



# Noise-Enhanced Associative Memories

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# Neural Associative Memory

Patterns of length N



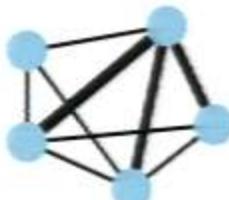
**Learning**

**No Structure**

**Correlation**

**Subspace**

$O(N)$

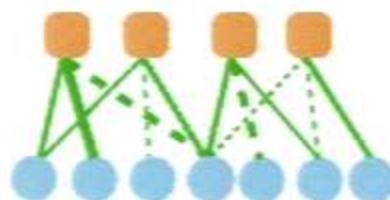


Hopefield' 82  
McEliece' 87

$\text{Poly}(N)$

Berrou' 11

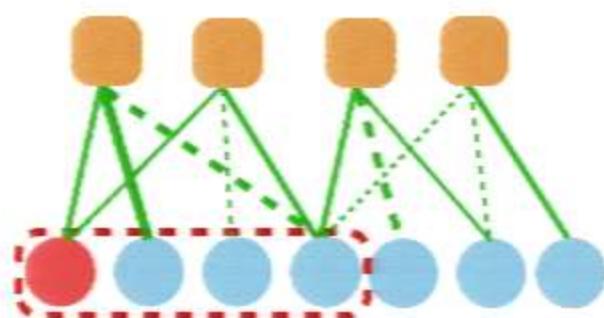
$\text{Exp}(N)$



Salavati' 12

# Noise Tolerance

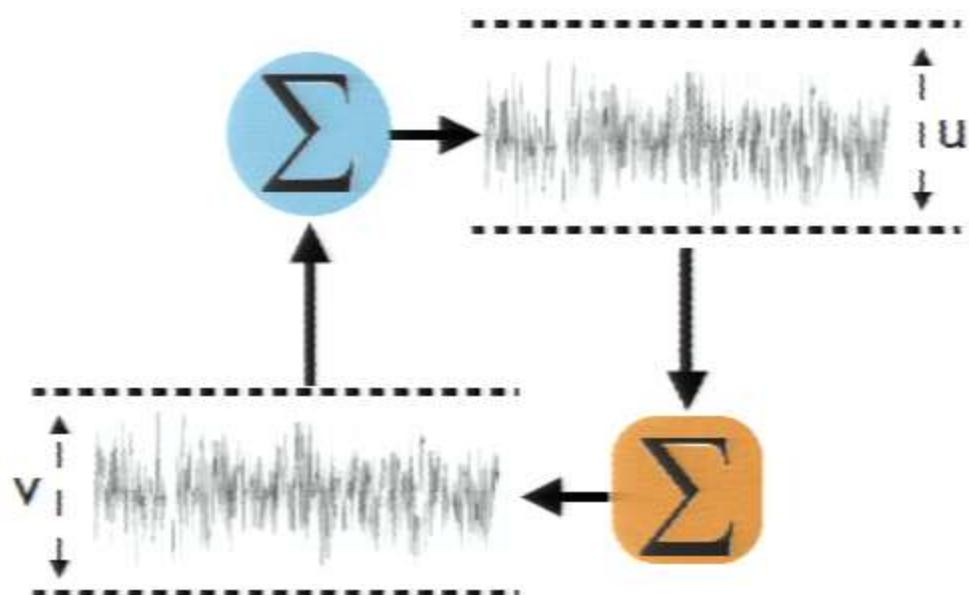
## External Noise



**Linear** fraction of corrupted elements can be corrected

Karbasi' 13

## Internal Noise

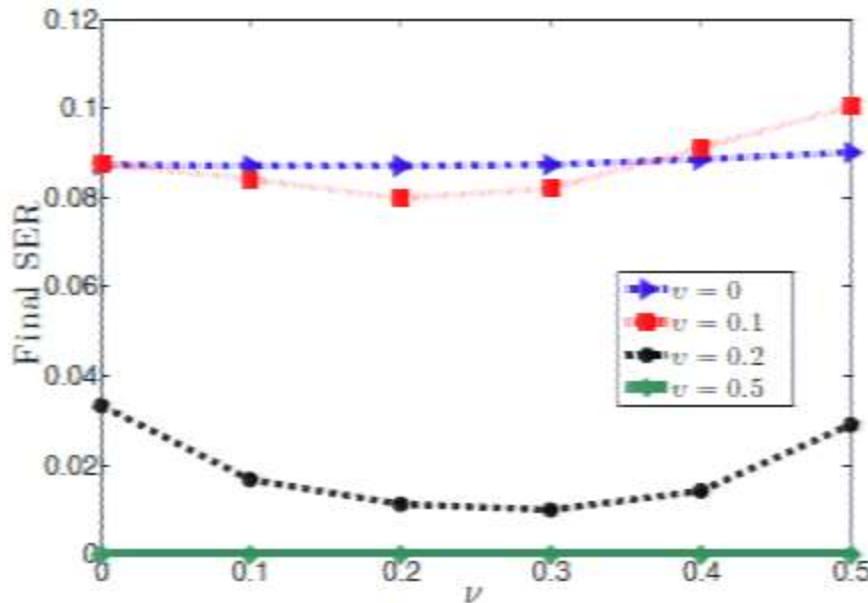
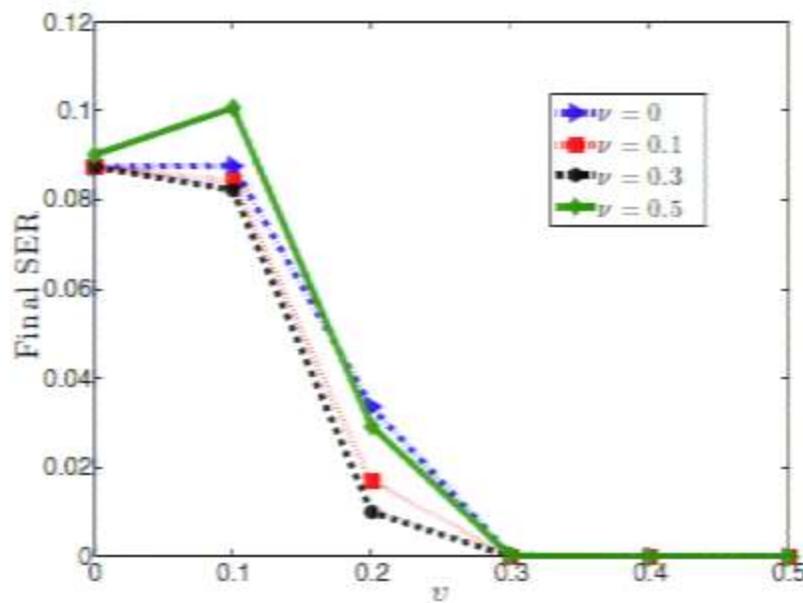


What Happens?

Amit' 94

# Surprising Effect

There are positive error levels  $(u^*, v^*)$  below which noise **improves** the recall performance.



$(u^*, v^*)$ : fixed points of a density evolution recursion

Internal noise below  $(u^*, v^*)$  does not degrade retrieval capacity