

Crisp Boundary Detection Using Pointwise Mutual Information

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## Original image


(Martin et al. 2004)


Goal: Find boundaries between image regions in a way that mimics human performance.


## How do you find a boundary?




Key observation: Pixels belonging to the same object have higher statistical association than pixels belonging to different objects.

$P(A, B)=$ how often each color A occurs next to each color B within this image.


## Pointwise mutual information (PMI)

$$
\operatorname{PMI}_{\rho}(A, B)=\log \frac{P(A, B)^{\rho}}{P(A) P(B)}
$$

Use PMI as affinity measure for affinity-based pixel grouping.

## Is PMI informative about object boundaries?



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PMI leverages internal image statistics



Internal statistics


## External statistics

## Algorithm

## Algorithm outline

1. Get affinity between pixel pairs using PMI - our contribution
2. Apply affinity-based boundary detection - standard techniques
(Arbeláez et al. 2011, gPb)

Step 1: Estimate feature co-occurrence distribution $P(A, B)$


Samples


Step 2: Derive $\operatorname{PMI}(A, B)$ from feature co-occurrence distribution

$\operatorname{PMI}(A, B)$


$$
\operatorname{PMI}_{\rho}(A, B)=\log \frac{P(A, B)^{\rho}}{P(A) P(B)}
$$

Step 3: Use PMI as affinity between each pair of nearby pixels


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## Step 4: Group pixels based on affinity (spectral clustering)



Segments


## Results



$$
\frac{1}{20}
$$

## Performance on BSDS500



> ODS: $\mathbf{0 . 7 4}$ OIS: $\mathbf{0 . 7 7}$ AP: $\mathbf{0 . 8 0}$

## Works on diverse stimuli

Cellphone photo


Satellite imagery


Art


## Boundary detection in XYT



## Summary

Pointwise mutual information is a powerful affinity measure, with applications to boundary detection and segmentation.

It is unsupervised and relies entirely on simple internal image statistics.

## Code available:

boundaries = findBoundaries(I);

## mit.edu/pmi-boundaries



