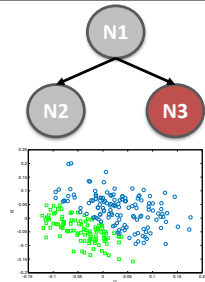
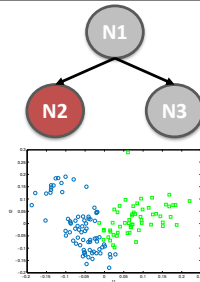
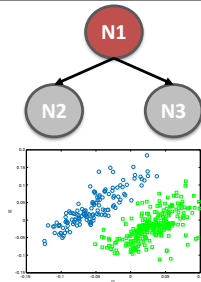


# Action Unit Intensity Estimation using Hierarchical Partial Least Squares

Tobias Gehrig\*, Ziad Al-Halah\*, Hazım Kemal Ekenel, Rainer Stiefelhagen | May 06, 2015

\* Both authors contributed equally to this study.

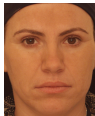
INSTITUTE FOR ANTHROPOMATICS AND ROBOTICS, COMPUTER VISION FOR HUMAN-COMPUTER INTERACTION LAB



# Motivation

How can facial expressions be described?

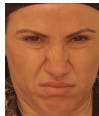
**Most popular way:** Prototypic expressions from emotions



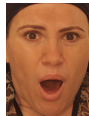
Neutral



Anger



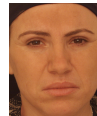
Disgust



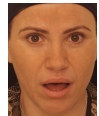
Fear



Happy



Sadness



Surprise

## Problems:

- Rarely occur in real-life in their idealized form
- Context is important:  
⇒ Judging only by face, he could be happy, but is actually frustrated





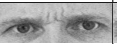



by star5112, on Flickr

# Motivation















How can facial expressions be described?

## Description without interpretation

- Facial Action Coding System (FACS) (Ekman and Friesen 1978 [1])

Upper Face Action Units						
AU 1	AU 2	AU 4	AU 5	AU 6	AU 7	
						
Inner Brow Raiser	Outer Brow Raiser	Brow Lowerer	Upper Lid Raiser	Cheek Raiser	Lid Tightener	

Lower Face Action Units						
AU 9	AU 10	AU 11	AU 12	AU 15	AU 17	AU 18
						
Nose Wrinkler	Upper Lip Raiser	Nasolabial Deepener	Lip Corner Puller	Lip Corner Depressor	Chin Raiser	Lip Pucker
AU 20	AU 23	AU 24	AU 25	AU 26	AU 27	AU 43
						
Lip Stretcher	Lip Tightener	Lip Pressor	Lips Part	Jaw Drop	Mouth Stretch	Eye Closure

Images taken from Tian et al. 2005 [5]

## ■ Intensity Estimation

0: not active	A: Trace	B: Slight	C: Marked Pronounced	D: Severe	E: Extreme Maximum
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# AU Intensity Estimation is Non-linear

- Task is non-linear due to variations in:
  - illumination
  - gender
    - eyebrow shape
  - age
    - skin texture and muscle structure
  - ethnicity
    - face shape

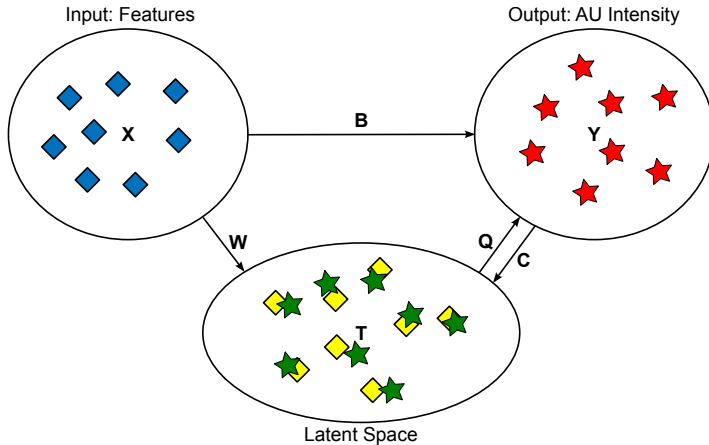


Images taken from Bosphorus database (Savran et al. 2008 [3])

- **Common approach:** specific features or non-linear machine learning
- **Drawback:** non-linear machine learning often overfits and is slow
- **Our solution:** hierarchical approach using locally linear models

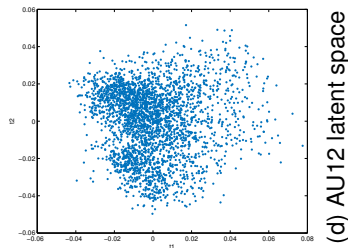
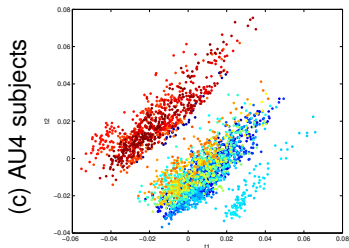
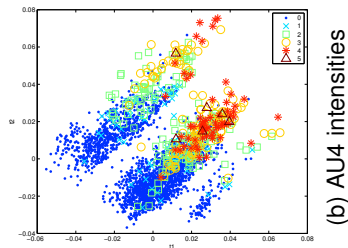
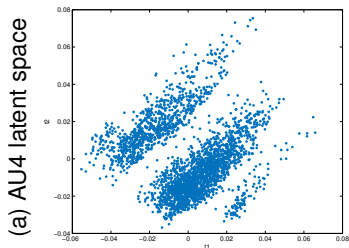


# Partial Least Square (PLS) Analysis



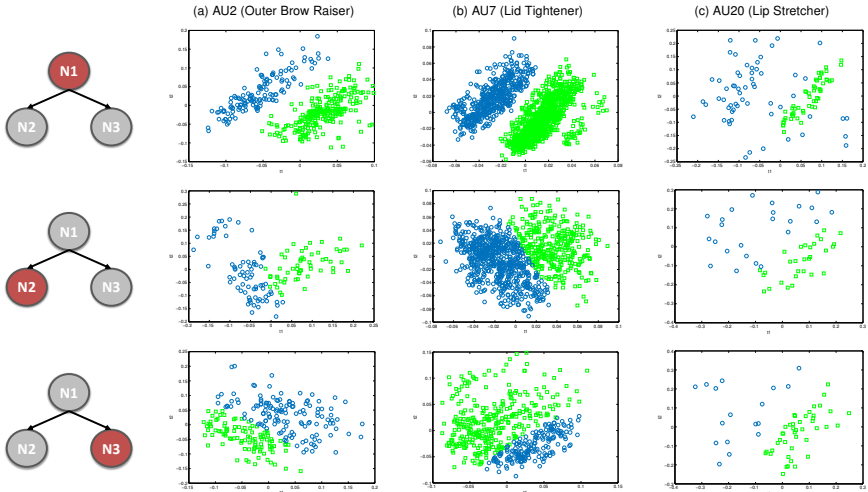
# Partial Least Square Analysis

Latent space (first two dimensions)



# Local PLS model latent spaces

First two levels of the hierarchy for different AUs



# Hierarchical PLS

## Algorithm

**input** :  $\mathbf{X}, \mathbf{Y}, (S=2)$

**output**: model

$PLS_{root} \leftarrow PLS\_fit(\mathbf{X}, \mathbf{Y})$

$(model, root) \leftarrow add\_to\_hierarchy([], PLS_{root})$

$node\_list \leftarrow push(root, node\_list)$

**while** *not is\_empty*( $node\_list$ ) **do**

$n_i \leftarrow pop(node\_list)$

$lt_{n_i} \leftarrow get\_latent\_space(\mathbf{X}_{n_i}, \mathbf{Y}_{n_i}, PLS_{n_i})$

$C_{n_i} \leftarrow cluster(lt_{n_i}, S)$

**if** *not is\_good*( $C_{n_i}$ ) **then**

        continue

**end**

**for**  $j \leftarrow 1$  to  $S$  **do**

$idx_j \leftarrow get\_cluster(j, C_{n_i})$

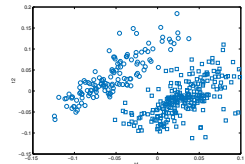
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**end**

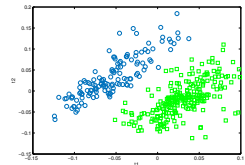
**end**



# Hierarchical PLS

## Algorithm

```
input :  $\mathbf{X}, \mathbf{Y}, (S=2)$   
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end
```



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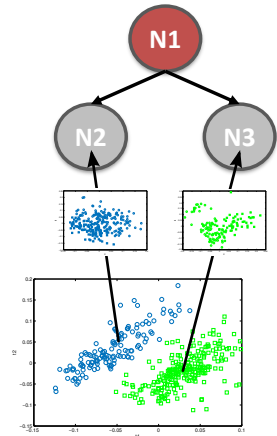
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**end**



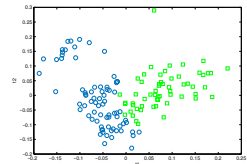
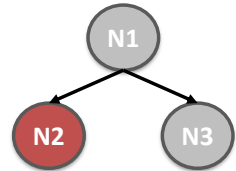
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         $node\_list \leftarrow push(n_j, node\_list)$ 
    end
end

```



# Hierarchical PLS

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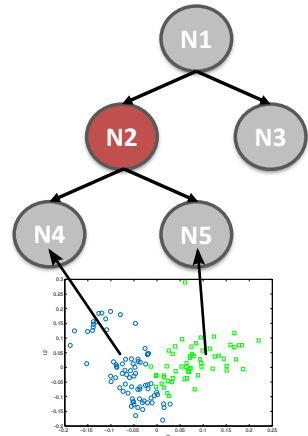
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**end**

**end**





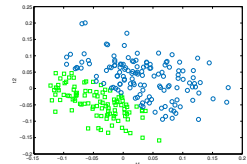
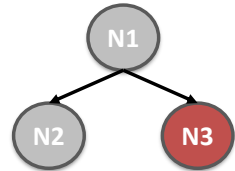
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         $(model, n_j) \leftarrow add\_to\_hierarchy(n_i, PLS_j)$ 
         $node\_list \leftarrow push(n_j, node\_list)$ 
    end
end

```



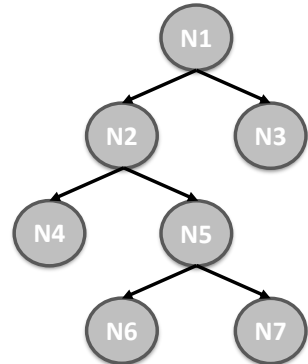
# Hierarchical PLS

## Algorithm

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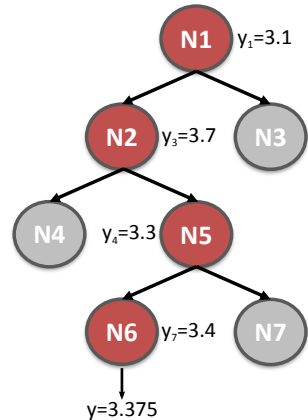
```



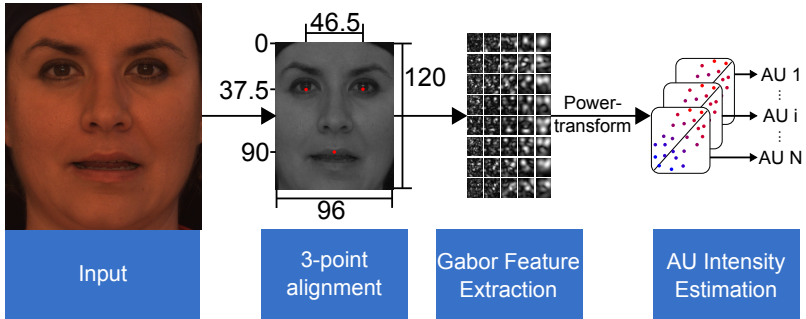
# Hierarchical PLS

## Model Combination

- Models at different levels of hierarchy are combined
- **Final estimate:** average over AU estimates in tree branch  
⇒ takes advantage of characteristics of models at each level
- Models towards root provide more stable and general estimations
- Models towards leaves are less stable but more accurate



# System Overview



	<b>Bosphorus</b>
	Savran et al. 2008 [3]
<b># Images</b>	2902
<b># Subjects</b>	105
<b># AUs</b>	43
<b>Experiment</b>	within-dataset



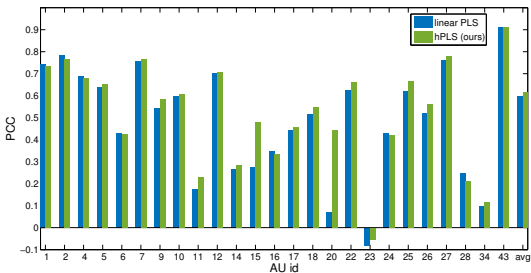
	<b>Extended Cohn-Kanade (CK+)</b>
	Lucey et al. 2010 [2]
	117
	73
	24
	across-dataset



- Official Bosphorus Benchmark (Savran et al. 2012) [4]:
  - 10-fold cross validation separately for each of 25 AUs
  - **Metric:** Pearson correlation coefficient (PCC) over all fold estimates
  - **Overall metric:** weighted sum of AU PCC values
  - **Weights:** number of samples for corresponding AU
- **Additional metric:** intraclass correlation coefficient (ICC)  
⇒ better for this task

# Within-Dataset Evaluation

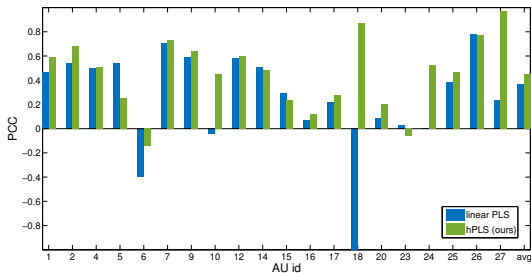
## Results on Bosphorus



Metric	hPLS (ours)	linear-PLS	RBF-PLS	Savran et al. 2012 [4]
PCC	<b>61.7</b>	59.6	60.5	57.6
ICC	<b>57.9</b>	57.3	56.0	-

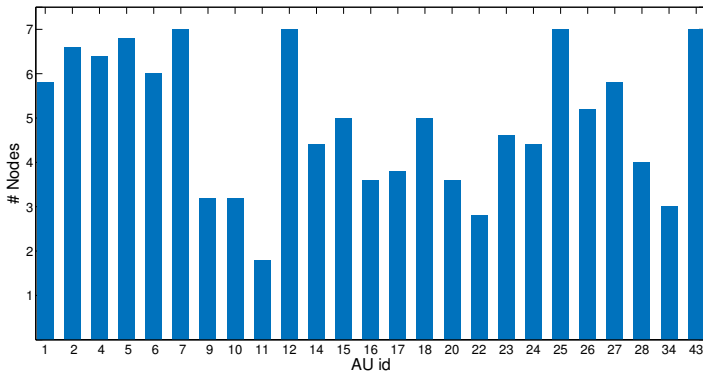
# Across-Dataset Evaluation

## Results on CK+



Metric	hPLS (ours)	linear-PLS	RBF-PLS
PCC	<b>44.9</b>	37.0	41.2
ICC	<b>41.2</b>	35.8	26.2





**Runtime:** Crossvalidation on Bosphorus incl. I/O

- Matlab implementation of hPLS: around 32 minutes
- C++ implementation of RBF kernel PLS: more than 7 hours

- Novel hierarchical locally-linear regression model for AU intensity estimation
- Automatically captures non-linear relations in data
- Adapts to varying complexity by learning suitable hierarchical structure
- Outperforms kernel-based models with lower computational costs
- Approach is generic  $\Rightarrow$  PLS can be replaced

## Action Unit Intensity Estimation using Hierarchical Partial Least Squares

Tobias Gehrig\*, Ziad Al-Halah\*, Hazım Kemal Ekenel, Rainer Stiefelhagen

\* Both authors contributed equally to this study.

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<http://cvhci.anthropomatik.kit.edu>



Paul Ekman and Wallace V. Friesen.

*Facial Action Coding System: A Technique for the Measurement of Facial Movement.*

Consulting Psychologists Press, Palo Alto, California, 1978.



P. Lucey, J. F. Cohn, T. Kanade, J. Saragih, and Z. Ambadar.

The Extended Cohn-Kanade Dataset (CK+): A complete dataset for action unit and emotion-specified expression.

*In The 3rd IEEE Workshop on CVPR for Human Communicative Behavior Analysis (CVPR4HB), 2010.*



A. Savran, N. Alyüz, H. Dibeklioglu, O. Çeliktutan, B. Gökberk, B. Sankur, and L. Akarun.

**Bosphorus Database for 3D Face Analysis.**

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A. Savran, B. Sankur, and M. T. Bilge.

**Regression-based Intensity Estimation of Facial Action Units.**

*Image and Vision Computing, 2012.*



Y.-L. Tian, T. Kanade, and J. F. Cohn.

***Facial Expression Analysis*, chapter 11.**

Springer, 2005.

## Motivation

How can facial expressions be described?

## Approach

AU Intensity Estimation is Non-linear  
Partial Least Squares (PLS) Analysis  
Hierarchical PLS (hPLS)

## Experiments

System Overview  
Datasets  
Evaluation Setup  
Within-Dataset Evaluation  
Across-Dataset Evaluation  
Computational Efficiency

## Conclusions