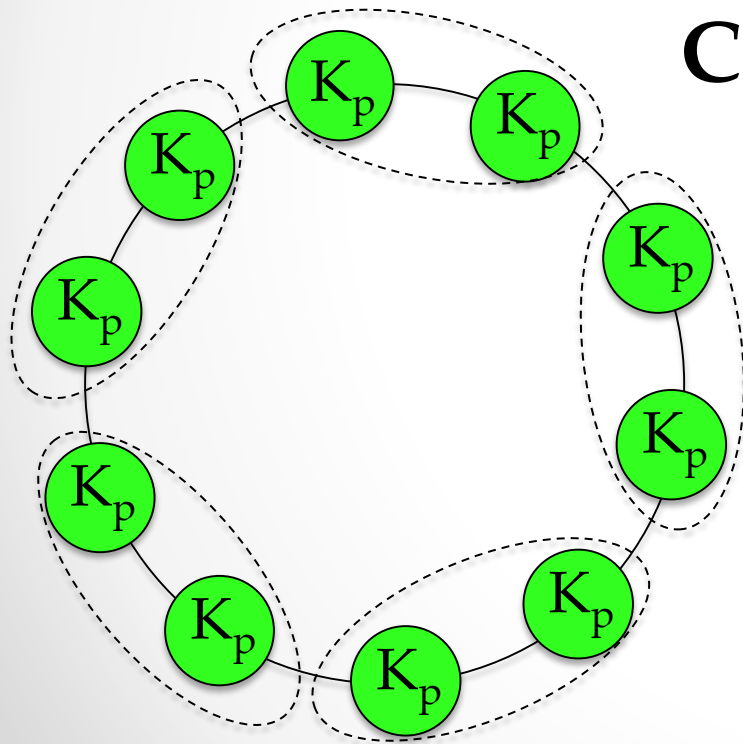
Problem: NP-complete (Brandes et al., 2007)!

Resolution limit

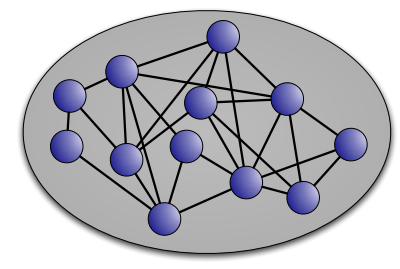
$$Q = \frac{1}{m} \sum_{c=1}^{n_c} \left[l_c - \frac{1}{4} \left(\frac{d_c}{\sqrt{m}} \right)^2 \right]$$

modularity's scale

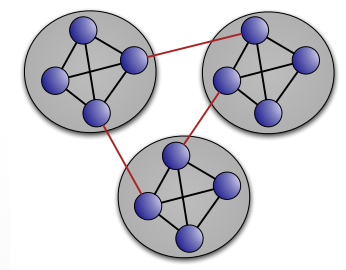
Consequences



$$d_c < \sqrt{m}$$



$$d_c < \sqrt{m}$$



?

Local optimization

Principle:

- Communities are local structures
- Local exploration of the network, involving the subgraph and its neighborhood

Advantages:

- Conceptual advantage: communities are “local”
- Absence of global scales -> no resolution limit
- One can analyze only parts of the network

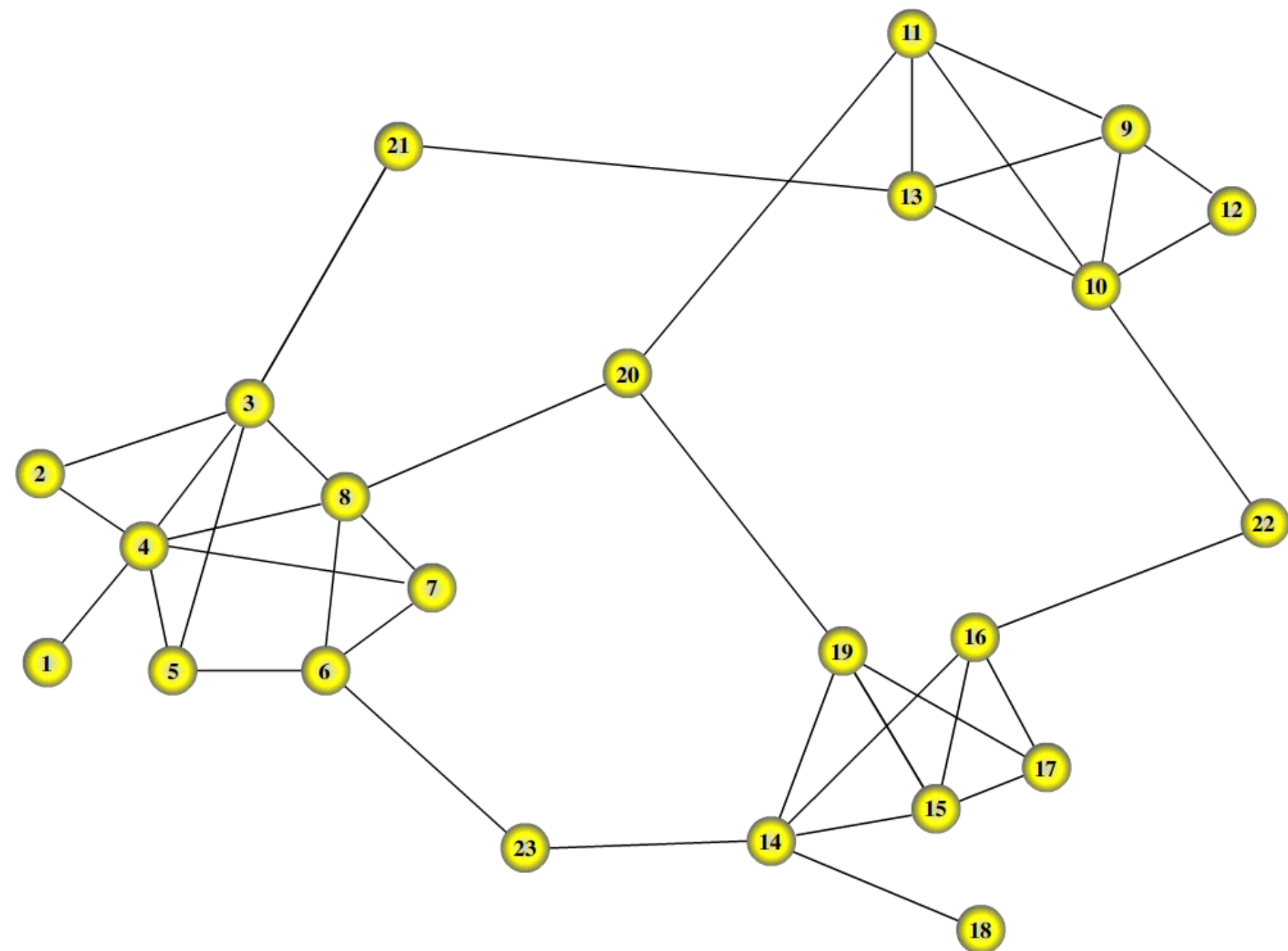
Local optimization

Implementation:

- Function $Q(C)$ that assigns a score to each subgraph
- Best cluster \rightarrow cluster corresponding to the maximum/minimum of $Q(C)$ over the set of subgraphs including a seed node

Example: Local Fitness Method (LFM)

Fitness of cluster C :
$$f_C = \frac{k_{in}^C}{(k_{in}^C + k_{out}^C)^\alpha} = \frac{2l_C}{d_C^\alpha}$$



Local optimization: OSLOM

Basics:

- LFM with fitness expressing the statistical significance of a cluster with respect to random fluctuations
- Statistical significance evaluated with Order Statistics

First multifunctional method:

- Link direction
- Link weight
- Overlapping clusters
- Hierarchy

A. Lancichinetti, F. Radicchi, J. J. Ramasco, S. F., PLoS One 6, e18961 (2011)

Local optimization: OSLOM



Order Statistics Local
Optimization Method

OSLOM

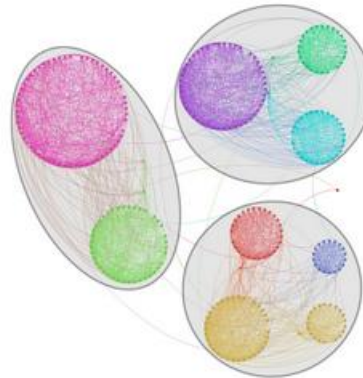
Welcome to OSLOM's Web page

OSLOM means Order Statistics Local Optimization Method and it's a clustering algorithm designed for networks.

[Download the code](#) (beta version 2.4, last update: September, 2011)

The package contains the source code and the instructions to compile and run the program. You will also get a simple script which we implemented to visualize the clusters found by OSLOM. This script writes a pajek file which in turn can be processed by [pajek](#) or [gephi](#).

This is a nice example of how the visualization looks like.



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<http://www.oslom.org/>

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collective

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Suggest Relevant Publications



Find The Clusters In Your Data

NetCom Analyzer is the first portal entirely dedicated to the analysis of community structure in networks. You can test your own algorithms, share them with the other users, and/or analyze your own datasets with the methods available in the library. You may also suggest relevant publications about community structure in networks, and publish new networked datasets with built-in communities.

[Join the Community](#)

Algorithms

FRINGE

Camilo Palazuelos, Marta Zorrilla

Clique Percolation Method

G. Palla, I. Derenyi, I. Farkas and T. Vicsek

Louvain Method

Vincent D. Blondel, Jean-Loup Guillaume, Renaud Lambiotte, Etienne Lefebvre

Edge Clustering Algorithm

Filippo Radicchi

Publications

FRINGE: a new approach to the detection of overlapping communities in graphs

Camilo Palazuelos, Marta Zorrilla

The map equation

Martin Rosvall, Daniel Axelsson, and Carl T. Bergstrom

Maps of random walks on complex networks reveal community structure

M. Rosvall and C. T. Bergstrom

Finding statistically significant communities in networks

Datasets

Zachary karate club

Vertices are members of a karate club in the United States, who were monitored during a period of three years. Edges connect members who had social interactions outside the club. W. W. Zachary, J. Anthropol. Res., 33, 452 (1977)

Dolphin social network

Vertices of the network are dolphins and two dolphins are connected if they were seen together more often than expected by chance. D. Lusseau, Proc. Royal Soc. London B, 270, S186 (2003)

American college football network

<http://www.netcom-analyzer.org/>

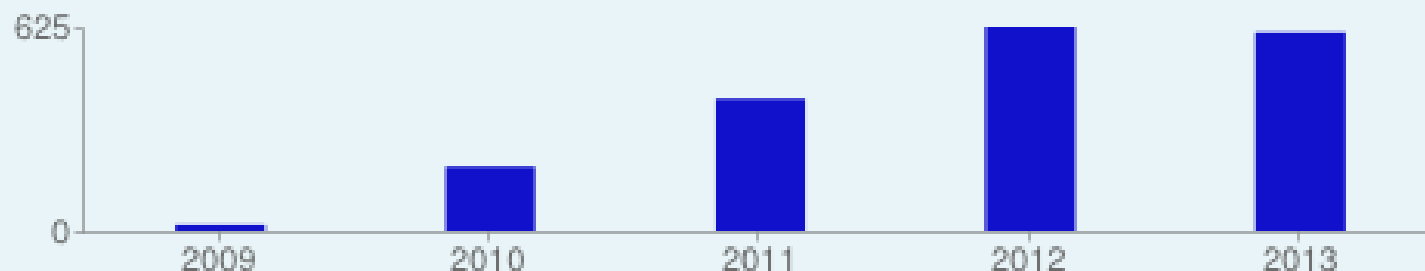
Summary

- 1) What is a community? **No unique answer! Definition is system- and problem-dependent**
- 2) Magic method? **No such thing! Domain dependent methods?**
- 3) **Global optimization** methods have important limits: **local optimization** looks more natural and promising
- 4) Attention on **validation**

Total citations

Cited by 1874

Citations per year



Scholar articles

Community detection in graphs

S Fortunato - Physics Reports, 2010

Cited by 1874 - Related articles - All 24 versions

S. F., Phys. Rep. 486,
75-174 (2010)

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Physics and Astronomy

Most Cited Physics Reports Articles

The most cited articles published since 2008, extracted from [SciVerse Scopus](#).

[Community detection in graphs](#)

Volume 486, Issues 3-5, February 2010, Pages 75-174

Fortunato, S.

The modern science of networks has brought significant advances to our understanding of complex systems. One of the most relevant features of graphs representing real systems is community structure, or clustering, i.e. the organization of vertices in clusters, with many edges joining vertices of the same cluster and comparatively few edges joining vertices of different clusters. Such clusters, or communities, can be considered as fairly independent compartments of a graph, playing a similar role like, e.g., the tissues or the organs in the human body. Detecting communities is of great importance in sociology, biology and computer science, disciplines where systems are often represented as graphs. This problem is very hard and not yet satisfactorily solved, despite the huge effort of a large interdisciplinary community of scientists working on it over the past few years. We will attempt a thorough exposition of the topic, from the definition of the main elements of the problem, to the presentation of most methods developed, with a special focus on techniques designed by statistical physicists, from the discussion of crucial issues like the significance of clustering and how methods should be tested and compared against each other, to the description of applications to real networks. © 2009 Elsevier B.V.

Acknowledgements

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Mikko Kivelä



Andrea Lancichinetti



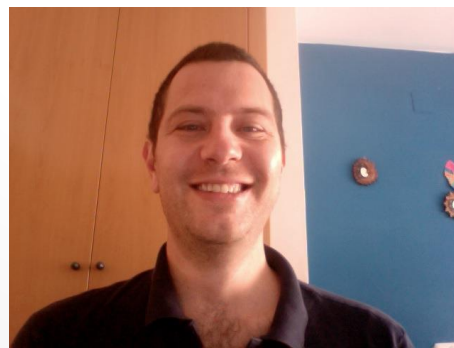
Vito Latora



Massimo Marchiori



Filippo Radicchi



José J. Ramasco



Jari Saramäki

